

Figure 8.3

Basic action of insertion sort (the shaded part is sorted)

| Array Position | 0 | 1 | 2 | 3 | 4 | 5 |
|---------------------------|---|---|---|---|---|---|
| Initial State | 8 | 5 | 9 | 2 | 6 | 3 |
| After $a[0..1]$ is sorted | 5 | 8 | 9 | 2 | 6 | 3 |
| After $a[0..2]$ is sorted | 5 | 8 | 9 | 2 | 6 | 3 |
| After $a[0..3]$ is sorted | 2 | 5 | 8 | 9 | 6 | 3 |
| After $a[0..4]$ is sorted | 2 | 5 | 6 | 8 | 9 | 3 |
| After $a[0..5]$ is sorted | 2 | 3 | 5 | 6 | 8 | 9 |

Figure 8.4

A closer look at the action of insertion sort (the dark shading indicates the sorted area; the light shading is where the new element was placed).

| Array Position | 0 | 1 | 2 | 3 | 4 | 5 |
|-------------------------|---|---|---|---|---|---|
| Initial State | 8 | 5 | | | | |
| After a[0..1] is sorted | 5 | 8 | 9 | | | |
| After a[0..2] is sorted | 5 | 8 | 9 | 2 | | |
| After a[0..3] is sorted | 2 | 5 | 8 | 9 | 6 | |
| After a[0..4] is sorted | 2 | 5 | 6 | 8 | 9 | 3 |
| After a[0..5] is sorted | 2 | 3 | 5 | 6 | 8 | 9 |

Insertion Sort

```
public static void insertionSort( Comparable [ ] a )
{
    for( int p = 1; p < a.length; p++ )
    {
        Comparable tmp = a[ p ];
        int j = p;

        for( ; j > 0 && tmp.compareTo( a[ j - 1 ] ) < 0; j-- )
            a[ j ] = a[ j - 1 ];
        a[ j ] = tmp;
    }
}
```

Figure 8.5

Shellsort after each pass if the increment sequence is {1, 3, 5}

| | | | | | | | | | | | | | |
|--------------|----|----|----|----|----|----|----|----|----|----|----|----|----|
| ORIGINAL | 81 | 94 | 11 | 96 | 12 | 35 | 17 | 95 | 28 | 58 | 41 | 75 | 15 |
| After 5-sort | 35 | 17 | 11 | 28 | 12 | 41 | 75 | 15 | 96 | 58 | 81 | 94 | 95 |
| After 3-sort | 28 | 12 | 11 | 35 | 15 | 41 | 58 | 17 | 94 | 75 | 81 | 96 | 95 |
| After 1-sort | 11 | 12 | 15 | 17 | 28 | 35 | 41 | 58 | 75 | 81 | 94 | 95 | 96 |

ShellSort

```
public static void shellsort( Comparable [ ] a )
{
    for( int gap = a.length / 2; gap > 0;
        gap = gap == 2 ? 1 : (int) ( gap / 2.2 ) )
        for( int i = gap; i < a.length; i++ )
        {
            Comparable tmp = a[ i ];
            int j = i;

            for( ; j >= gap && tmp.compareTo( a[ j - gap ] ) < 0; j -= gap )
                a[ j ] = a[ j - gap ];
            a[ j ] = tmp;
        }
}
```

Merge Sort

```
public static void mergeSort( Comparable [ ] a ) {  
    Comparable [ ] tmpArray = new Comparable[ a.length ];  
    mergeSort( a, tmpArray, 0, a.length - 1 );  
}  
private static void mergeSort( Comparable [ ] a, Comparable [ ]  
    tmpArray,  
    int left, int right )  
{  
    if( left < right )  
    {  
        int center = ( left + right ) / 2;  
        mergeSort( a, tmpArray, left, center );  
        mergeSort( a, tmpArray, center + 1, right );  
        merge( a, tmpArray, left, center + 1, right );  
    }  
}
```

Merge in Merge Sort

```
private static void merge( Comparable [ ] a, Comparable [ ] tmpArray,
                          int leftPos, int rightPos, int rightEnd )
{
    int leftEnd = rightPos - 1;
    int tmpPos = leftPos;
    int numElements = rightEnd - leftPos + 1;
    while( leftPos <= leftEnd && rightPos <= rightEnd )
        if( a[ leftPos ].compareTo( a[ rightPos ] ) < 0 )
            tmpArray[ tmpPos++ ] = a[ leftPos++ ];
        else
            tmpArray[ tmpPos++ ] = a[ rightPos++ ];
    while( leftPos <= leftEnd ) // Copy rest of first half
        tmpArray[ tmpPos++ ] = a[ leftPos++ ];
    while( rightPos <= rightEnd ) // Copy rest of right half
        tmpArray[ tmpPos++ ] = a[ rightPos++ ];

    for( int i = 0; i < numElements; i++, rightEnd-- )
        a[ rightEnd ] = tmpArray[ rightEnd ];
}
```

Figure 8.10 Quicksort

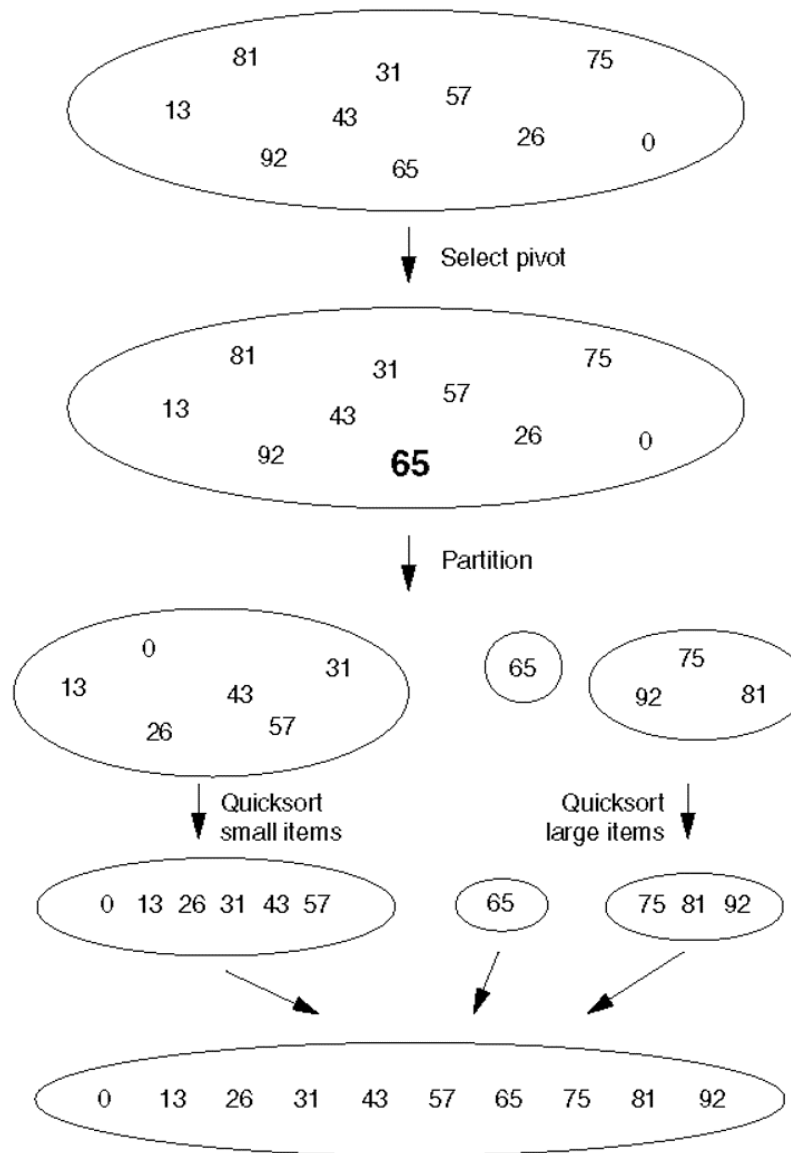


Figure 8.11 Partitioning algorithm: Pivot element 6 is placed at the end.

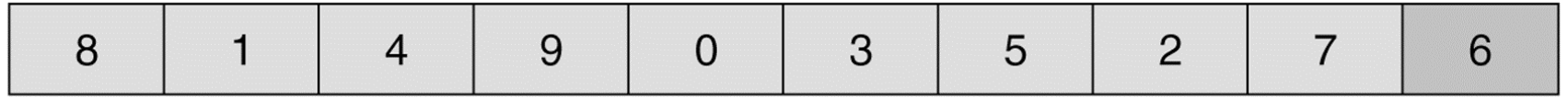


Figure 8.12 Partitioning algorithm: i stops at large element 8; j stops at small element 2.

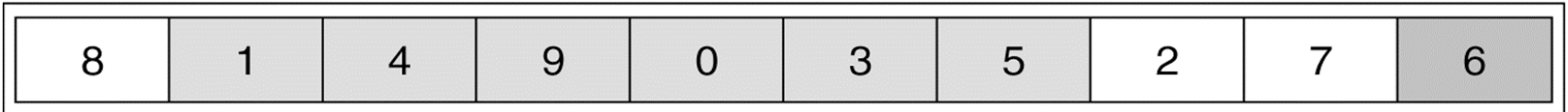


Figure 8.13 Partitioning algorithm: The out-of-order elements 8 and 2 are swapped.

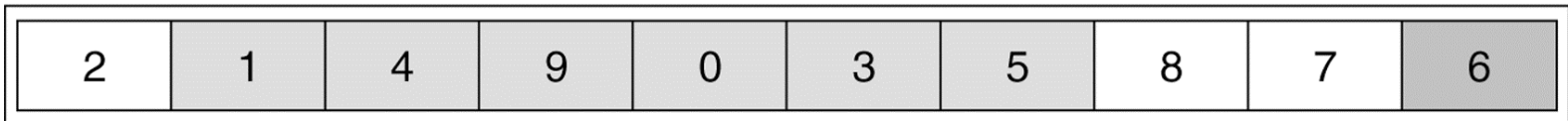


Figure 8.14 Partitioning algorithm: i stops at large element 9; j stops at small element 5.

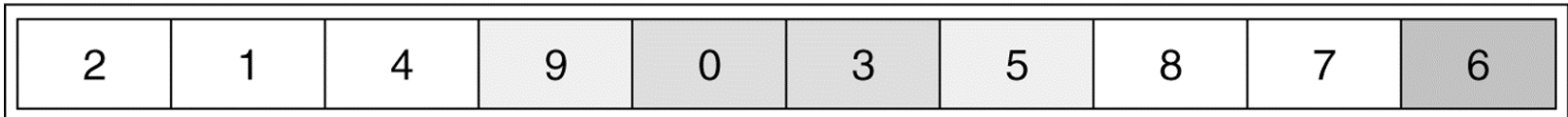


Figure 8.15 Partitioning algorithm: The out-of-order elements 9 and 5 are swapped.

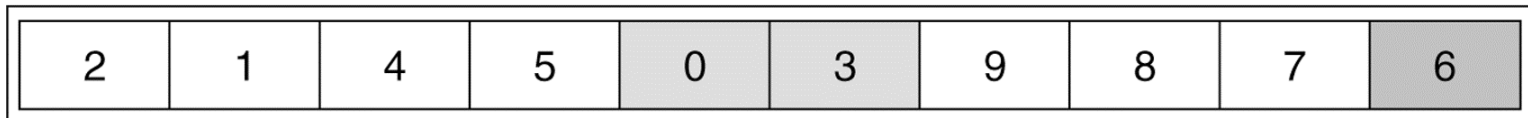


Figure 8.16 Partitioning algorithm: i stops at large element 9; j stops at small element 3.

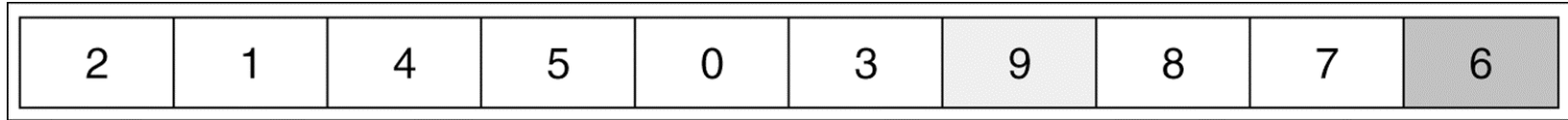


Figure 8.17 Partitioning algorithm: Swap pivot and element in position i.

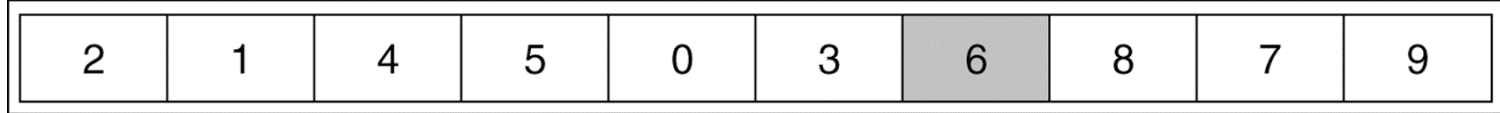


Figure 8.18 Original array

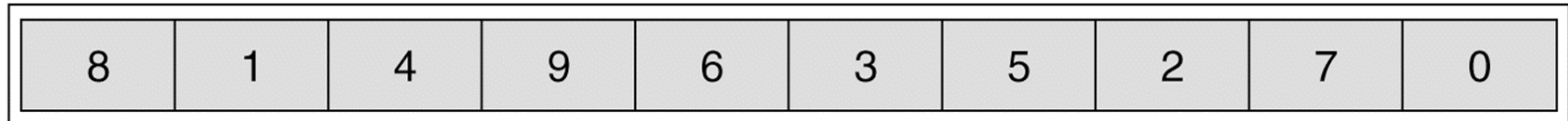


Figure 8.19 Result of sorting three elements (first, middle, and last)

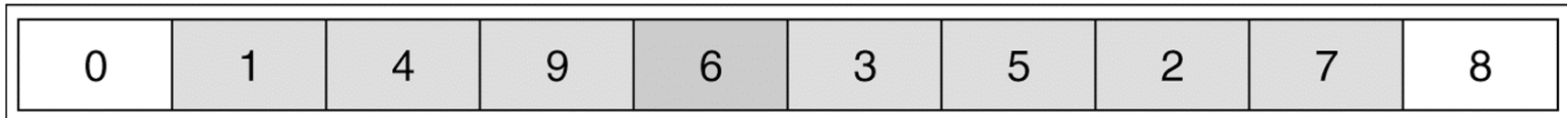
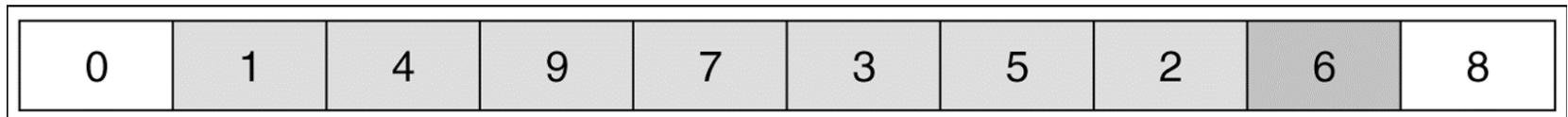


Figure 8.20 Result of swapping the pivot with the next-to-last element



Quicksort

```
public static void quicksort( Comparable [ ] a ) { quicksort( a, 0, a.length - 1 ); }
private static void quicksort( Comparable [ ] a, int low, int high )
{
    if( low + CUTOFF > high ) insertionSort( a, low, high );
    else { // Sort low, middle, high
        int middle = ( low + high ) / 2;
        if( a[ middle ].compareTo( a[ low ] ) < 0 ) swapReferences( a, low, middle );
        if( a[ high ].compareTo( a[ low ] ) < 0 ) swapReferences( a, low, high );
        if( a[ high ].compareTo( a[ middle ] ) < 0 ) swapReferences( a, middle, high );
        swapReferences( a, middle, high - 1 ); // Place pivot at position high - 1
        Comparable pivot = a[ high - 1 ];
        int i, j; // Begin partitioning
        for( i = low, j = high - 1; ; ) {
            while( a[ ++i ].compareTo( pivot ) < 0 ) /* Do nothing */ ;
            while( pivot.compareTo( a[ --j ] ) < 0 ) /* Do nothing */ ;
            if( i >= j ) break;
            swapReferences( a, i, j );
        }
        swapReferences( a, i, high - 1 );
        quicksort( a, low, i - 1 ); // Sort small elements
        quicksort( a, i + 1, high ); // Sort large elements
    }
}
```