





Rec	-Black Trees
$\label{eq:response} \begin{array}{l} \hline RB-Insert (T,z) \qquad // \ gg 261 \\ // \ Insert node z \ in tree T \\ y = NIL \\ x = root[T] \\ while (x \neq NIL) \ do \\ y = x \\ if (key[z] < key[x]) \\ x = left[x] \\ x = right[x] \\ p[z] = y \\ if (y = z NIL) \\ root[T] = z \\ else \ ight[y] = z \\ else \ ight[y] = z \\ // \ new \ stuff \\ left[y] = x \\ left[y] = x \\ left[y] = x \\ right[z] = NIL[T] \\ right[z] = NIL[T] \\ right[z] = NIL[T] \\ right[z] = NIL[T] \\ right[z] = RED \\ RB-Insert-Fixue (Tz) \\ \end{array}$	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$



	Rotations
LeftRotate(T,x) // p // right child of x b // Subtrees need to y = right[x]	<u>g 278</u> ecomes x's parent. b be readjusted.
right[x] = left[y] p[left[y]] = x p[y] = p[x]	// y's left subtree becomes x's right
if (p[x] == NIL[T]) t root[T] = y else if (x == left[p[>	rhen (]]) then
lett[p[x]] = y else right[p[x]] = y left[y] = x p[x] = y	
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- Why is it needed?
 - Because basic data structures not enough for all operations
 storing extra information helps execute special operations more efficiently.

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- Can any data structure be augmented?
 Yes. Any data structure can be augmented.
- Can a data structure be augmented with any additional information?

- Theoretically, yes.

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 How to choose which additional information to store.
 Only if we can maintain the additional information efficiently under all operations. That means, with additional information, we need to perform old and new operations efficiently maintain the additional information efficiently.

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- 1. choose an underlying data structure
- determine additional information to be maintained in the underlying data structure,
- 3. develop new operations,
- verify that the additional information can be maintained for the modifying operations on the underlying data structure.

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OS-Select	
OS-SELECT(x i) //page 304	
// Select the node with rank i	
// in the subtree rooted at x	
1. r = size[left[x]]+1	
2. if i = r then	
3. return x	
4. elseif i < r then	
return OS-SELECT (left[x], i)	
6. else return OS-SELECT (right[x], i-r)	
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