

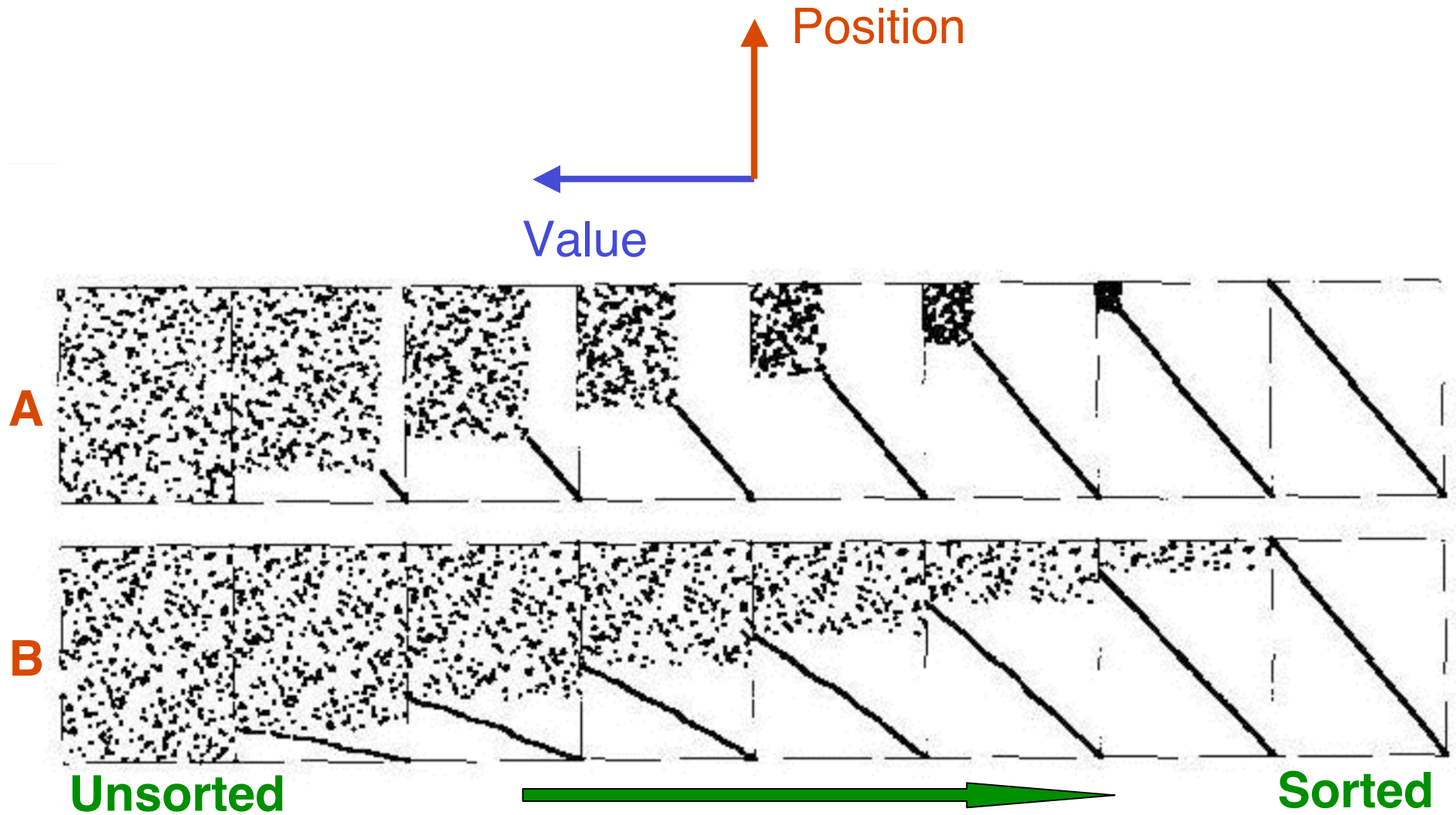
Sorting Algorithms

- Number of Comparisons
- Number of Data Movements
- Additional Space Requirements

Sorting Algorithms

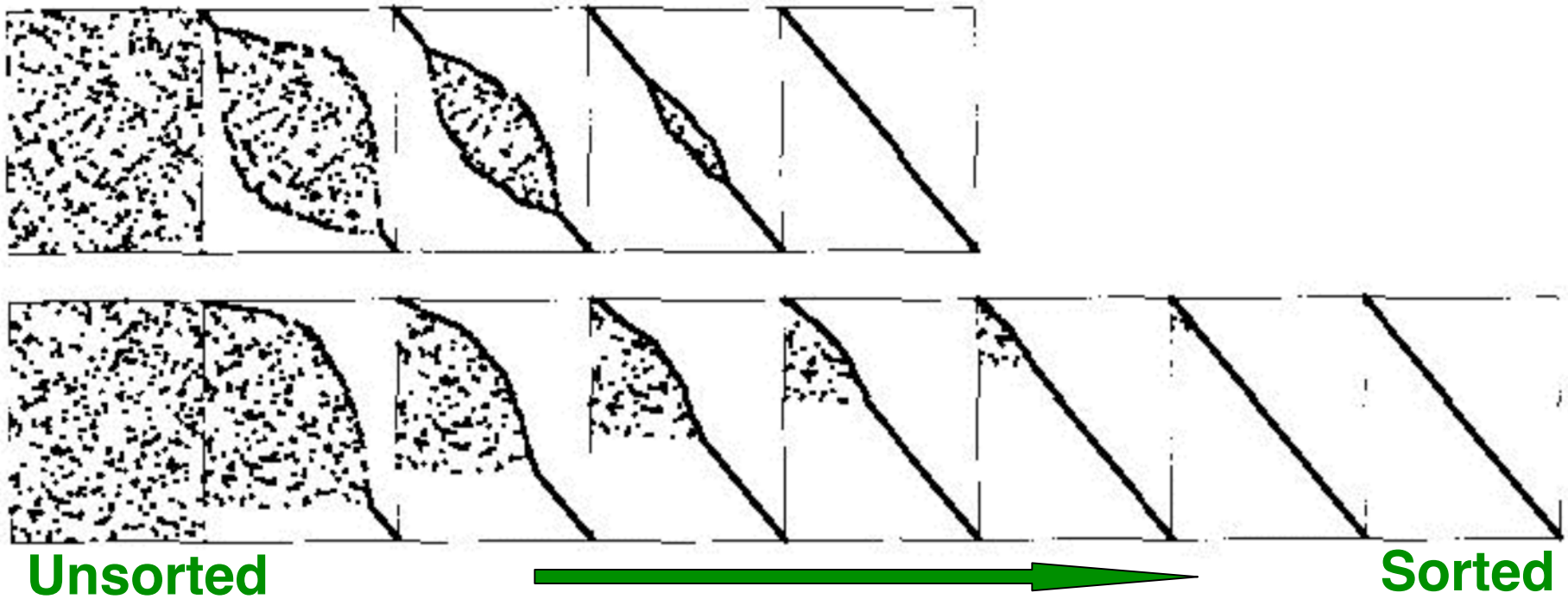
- SelectionSort
- InsertionSort
- BubbleSort
- ShakerSort
- QuickSort
- MergeSort
- HeapSort
- Bucket & Radix Sort
- Counting Sort

Visualizing Algorithms 1

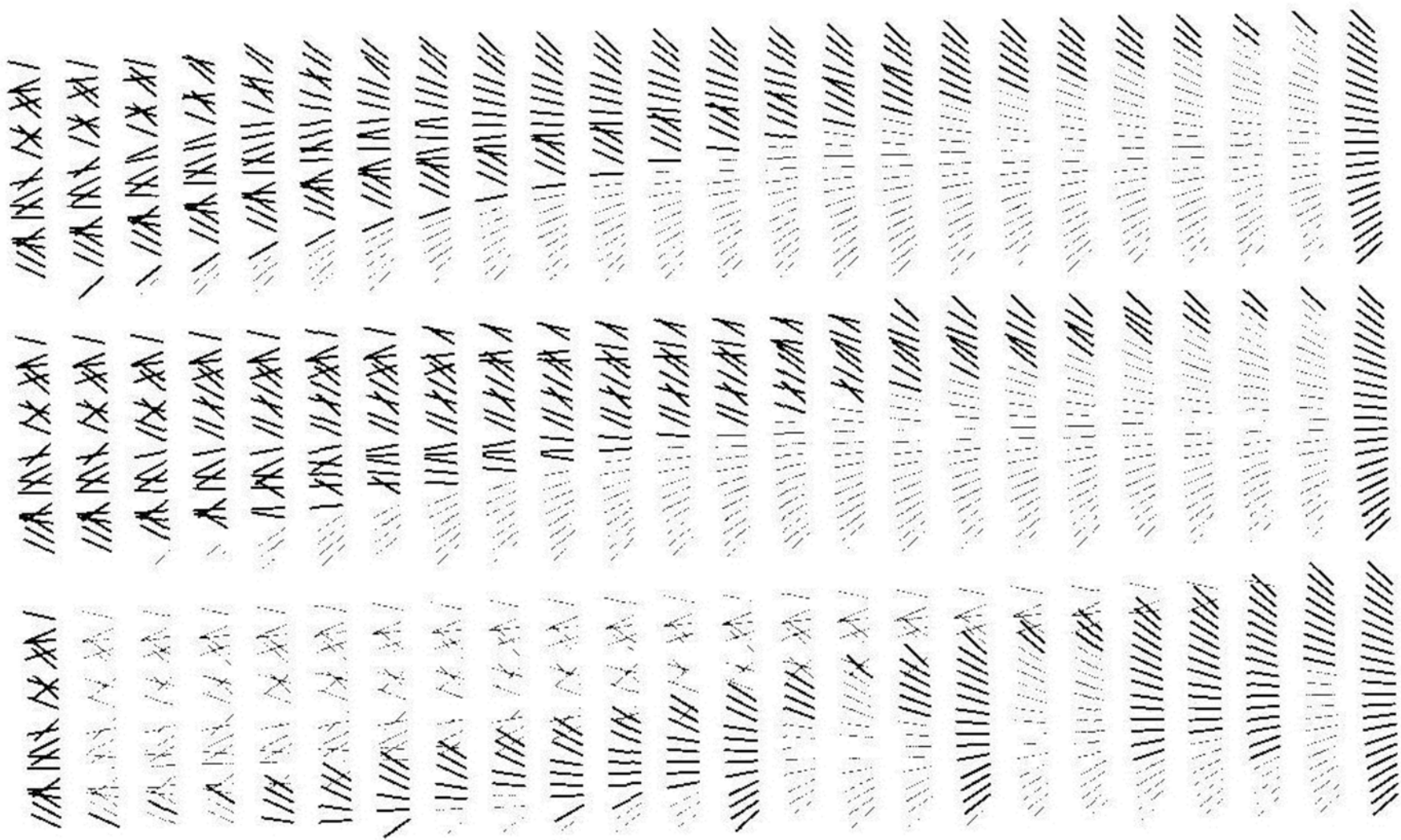


Visualizing Algorithms 2

Position
Value



Visualizing Comparisons 3



Animation Demos

<http://cg.scs.carleton.ca/~morin/misc/sortalg/>

Comparing $O(n^2)$ Sorting Algorithms

- InsertionSort and SelectionSort (and ShakerSort) are roughly twice as fast as BubbleSort for small files.
- InsertionSort is the best for very small files.
- $O(n^2)$ sorting algorithms are **NOT** useful for large random files.
- If **comparisons** are very expensive, then among the $O(n^2)$ sorting algorithms, insertionsort is best.
- If **data movements** are very expensive, then among the $O(n^2)$ sorting algorithms, ?? is best.

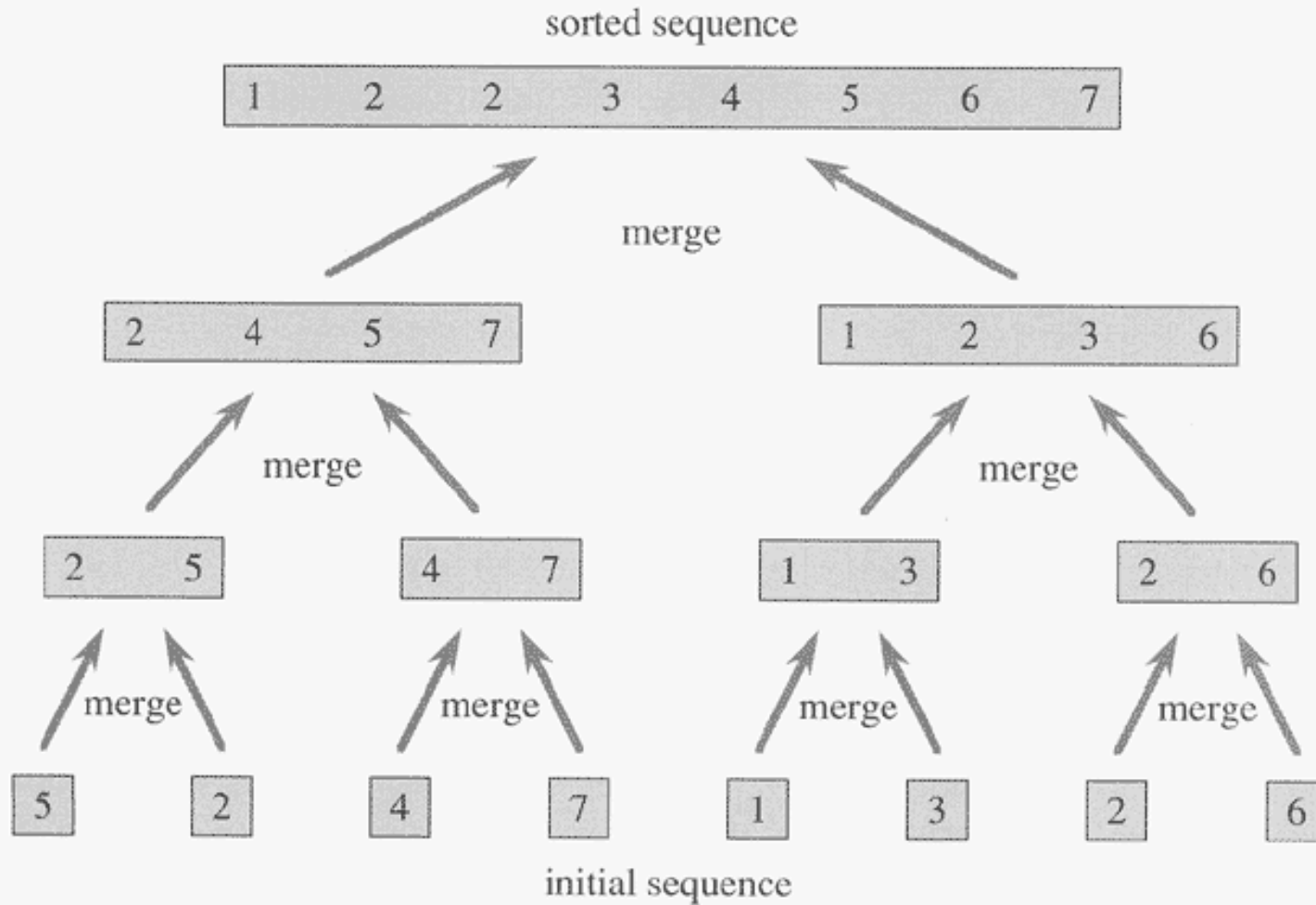


Figure 2.4 The operation of merge sort on the array $A = \langle 5, 2, 4, 7, 1, 3, 2, 6 \rangle$. The lengths of the sorted sequences being merged increase as the algorithm progresses from bottom to top.

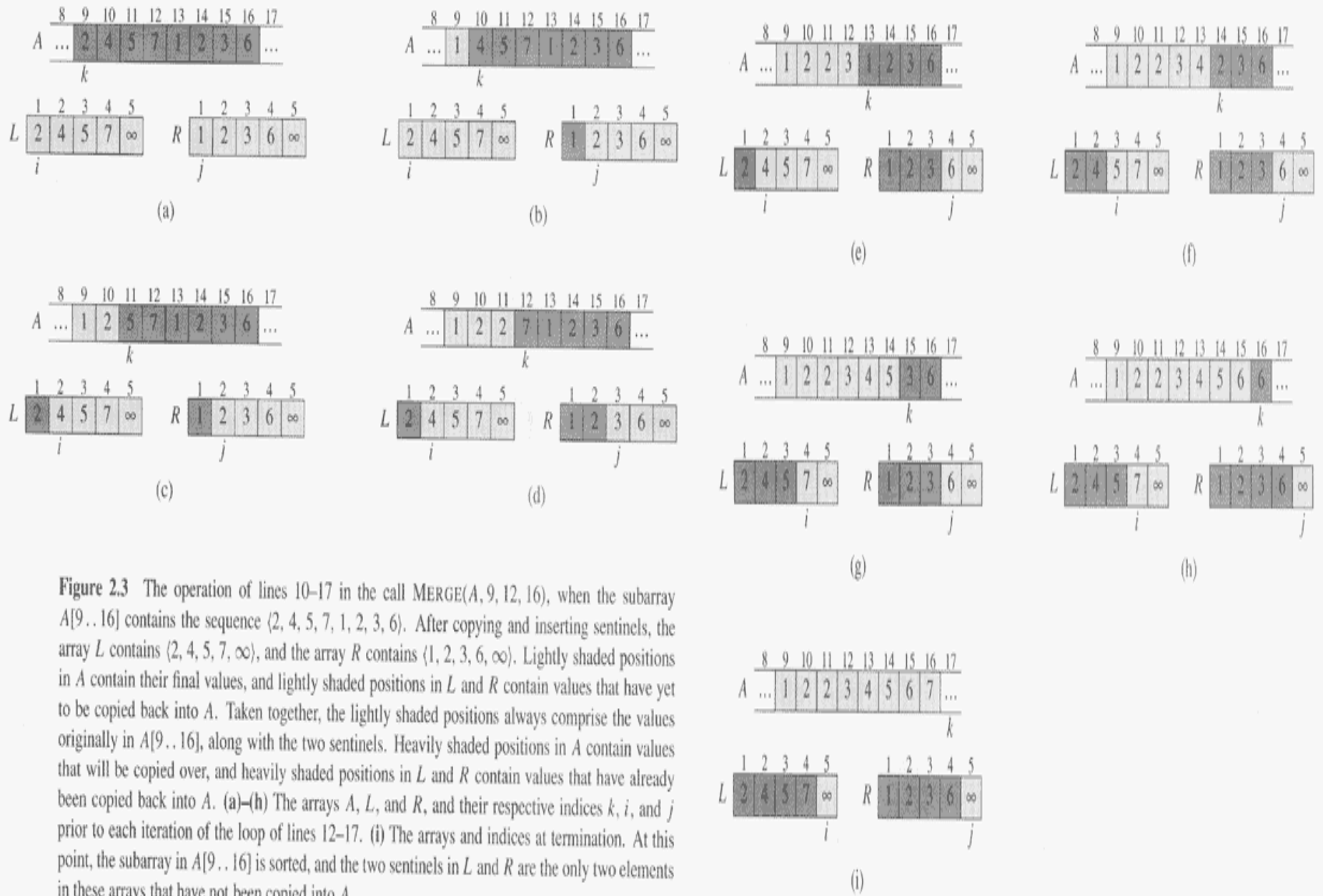


Figure 2.3 The operation of lines 10–17 in the call `MERGE(A, 9, 12, 16)`, when the subarray $A[9..16]$ contains the sequence $\langle 2, 4, 5, 7, 1, 2, 3, 6 \rangle$. After copying and inserting sentinels, the array L contains $\langle 2, 4, 5, 7, \infty \rangle$, and the array R contains $\langle 1, 2, 3, 6, \infty \rangle$. Lightly shaded positions in A contain their final values, and lightly shaded positions in L and R contain values that have yet to be copied back into A . Taken together, the lightly shaded positions always comprise the values originally in $A[9..16]$, along with the two sentinels. Heavily shaded positions in A contain values that will be copied over, and heavily shaded positions in L and R contain values that have already been copied back into A . (a)–(h) The arrays A , L , and R , and their respective indices k , i , and j prior to each iteration of the loop of lines 12–17. (i) The arrays and indices at termination. At this point, the subarray in $A[9..16]$ is sorted, and the two sentinels in L and R are the only two elements in these arrays that have not been copied into A .

```
MERGE( $A, p, q, r$ )
1   $n_1 \leftarrow q - p + 1$ 
2   $n_2 \leftarrow r - q$ 
3  create arrays  $L[1 .. n_1 + 1]$  and  $R[1 .. n_2 + 1]$ 
4  for  $i \leftarrow 1$  to  $n_1$ 
5      do  $L[i] \leftarrow A[p + i - 1]$ 
6  for  $j \leftarrow 1$  to  $n_2$ 
7      do  $R[j] \leftarrow A[q + j]$ 
8   $L[n_1 + 1] \leftarrow \infty$ 
9   $R[n_2 + 1] \leftarrow \infty$ 
10  $i \leftarrow 1$ 
11  $j \leftarrow 1$ 
12 for  $k \leftarrow p$  to  $r$ 
13     do if  $L[i] \leq R[j]$ 
14         then  $A[k] \leftarrow L[i]$ 
15              $i \leftarrow i + 1$ 
16     else  $A[k] \leftarrow R[j]$ 
17          $j \leftarrow j + 1$ 
```

Assumption: Array A is sorted from positions p to q and also from positions q+1 to r.

MERGE-SORT(A, p, r)

1 **if** $p < r$

2 **then** $q \leftarrow \lfloor (p + r) / 2 \rfloor$

3 MERGE-SORT(A, p, q)

4 MERGE-SORT($A, q + 1, r$)

5 MERGE(A, p, q, r)

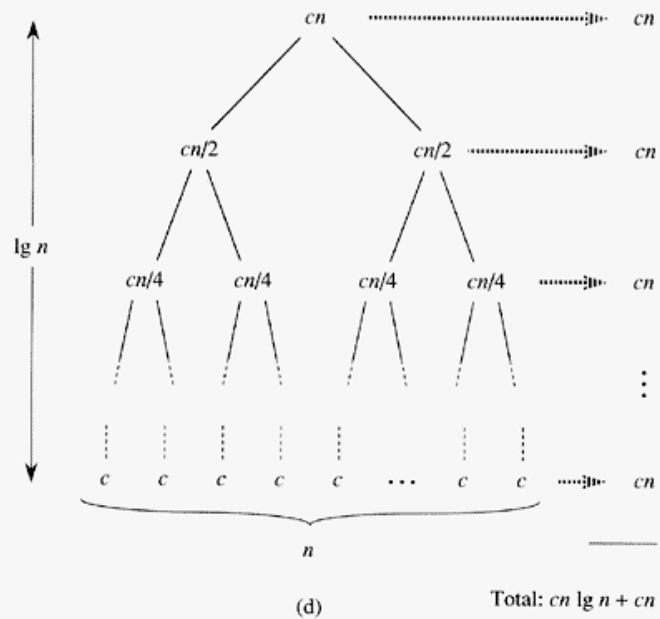
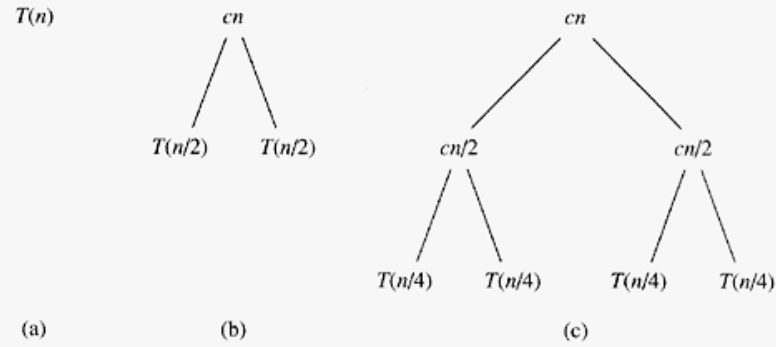


Figure 2.5 The construction of a recursion tree for the recurrence $T(n) = 2T(n/2) + cn$. Part (a) shows $T(n)$, which is progressively expanded in (b)–(d) to form the recursion tree. The fully expanded tree in part (d) has $\lg n + 1$ levels (i.e., it has height $\lg n$, as indicated), and each level contributes a total cost of cn . The total cost, therefore, is $cn \lg n + cn$, which is $\Theta(n \lg n)$.

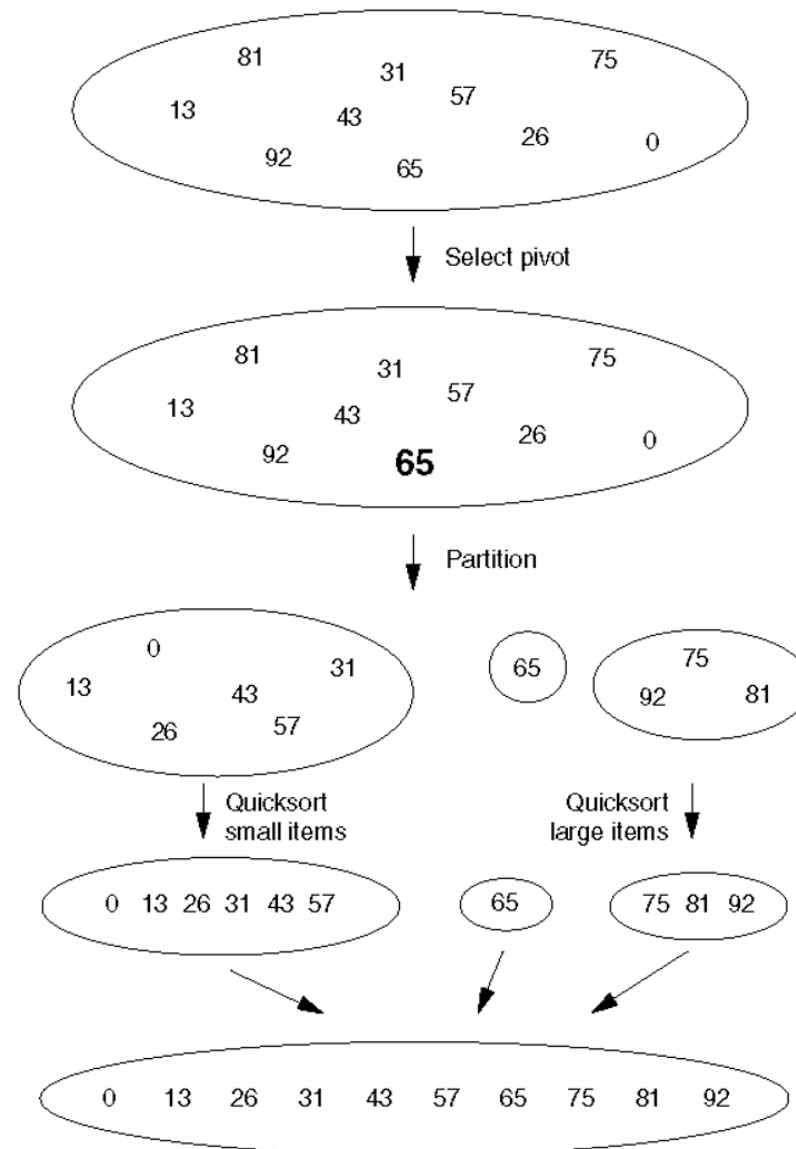
Merge: Algorithm Invariants

- Merge (many lists)
 - ??

Animation Demis

<http://cg.scs.carleton.ca/~morin/misc/sortalg/>

Figure 8.10 Quicksort



Partition

Figure A If 6 is used as pivot, the end result after partitioning is as shown in the Figure B.

2	1	4	5	0	3	9	8	7	6
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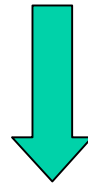


Figure B Result after Partitioning

2	1	4	5	0	3	6	8	7	9
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QuickSort

QUICKSORT(*array A, int p, int r*)

```
1  if ( $p < r$ )
2      then  $q \leftarrow \text{PARTITION}(A, p, r)$ 
3          QUICKSORT( $A, p, q - 1$ )
4          QUICKSORT( $A, q + 1, r$ )
```

To sort array call QUICKSORT($A, 1, \text{length}[A]$).

PARTITION(*array A, int p, int r*)

```
1   $x \leftarrow A[r]$  ▷ Choose pivot
2   $i \leftarrow p - 1$ 
3  for  $j \leftarrow p$  to  $r - 1$ 
4      do if ( $A[j] \leq x$ )
5          then  $i \leftarrow i + 1$ 
6              exchange  $A[i] \leftrightarrow A[j]$ 
7  exchange  $A[i + 1] \leftrightarrow A[r]$ 
8  return  $i + 1$ 
```

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Problems to think about!

- What is the least number of comparisons you need to sort a list of 3 elements? 4 elements? 5 elements?
- How to arrange a tennis tournament in order to find the tournament **champion** with the least number of matches?
How many tennis matches are needed?