COP 6405: Analysis of Algorithms FINAL REVIEW - PART 2; Fall 2019

- 1. By relaxing the edges of a weighted DAG (directed acyclic graph) according to a *topological sort* of its vertices, we can compute shortest paths from a single source in O(m+n) time, which is the time it takes to run topological sort in a DAG. Make sure you know how and why this works as explained in Section 24.2.
- 2. Solve 24.2-4 on page 658. It asks you to count the number of paths (not shortest paths) in a DAG.
- 3. Solve problem 24.3-2 on page 663, which asks for an example where Dijkstra's algorithm would fail when there are negative weight edges.
- 4. Solve problem 24.3-8 on page 664.
- 5. Solve problem 24.3-10 on page 664.
- 6. Explain the RELAX operation on an edge used in DIJKSTRA's algorithm. Explain why it is important to relax the edges of the graph in the right order.
- 7. Study algorithm TRANSITIVE CLOSURE on page 698 that modifies FLOYD-WARSHALL's algorithm to solve the *Transitive Closure* problem. Look at the difference between the two algorithms and describe the changes.
- 8. Solve problem 26.1-7 on page 714.
- 9. Write down precisely the statement of Menger's theorem connecting maximum flow to cuts.
- 10. Solve problem 26.2-6 on page 730.
- 11. Solve problem 26.2-11 on page 731.