

# COT 6405: Analysis of Algorithms

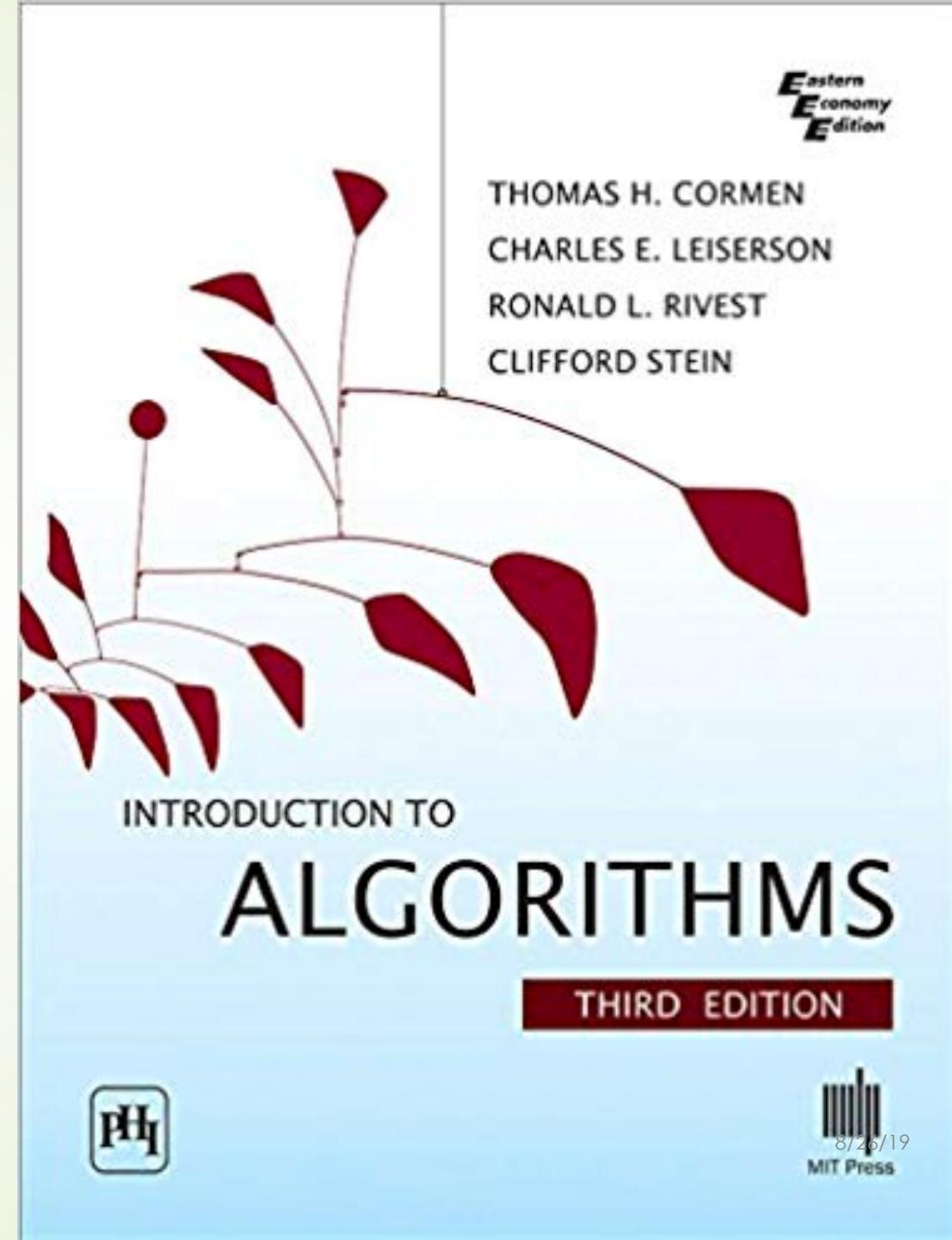
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[www.cs.fiu.edu/~giri/teach/6405F19.html](http://www.cs.fiu.edu/~giri/teach/6405F19.html)

# Text

**3<sup>rd</sup> Edition**

- **ISBN-13:**  
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# Course Preliminaries

- ▶ Course Webpage:

**<http://www.cs.fiu.edu/~giri/teach/6405F19.html>**

- ▶ Lecture Slides; Reading Material; Announcements; HWs
- ▶ VISIT OFTEN!

▶ Class meets MW 2:00 – 3:15 PM, CASE/ECS 235

▶ Office ECS 254B; Office Hours: By Appointment Only

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▶ Final: Monday, 12/11/2019, 12:00 – 2:00 PM, CASE 235

**<http://www.cs.fiu.edu/~giri/teach/6405F19.html>**

# Momentos

- ▶ Slides and Audio online
- ▶ Need to register
  - ▶ Go to [\*\*https://fiu.momentos.life\*\*](https://fiu.momentos.life)
  - ▶ If you don't already have an account
    - ▶ Click on "Sign up"
    - ▶ Follow instructions & use referral code: **5T6LSV**
  - ▶ If you have an account, "Add Course" with code **5T6LSV**
  - ▶ Verify account using link sent to email

# Why I am here?

**I am here because ...**

► **It's required**

- What do I expect to learn in this class?
- Who should know about **Algorithms**?
- Is there a future in this field?
- Would I ever need it if I want to be a software engineer or work with databases?

**Hate being here because ...**

► **It's required**

# Questions you should ask ...

- ▶ What do I expect to learn in this class?
- ▶ Who should know about **Algorithms**?
- ▶ Is there a future in this field?
- ▶ Would I ever need it if I want to be a software engineer or work with databases?



# **Person of the Year ...**

# Time's Person of the Year

2018



2017



# The first hundred votes ...

Who won  
a  
majority?

48	12	9	12	23	12	22	12	12	12
48	93	93	93	12	12	93	12	93	12
12	93	48	48	12	12	12	33	79	12
12	12	93	12	12	9	12	23	12	12
12	12	12	33	93	93	93	12	12	12
12	9	12	23	93	48	48	12	12	44
93	93	93	12	12	9	12	23	12	55
12	12	48	12	48	48	12	48	88	12
12	12	93	12	12	9	12	23	12	12
12	12	12	33	93	93	93	12	12	12

Every number in the table corresponds to a vote for a person with that ID

# Standard Approaches

- ▶ **Keep a list of candidates and their counts**
  - ▶ Every vote needs to be compared against every candidate in the worst case
- ▶ **Sort the list and count**
  - ▶ Sorting is the bottleneck
  - ▶ Can we avoid sorting?

11

48	93	93	93	12	12	93	12	93	12	93	12	93	12	9	12	23	12	93	93	93	12	9	12	23
12	93	48	48	12	12	12	12	33	79	12	12	33	93	93	93	12	12	93	48	48	93	93	93	12
12	12	93	12	12	9	12	23	12	12	12	23	93	48	48	12	12	12	93	12	93	48	48	12	12
12	12	12	33	93	93	93	12	12	12	93	12	12	9	12	23	12	12	12	12	33	12	9	12	23
12	9	12	23	93	48	48	12	12	44	48	48	12	48	88	12	12	9	12	23	48	48	12	48	12
93	93	93	12	12	9	12	23	12	55	12	9	12	23	12	12	93	93	93	12	12	9	12	23	
12	12	48	12	48	48	12	48	88	12	93	93	93	12	12	12	93	12	48	12	93	93	93	12	12
12	12	93	12	12	9	12	23	12	12	12	12	9	12	23	12	55	12	12	93	12	12	33	79	12
12	12	12	33	93	93	93	12	12	12	12	12	12	12	33	93	93	93	12	12	12	12	23	12	12
48	48	12	12	12	33	79	12	12	33	93	93	93	12	12	93	48	12	33	79	93	12	12	12	12
93	12	12	9	12	23	12	12	12	23	93	48	48	12	12	12	93	12	23	12	48	12	12	44	12
12	33	93	93	93	12	12	12	93	12	12	9	12	23	12	12	12	93	12	12	12	23	12	55	12
12	23	93	48	48	12	12	44	48	48	12	48	88	12	12	9	12	48	12	12	12	48	88	12	12
93	12	12	9	12	23	12	12	12	9	12	23	12	55	12	12	93	12	23	12	12	23	12	12	12
48	12	48	48	12	48	88	12	93	93	93	12	12	12	93	12	48	12	48	88	12	23	12	12	12
93	12	12	9	12	23	12	12	12	9	12	23	12	55	12	12	93	12	23	12	12	93	12	12	12
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12	33	93	93	93	12	12	12	93	12	12	9	12	23	12	12	12	93	12	12	12	23	12	55	12
12	23	93	48	48	12	12	44	48	48	12	48	88	12	12	9	12	48	12	12	12	48	88	12	12
93	12	12	9	12	23	12	55	12	9	12	23	12	12	93	93	93	12	23	12	12	23	12	12	12
48	12	48	48	12	48	88	12	93	93	93	12	12	12	93	12	48	12	48	88	12	23	12	12	12
48	48	12	12	12	12	33	79	12	12	33	93	93	93	12	12	93	48	12	33	79	93	12	12	12
93	12	12	9	12	23	12	12	12	23	93	48	48	12	12	12	93	12	23	12	48	12	12	44	
12	33	93	93	93	12	12	12	93	12	12	9	12	23	12	12	12	93	12	12	12	23	12	55	12
12	23	93	48	48	12	12	44	48	48	12	48	88	12	12	9	12	48	12	12	12	48	88	12	12
93	12	12	9	12	23	12	55	12	9	12	23	12	12	93	93	93	12	23	12	12	23	12	12	12
48	12	48	48	12	48	88	12	93	93	93	12	12	12	93	12	48	12	48	88	93	93	12	12	12
93	12	12	9	12	23	12	12	12	9	12	23	12	55	12	12	93	12	23	12	9	12	23	12	12
48	12	48	48	12	48	88	12	93	93	93	12	12	12	93	12	48	12	48	88	12	23	12	12	12
93	12	12	9	12	23	12	12	12	9	12	23	12	55	12	12	93	12	23	12	9	12	23	12	12
12	23	93	48	48	12	12	44	48	48	12	48	88	12	12	9	12	48	12	12	12	48	88	12	12
93	12	12	9	12	23	12	55	12	9	12	23	12	12	93	93	93	12	23	12	12	23	12	12	12
48	12	48	48	12	48	88	12	93	93	93	12	12	12	93	12	48	12	48	88	12	23	12	12	12

# Wacky Ideas, anyone?

- ▶ What if I pick two random votes and they turn out to be different?
  - ▶ Discard and reduce the problem size
- ▶ What if I pick two random votes and they are the same?
  - ▶ Well, this needs work and you will need to think about it!

48	12	9	12	23	12	22	12	12	12
48	93	93	93	12	12	93	12	93	12
12	93	48	48	12	12	12	33	79	12
12	12	93	12	12	9	12	23	12	12
12	12	12	33	93	93	93	12	12	12
12	9	12	23	93	48	48	12	12	44
93	93	93	12	12	9	12	23	12	55
12	12	48	12	48	48	12	48	88	12
12	12	93	12	12	9	12	23	12	12
12	12	12	33	93	93	93	12	12	12

# Difference between Intro and Analysis of Algorithms?

- ▶ More on how to analyze ... more on complexity
- ▶ More on correctness ...
- ▶ More algorithms ...
- ▶ More data structures ... bigger bag of tricks
- ▶ More on different algorithmic models ...
  - ▶ Randomized, online, amortized, adaptive, approximation, heuristic, quantum,

# Evaluation

► Exams (2)	45%
► Quizzes	10%
► HW Assignments	35%
► Class Participation	10%

# What you should already know ...

- ▶ **Array Lists**
- ▶ **Linked Lists**
- ▶ **Sorted Lists**
- ▶ **Stacks and Queues**
- ▶ **Basic Sorting Algorithms**
- ▶ **Trees**
- ▶ **Binary Search Trees**
- ▶ **Heaps and Priority Queues**
- ▶ **Graphs**
  - ▶ **Adjacency Lists**
  - ▶ **Adjacency Matrices**

# The Algorithmic Process

- ▶ **Formulate the question**
- ▶ **Write down a basic idea, an approach**
- ▶ **Write down pseudocode**
- ▶ **Prove correctness**
- ▶ **Analyze pseudocode and think about upper and lower bounds**
- ▶ **Iterate**

# History of Algorithms

- ▶ **Euclid, 300 BC**
- ▶ **Bhaskara, 6<sup>th</sup> c**
- ▶ **Al Khwarizmi, 9th c**
- ▶ **Fibonacci, 13<sup>th</sup> c**
- ▶ **Gauss, 18-19<sup>th</sup> c**
- ▶ **Babbage, 19<sup>th</sup> c**
- ▶ **Turing, 20<sup>th</sup> c**
- ▶ **von Neumann, 20<sup>th</sup> c**
- ▶ **Knuth, Karp, Tarjan, Rabin, ..., 20-21<sup>st</sup> c**

# Reading for next class

- ▶ **Big-Oh notation**
  - ▶ Chapter 2, 3
- ▶ **All sorting algorithms and their analysis**
  - ▶ Chapters 2, 6, 7, 8