

CAP 5510: Introduction to Bioinformatics  
CGS 5166: Bioinformatics Tools

**Giri Narasimhan**

ECS 254; Phone: x3748

[giri@cis.fiu.edu](mailto:giri@cis.fiu.edu)

[www.cis.fiu.edu/~giri/teach/BioinfS13.html](http://www.cis.fiu.edu/~giri/teach/BioinfS13.html)

# Gene Expression

- ❑ Process of transcription and/or translation of a gene is called **gene expression**.
- ❑ Every cell of an organism has the same genetic material, but different genes are **expressed** at different times.
- ❑ Patterns of gene expression in a cell is indicative of its state.

# Hybridization

- If two complementary strands of DNA or mRNA are brought together under the right experimental conditions they will hybridize.
- $A$  hybridizes to  $B \Rightarrow$ 
  - $A$  is reverse complementary to  $B$ , or
  - $A$  is reverse complementary to a subsequence of  $B$ .
- It is possible to experimentally verify whether  $A$  hybridizes to  $B$ , by labeling  $A$  or  $B$  with a radioactive or fluorescent tag, followed by excitation by laser.

# Measuring gene expression

- Gene expression for a single gene can be measured by extracting mRNA from the cell and doing a simple **hybridization** experiment.
- Given a sample of cells, gene expression for every gene can be measured using a single microarray experiment.

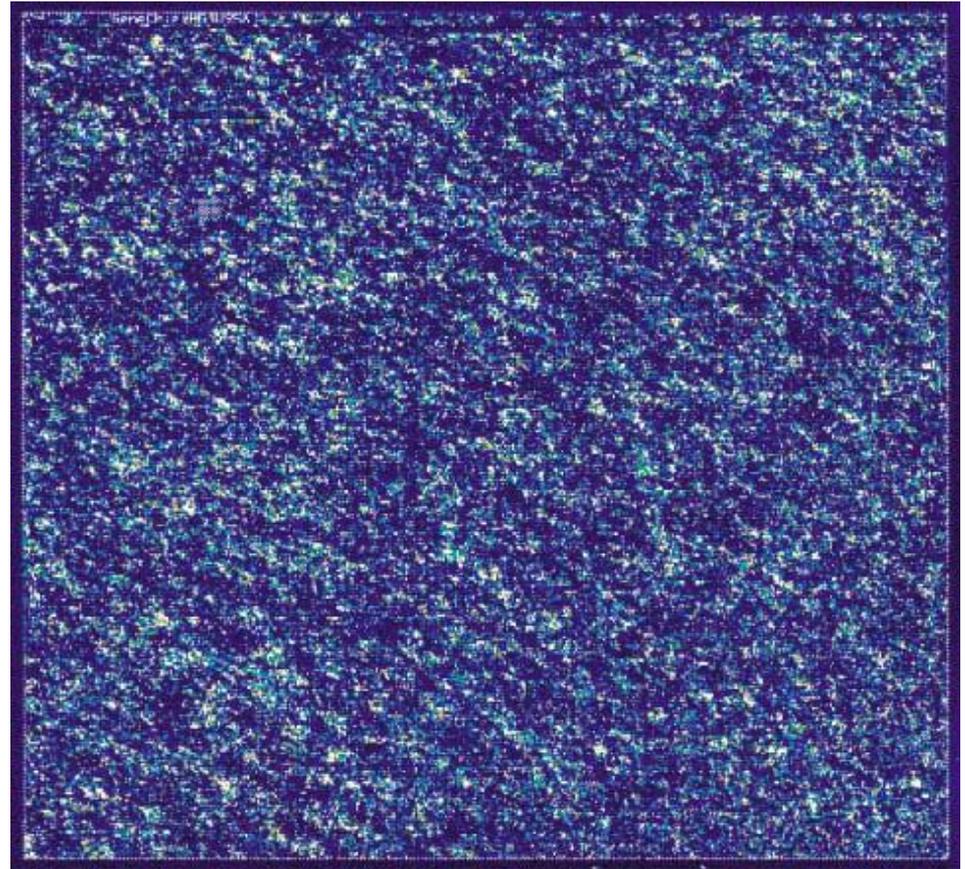
# Microarray/DNA chip technology

- High-throughput method to study gene expression of thousands of genes simultaneously.
- Many applications:
  - Genetic disorders & Mutation/polymorphism detection
  - Study of disease subtypes
  - Drug discovery & toxicology studies
  - Pathogen analysis
  - Differing expressions over time, between tissues, between drugs, across disease states

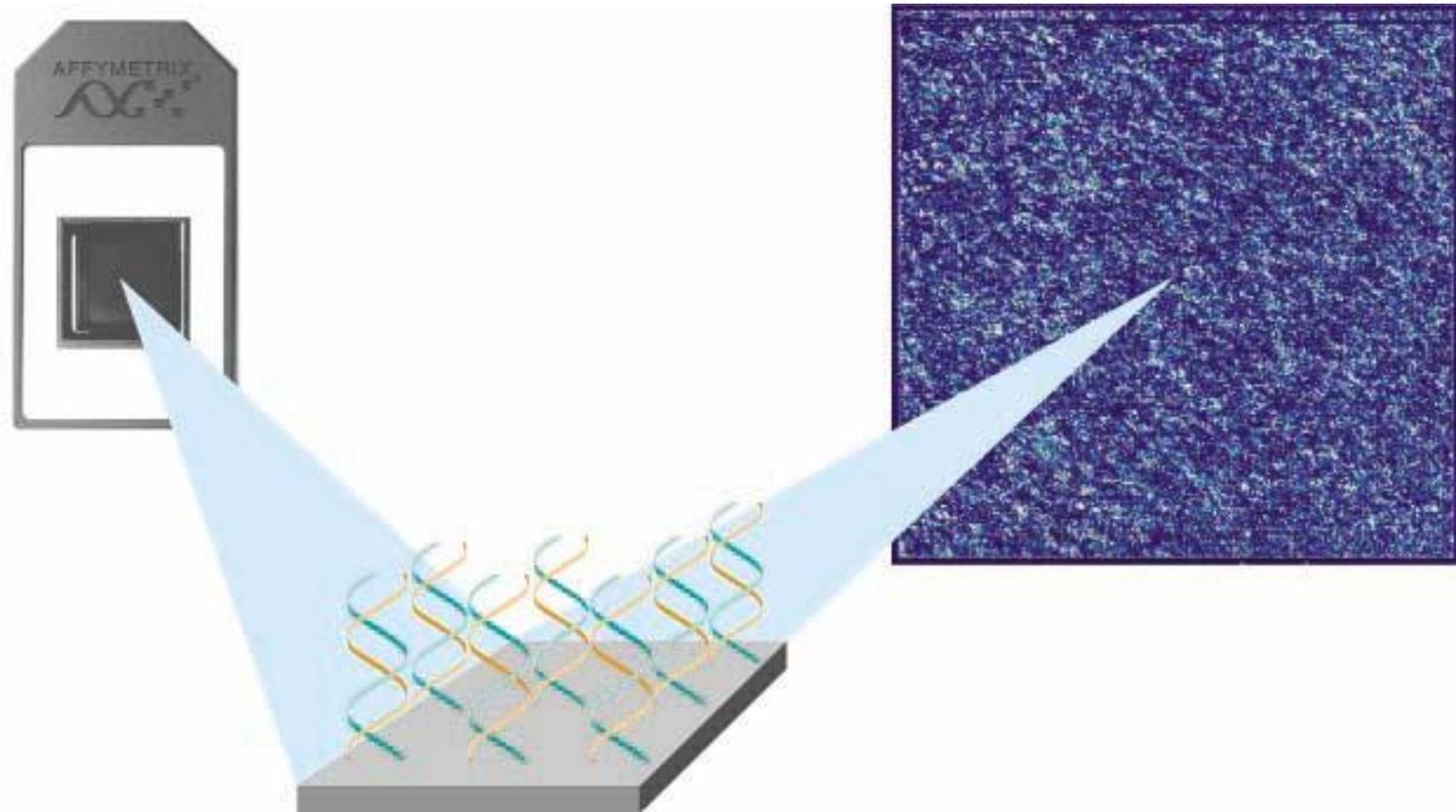
# Microarray Data

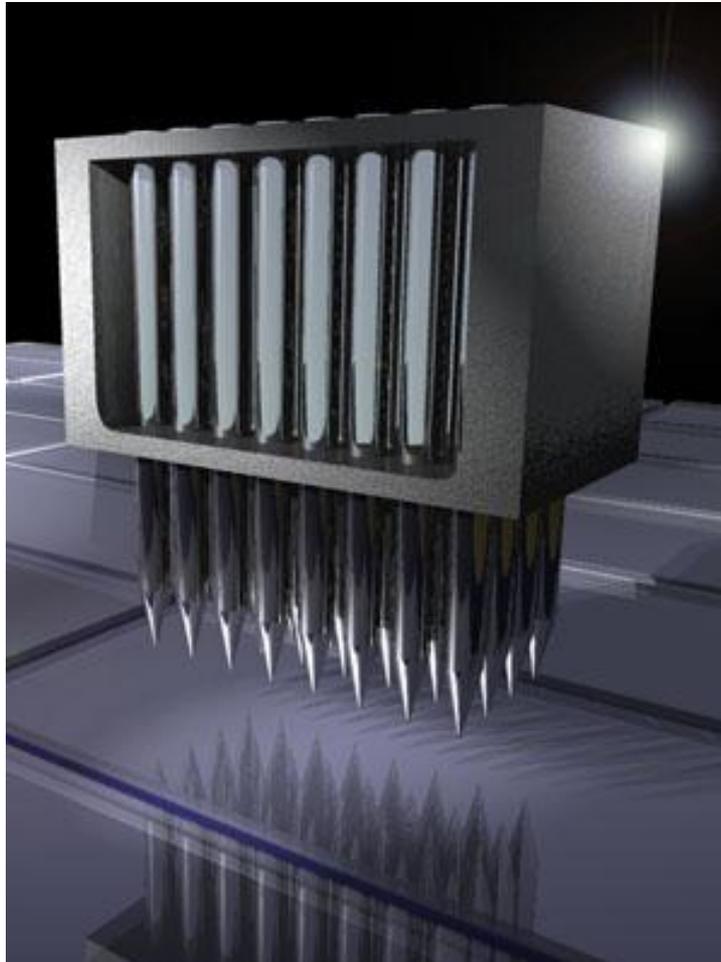
Gene	Expression Level
Gene1	
Gene2	
Gene3	
...	

# Gene Chips

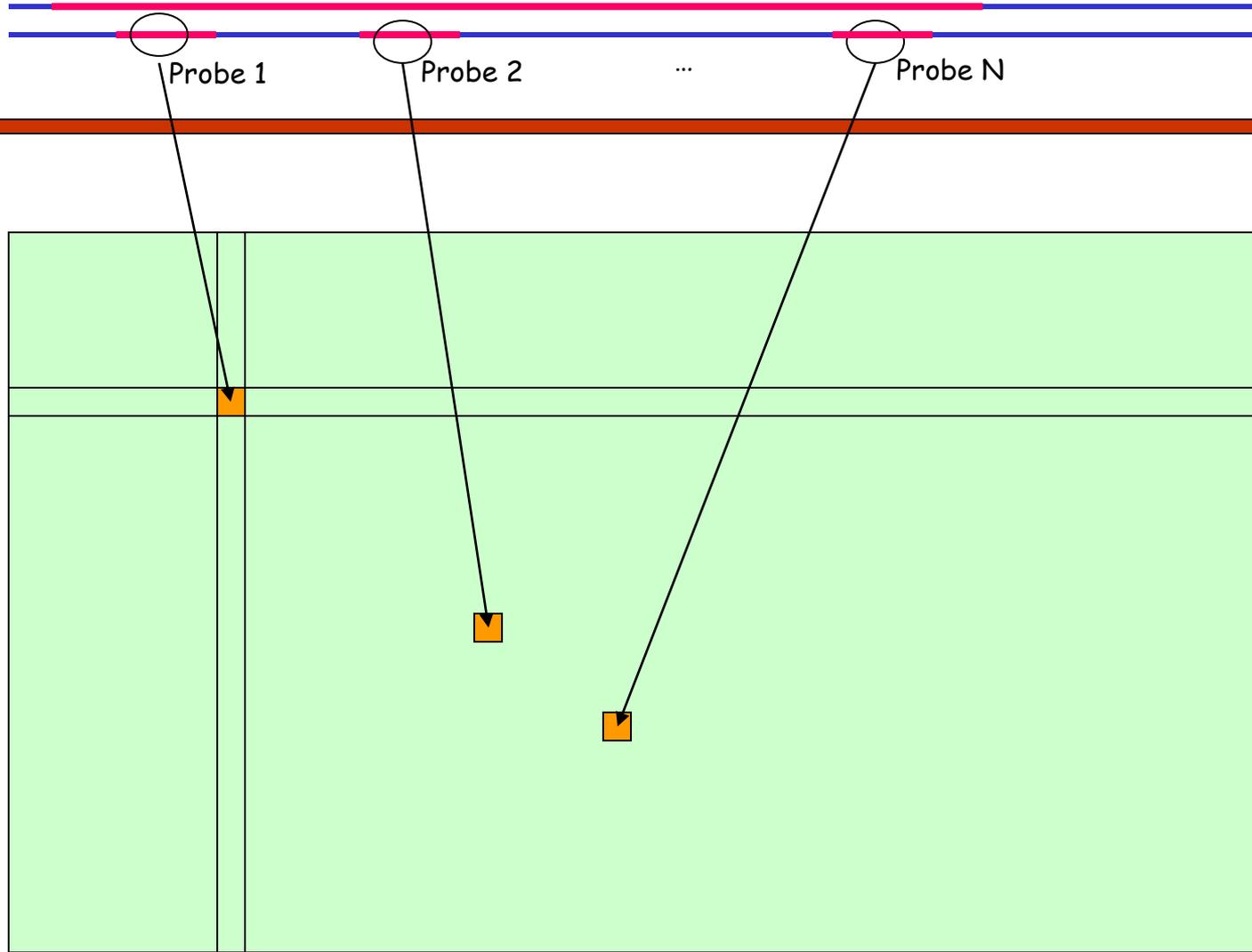


# DNA Chips & Images





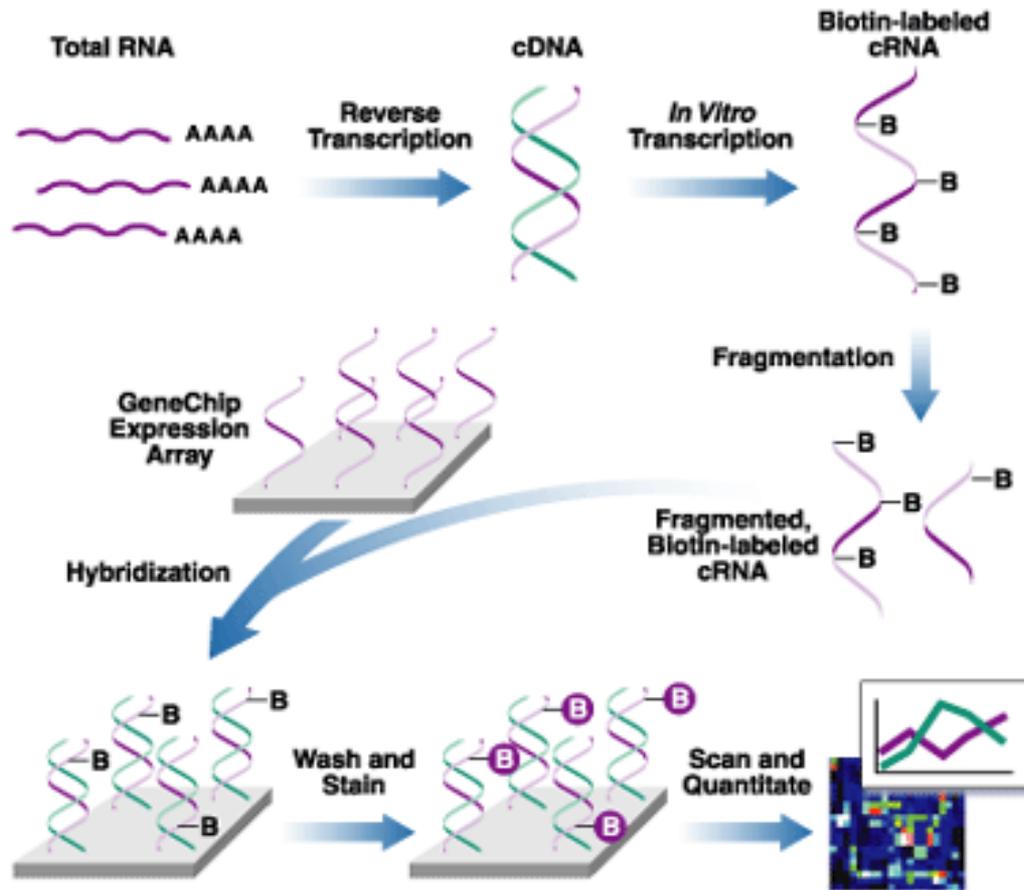
# Gene g



# Microarray/DNA chips (Simplified)

- ❑ Construct **probes** corresponding to reverse complements of genes of interest.
- ❑ Microscopic quantities of probes placed on solid surfaces at defined spots on the chip.
- ❑ Extract mRNA from sample cells and **label** them.
- ❑ Apply labeled sample (mRNA extracted from cells) to every spot, and allow hybridization.
- ❑ Wash off unhybridized material.
- ❑ Use optical detector to measure amount of fluorescence from each spot.

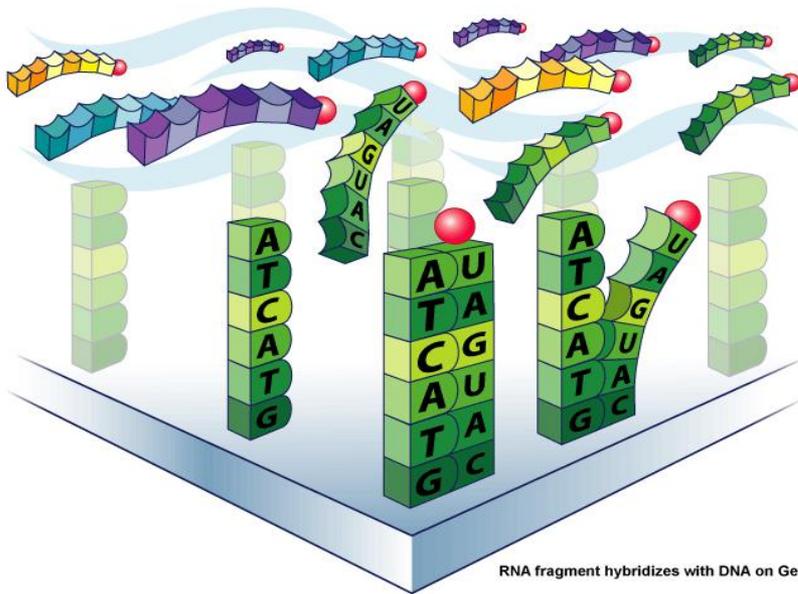
# Affymetrix DNA chip schematic



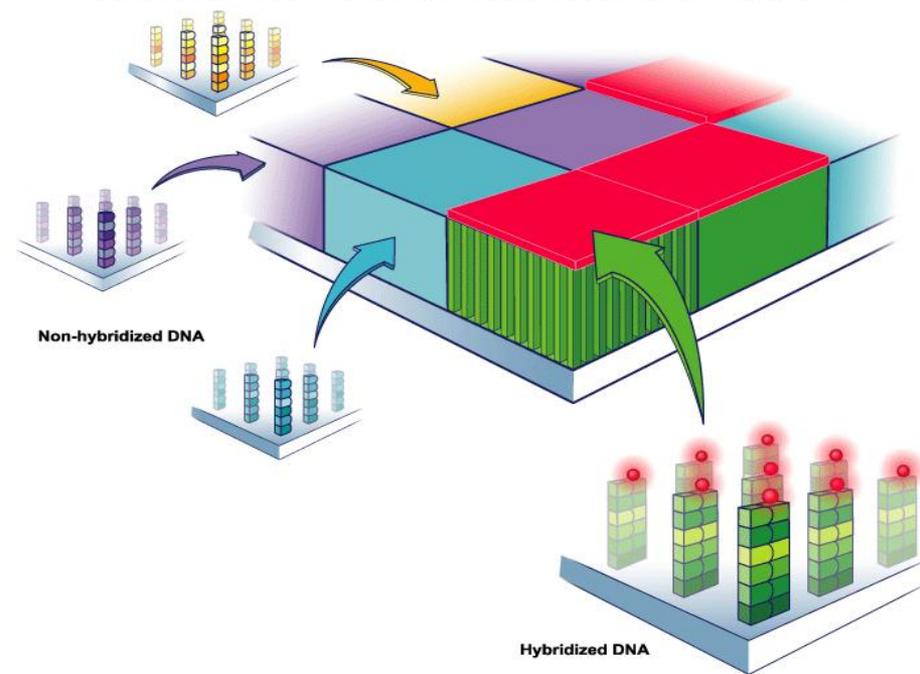
[www.affymetrix.com](http://www.affymetrix.com)

# What's on the slide?

RNA fragments with fluorescent tags from sample to be tested



Shining a laser light at GeneChip® array causes tagged DNA fragments that hybridized to glow



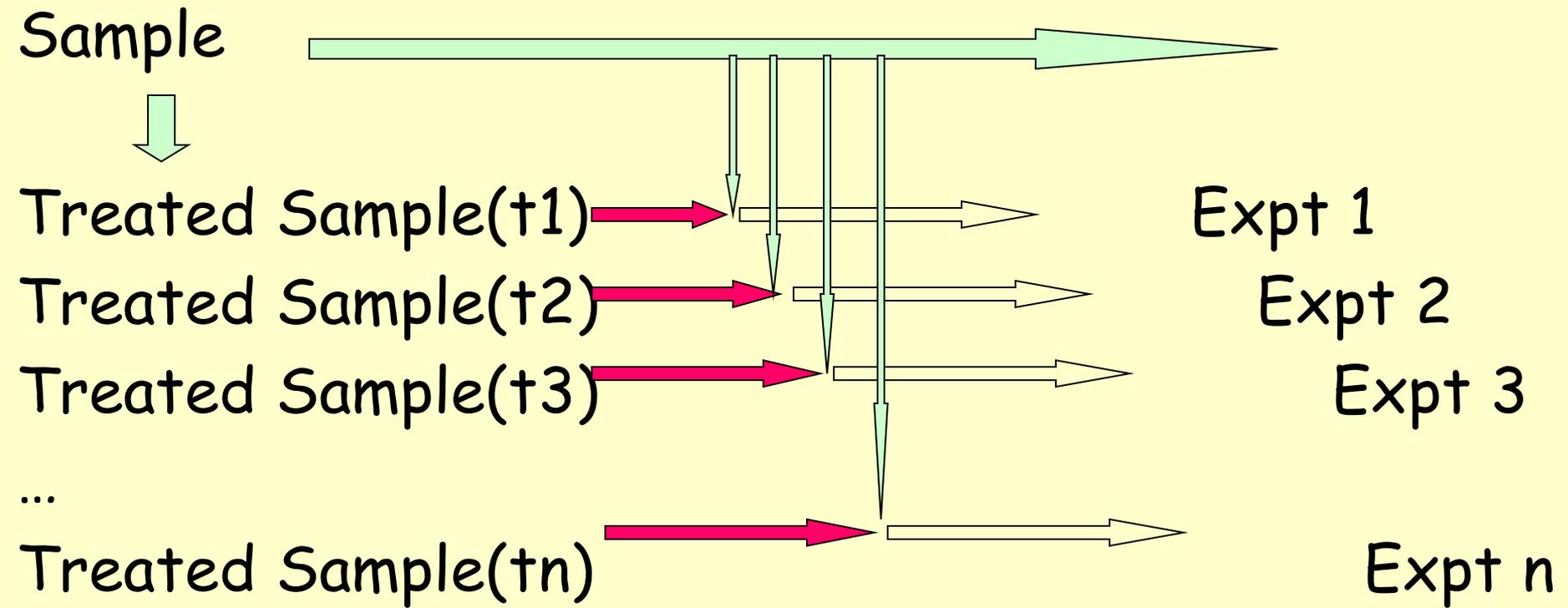
# Microarrays: competing technologies

## □ Affymetrix & Agilent

### □ Differ in:

- method to place DNA: Spotting vs. photolithography
- Length of probe
- Complete sequence vs. series of fragments

# Study effect of treatment over time





AFGC

# 2-color DNA microarray



Treated

mRNA

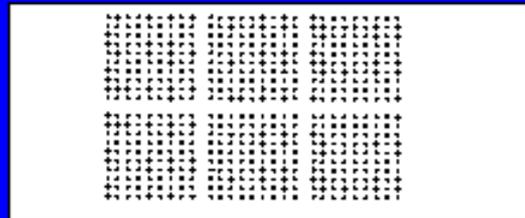
Cy5 Probe



Control

mRNA

Cy3 Probe

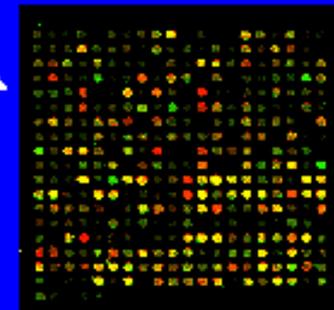


Simultaneous hybridization

Normalization

Data extraction

Scanning



# How to compare 2 cell samples with Two-Color Microarrays?

- ❑ mRNA from sample 1 is extracted and labeled with a **red fluorescent** dye.
- ❑ mRNA from sample 2 is extracted and labeled with a **green fluorescent** dye.
- ❑ Mix the samples and apply it to every spot on the microarray. Hybridize sample mixture to probes.
- ❑ Use optical detector to measure the amount of **green** and **red** fluorescence at each spot.

# Sources of Variations & Experimental Errors

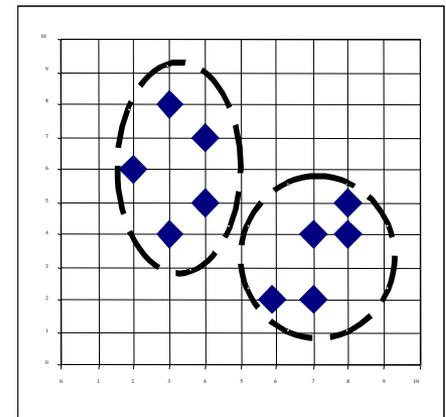
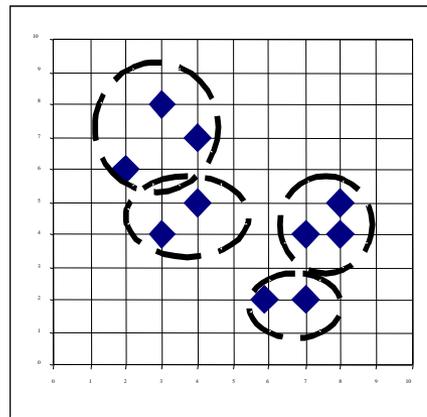
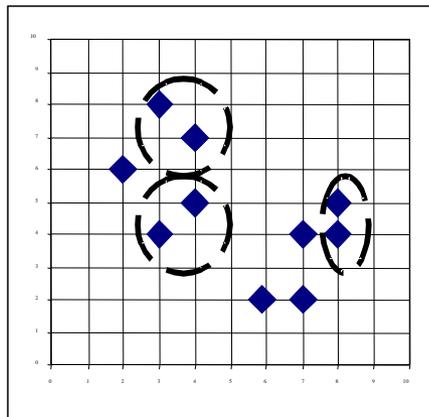
- ❑ Variations in cells/individuals
- ❑ Variations in mRNA extraction, isolation, introduction of dye, variation in dye incorporation, dye interference
- ❑ Variations in probe concentration, probe amounts, substrate surface characteristics
- ❑ Variations in hybridization conditions and kinetics
- ❑ Variations in optical measurements, spot misalignments, discretization effects, noise due to scanner lens and laser irregularities
- ❑ Cross-hybridization of sequences with high sequence identity
- ❑ Limit of factor 2 in precision of results
- ❑ Variation changes with intensity: larger variation at low or high expression levels

Need to Normalize data

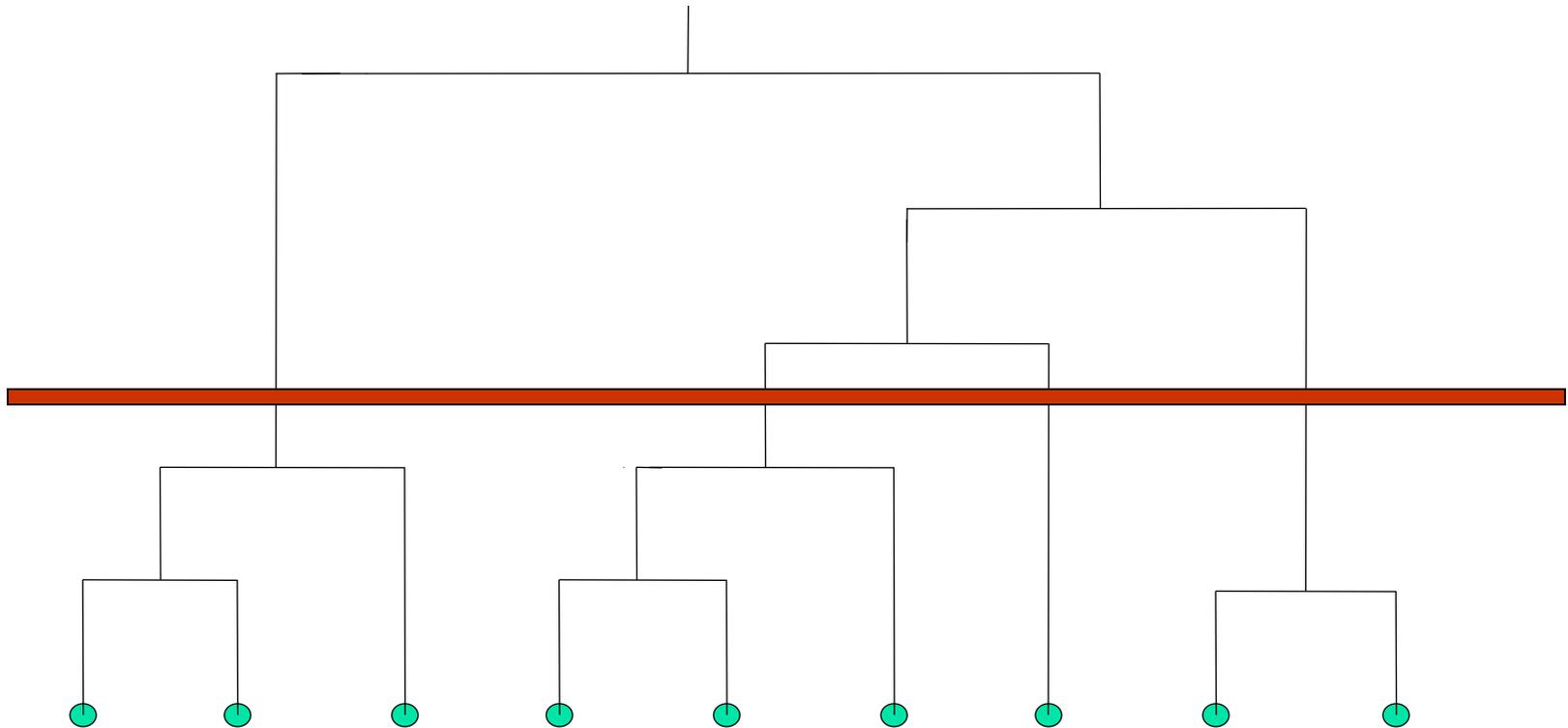
# Clustering

- Clustering is a general method to study patterns in gene expressions.
- Several known methods:
  - *Hierarchical Clustering* (Bottom-Up Approach)
  - *K-means Clustering* (Top-Down Approach)
  - *Self-Organizing Maps (SOM)*

# Hierarchical Clustering: Example



# A Dendrogram



# Hierarchical Clustering [Johnson, SC, 1967]

- Given  $n$  points in  $\mathbb{R}^d$ , compute the distance between every pair of points
- While (not done)
  - Pick closest pair of points  $s_i$  and  $s_j$  and make them part of the same cluster.
  - Replace the pair by an average of the two  $s_{ij}$

Try the applet at:

[http://home.dei.polimi.it/matteucc/Clustering/tutorial\\_html/AppletH.html](http://home.dei.polimi.it/matteucc/Clustering/tutorial_html/AppletH.html)

# Distance Metrics

□ For clustering, define a distance function:

● **Euclidean distance** metrics

$$D_k(X, Y) = \left( \sum_{i=1}^d (X_i - Y_i)^k \right)^{1/k}$$

k=2: Euclidean Distance

● **Pearson correlation coefficient**

$$r_{xy} = \frac{1}{d} \sum_{i=1}^d \frac{(X_i - \bar{X})(Y_i - \bar{Y})}{S_x S_y}$$

$-1 \leq \rho_{xy} \leq 1$

**EXHIBIT 3.4** Joint Probability Model for the Ratings of Two People

(a)  $\rho_{XY} = 0$

x	y			Total
	1	2	3	
3	1/9	1/9	1/9	1/3
2	1/9	1/9	1/9	1/3
1	1/9	1/9	1/9	1/3
Total	1/3	1/3	1/3	1

(b)  $\rho_{XY} = \frac{1}{2}$

x	y			Total
	1	2	3	
3	1/18	1/18	4/18	1/3
2	1/18	4/18	1/18	1/3
1	4/18	1/18	1/18	1/3
Total	1/3	1/3	1/3	1

(c)  $\rho_{XY} = -\frac{1}{2}$

x	y			Total
	1	2	3	
3	4/18	1/18	1/18	1/3
2	1/18	4/18	1/18	1/3
1	1/18	1/18	4/18	1/3
Total	1/3	1/3	1/3	1

(d)  $\rho_{XY} = \frac{1}{3}$

x	y			Total
	1	2	3	
3	1/27	2/27	6/27	1/3
2	2/27	5/27	2/27	1/3
1	6/27	2/27	1/27	1/3
Total	1/3	1/3	1/3	1

(e)  $\rho_{XY} = -\frac{2}{3}$

x	y			Total
	1	2	3	
3	6/27	2/27	1/27	1/3
2	2/27	5/27	2/27	1/3
1	1/27	2/27	6/27	1/3
Total	1/3	1/3	1/3	1

(f)  $\rho_{XY} = \frac{2}{3}$

x	y			Total
	1	2	3	
3	1/36	2/36	9/36	1/3
2	2/36	8/36	2/36	1/3
1	9/36	2/36	1/36	1/3
Total	1/3	1/3	1/3	1

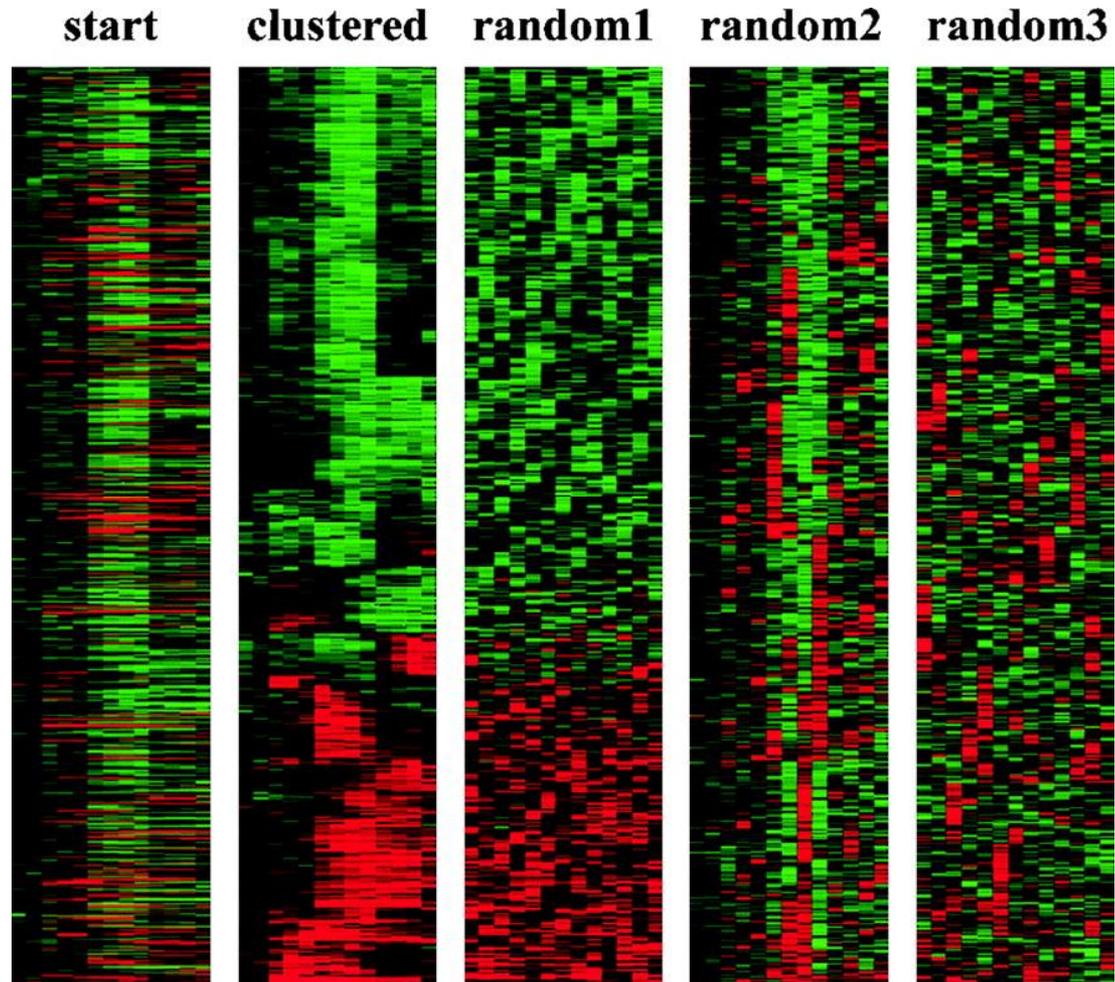
(g)  $\rho_{XY} = -\frac{1}{3}$

x	y			Total
	1	2	3	
3	9/36	2/36	1/36	1/3
2	2/36	8/18	2/18	1/3
1	1/36	2/36	9/36	1/3
Total	1/3	1/3	1/3	1

# Clustering of gene expressions

- Represent each gene as a vector or a point in  $d$ -space where  $d$  is the number of arrays or experiments being analyzed.

# Clustering Random vs. Biological Data



From Eisen MB, et al, PNAS 1998 95(25):14863 -8

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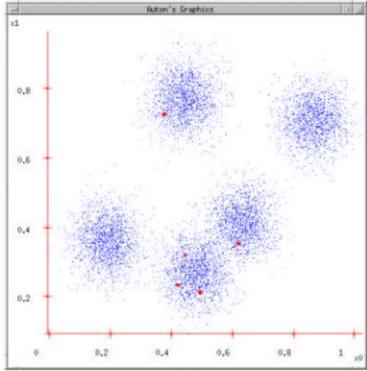
# K-Means Clustering: Example

Example from Andrew Moore's tutorial on Clustering.

Start

### K-means

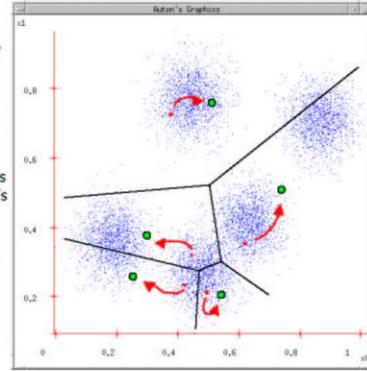
1. Ask user how many clusters they'd like. (e.g.  $k=5$ )
2. Randomly guess  $k$  cluster Center locations



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K-means and Hierarchical Clustering: Slide 7

### K-means

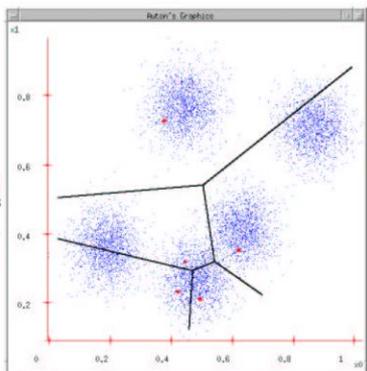
1. Ask user how many clusters they'd like. (e.g.  $k=5$ )
2. Randomly guess  $k$  cluster Center locations
3. Each datapoint finds out which Center it's closest to.
4. Each Center finds the centroid of the points it owns



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K-means and Hierarchical Clustering: Slide 9

### K-means

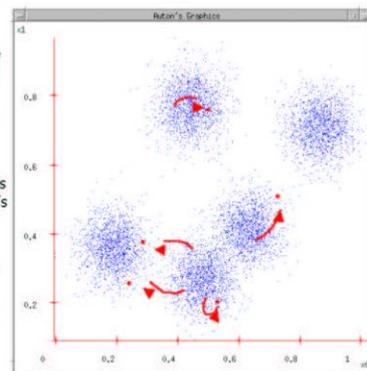
1. Ask user how many clusters they'd like. (e.g.  $k=5$ )
2. Randomly guess  $k$  cluster Center locations
3. Each datapoint finds out which Center it's closest to. (Thus each Center "owns" a set of datapoints)



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K-means and Hierarchical Clustering: Slide 8

### K-means

1. Ask user how many clusters they'd like. (e.g.  $k=5$ )
2. Randomly guess  $k$  cluster Center locations
3. Each datapoint finds out which Center it's closest to.
4. Each Center finds the centroid of the points it owns...
5. ...and jumps there
6. ...Repeat until terminated!



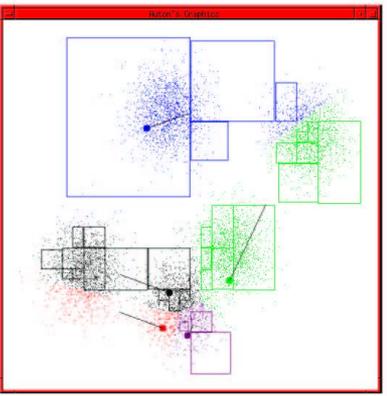
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K-means and Hierarchical Clustering: Slide 10

## K-means Start

Advance apologies: in Black and White this example will deteriorate

Example generated by Dan Pelleg's super-duper fast K-means system:

*Dan Pelleg and Andrew Moore. Accelerating Exact k-means Algorithms with Geometric Reasoning. Proc. Conference on Knowledge Discovery in Databases 1999, (KDD99) (available on [www.autonlab.org/pap.html](http://www.autonlab.org/pap.html))*

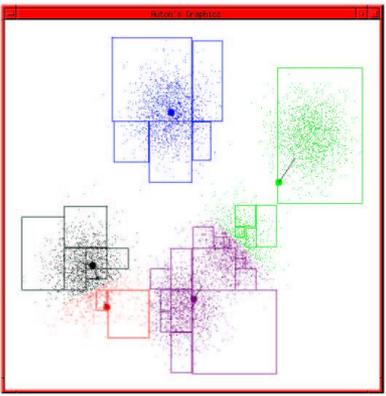


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K-means and Hierarchical Clustering: Slide 11

## K-means continues

...

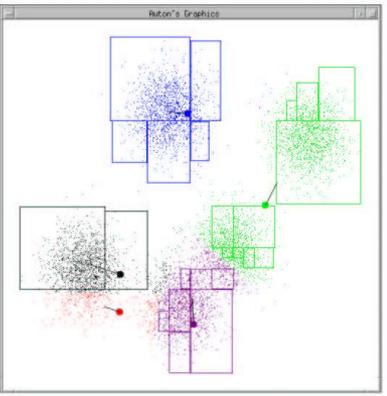


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K-means and Hierarchical Clustering: Slide 13

## K-means continues

...

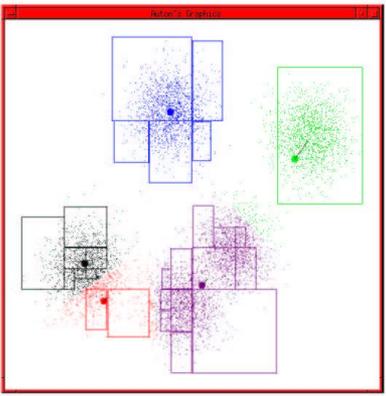


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K-means and Hierarchical Clustering: Slide 12

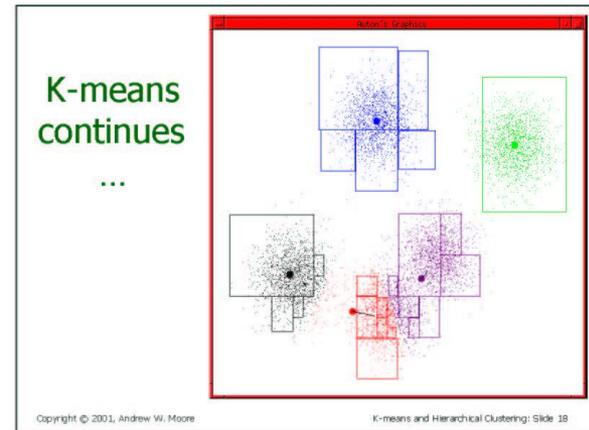
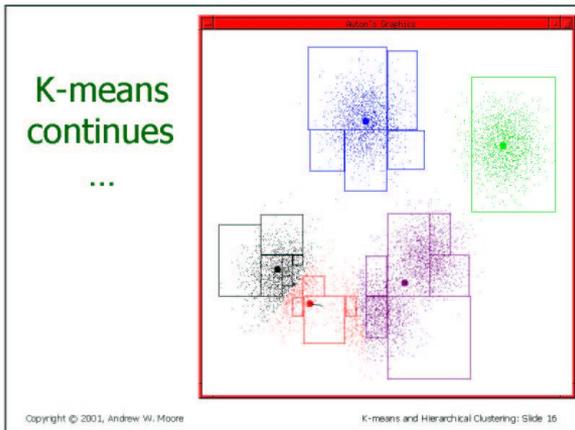
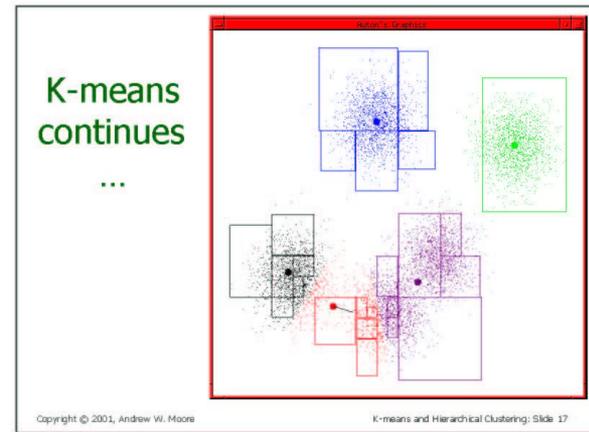
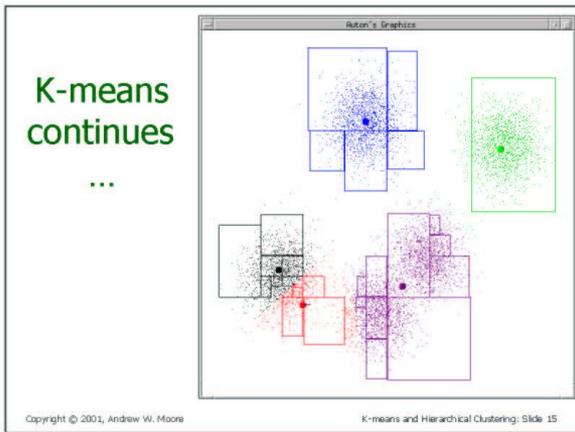
## K-means continues

...



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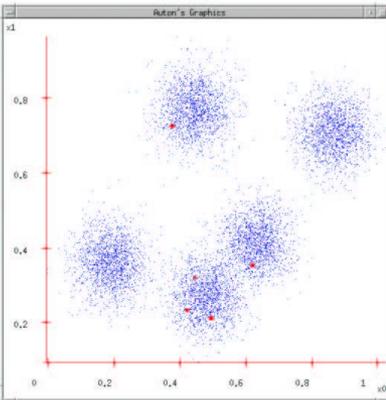
K-means and Hierarchical Clustering: Slide 14



Start

### K-means

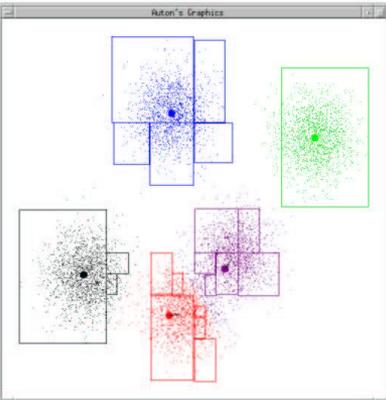
1. Ask user how many clusters they'd like. (e.g.  $k=5$ )
2. Randomly guess k cluster Center locations



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K-means and Hierarchical Clustering: Slide 7

### K-means continues

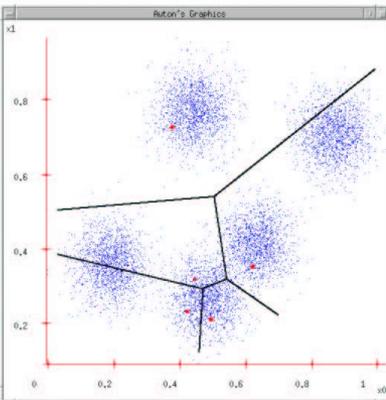
...



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K-means and Hierarchical Clustering: Slide 19

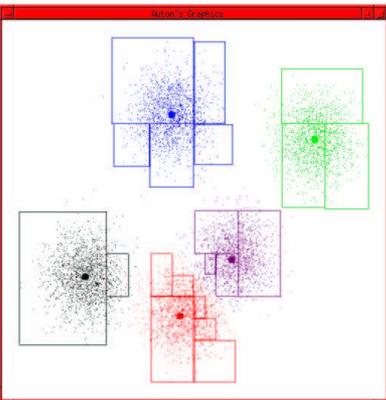
### K-means

1. Ask user how many clusters they'd like. (e.g.  $k=5$ )
2. Randomly guess k cluster Center locations
3. Each datapoint finds out which Center it's closest to. (Thus each Center "owns" a set of datapoints)



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K-means and Hierarchical Clustering: Slide 8

### K-means terminates



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K-means and Hierarchical Clustering: Slide 20

End

# K-Means Clustering [McQueen '67]

## Repeat

- Start with randomly chosen cluster centers
- Assign points to give greatest increase in score
- Recompute cluster centers
- Reassign points

until (no changes)

[Try the applet at:](http://home.dei.polimi.it/matteucc/Clustering/tutorial_html/AppletH.html)

[http://home.dei.polimi.it/matteucc/Clustering/tutorial\\_html/AppletH.html](http://home.dei.polimi.it/matteucc/Clustering/tutorial_html/AppletH.html)

# Comparisons

## □ Hierarchical clustering

- Number of clusters not preset.
- Complete hierarchy of clusters
- Not very robust, not very efficient.

## □ K-Means

- Need definition of a **mean**. Categorical data?
- More efficient and often finds optimum clustering.

## Functionally related genes behave similarly across experiments

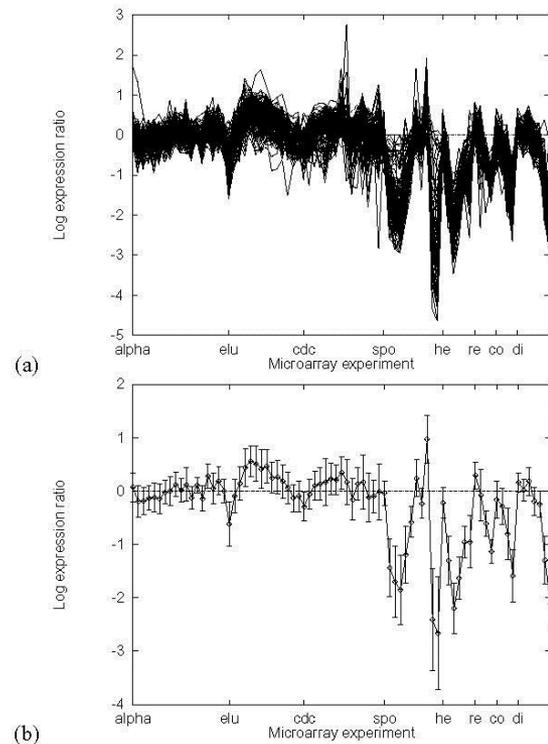


Figure 1: **Expression profiles of the cytoplasmic ribosomal proteins.** Figure (a) shows the expression profiles from the data in [Eisen et al., 1998] of 121 cytoplasmic ribosomal proteins, as classified by MYGD [MYGD, 1999]. The logarithm of the expression ratio is plotted as a function of DNA microarray experiment. Ticks along the X-axis represent the beginnings of experimental series. They are, from left to right, cell division cycle after synchronization with  $\alpha$  factor arrest (alpha), cell division cycle after synchronization by centrifugal elutriation (elu), cell division cycle measured using a temperature sensitive *cdc15* mutant (cdc), sporulation (spo), heat shock (he), reducing shock (re), cold shock (co), and diauxic shift (di). Sporulation is the generation of a yeast spore by meiosis. Diauxic shift is the shift from anaerobic (fermentation) to aerobic (respiration) metabolism. The medium starts rich in glucose, and yeast cells ferment, producing ethanol. When the glucose is used up, they switch to ethanol as a source for carbon. Heat, cold, and reducing shock are various ways to stress the yeast cell. Figure (b) shows the average, plus or minus one standard deviation, of the data in Figure (a).

# Self-Organizing Maps [Kohonen]

- ❑ Kind of neural network.
- ❑ Clusters data and find complex relationships between clusters.
- ❑ Helps reduce the dimensionality of the data.
- ❑ Map of 1 or 2 dimensions produced.
- ❑ Unsupervised Clustering
- ❑ Like K-Means, except for visualization

# SOM Architectures

- 2-D Grid
- 3-D Grid
- Hexagonal Grid

# SOM Algorithm

- Select SOM architecture, and initialize weight vectors and other parameters.
- **While** (stopping condition not satisfied) **do** for each input point  $x$ 
  - winning node  $q$  has weight vector **closest** to  $x$ .
  - **Update** weight vector of  $q$  and its **neighbors**.
  - **Reduce neighborhood size** and **learning rate**.

# SOM Algorithm Details

□ Distance between  $x$  and weight vector:  $\|x - w_i\|$

□ Winning node:  $q(x) = \min_i \|x - w_i\|$

□ Weight update function (for neighbors):

$$w_i(k+1) = w_i(k) + m(k, x, i)[x(k) - w_i(k)]$$

□ Learning rate:

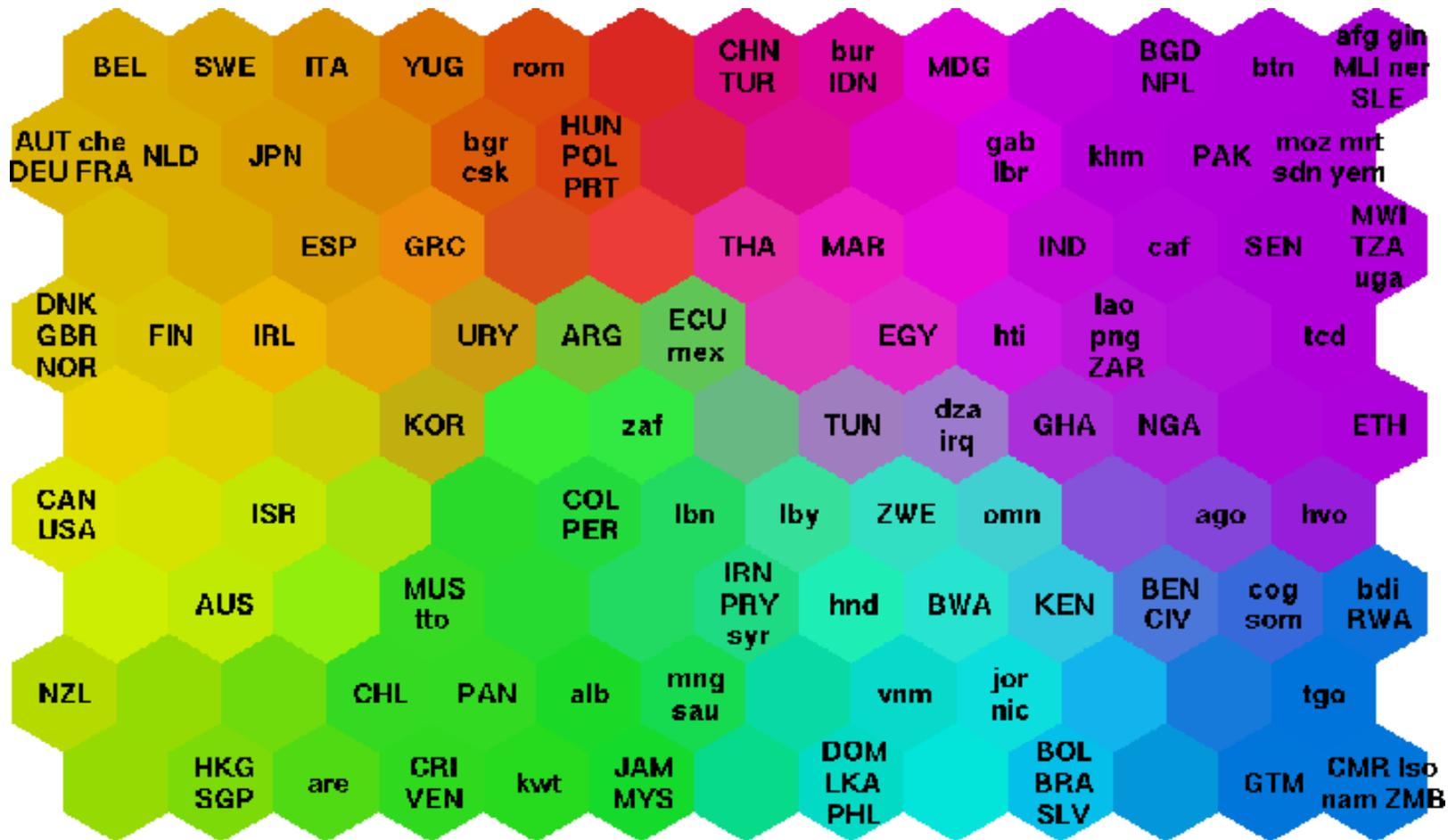
$$m(k, x, i) = h_0(k) \exp\left\{-\frac{\|r_i - r_{q(x)}\|^2}{S^2}\right\}$$

# World Bank Statistics

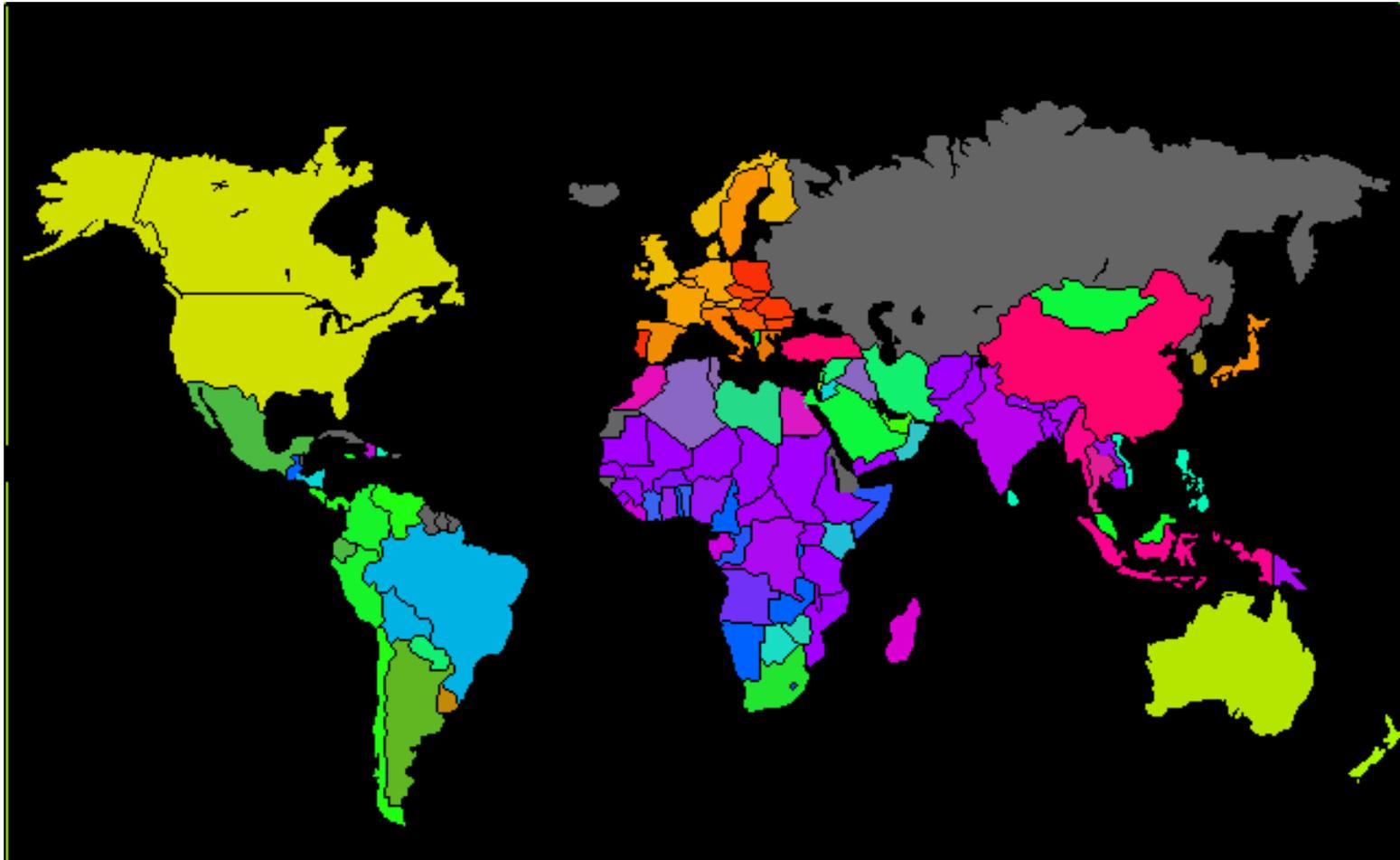
- ❑ Data: World Bank statistics of countries in 1992.
- ❑ 39 indicators considered e.g., health, nutrition, educational services, etc.
- ❑ The complex joint effect of these factors can be visualized by organizing the countries using the self-organizing map.

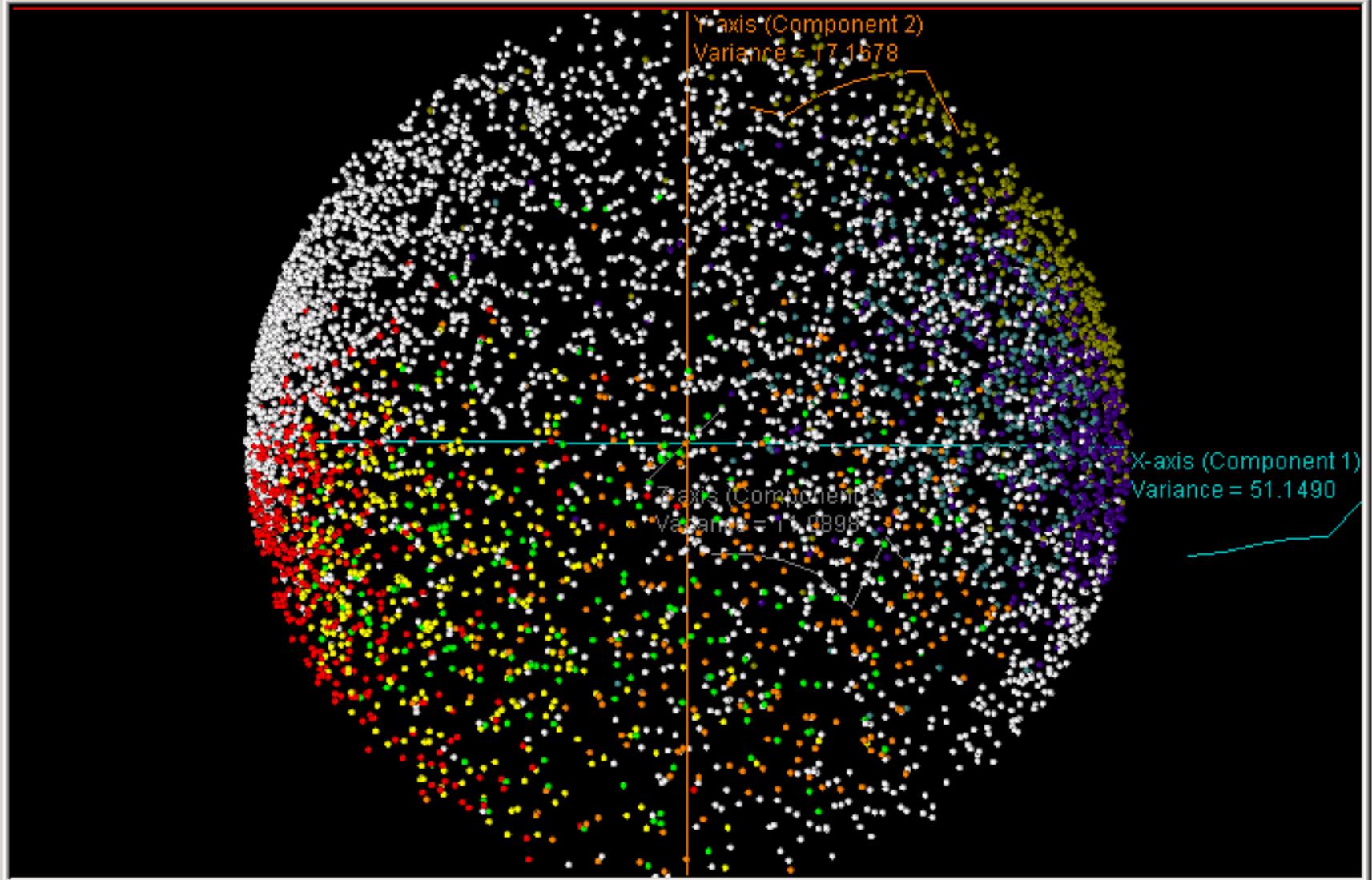


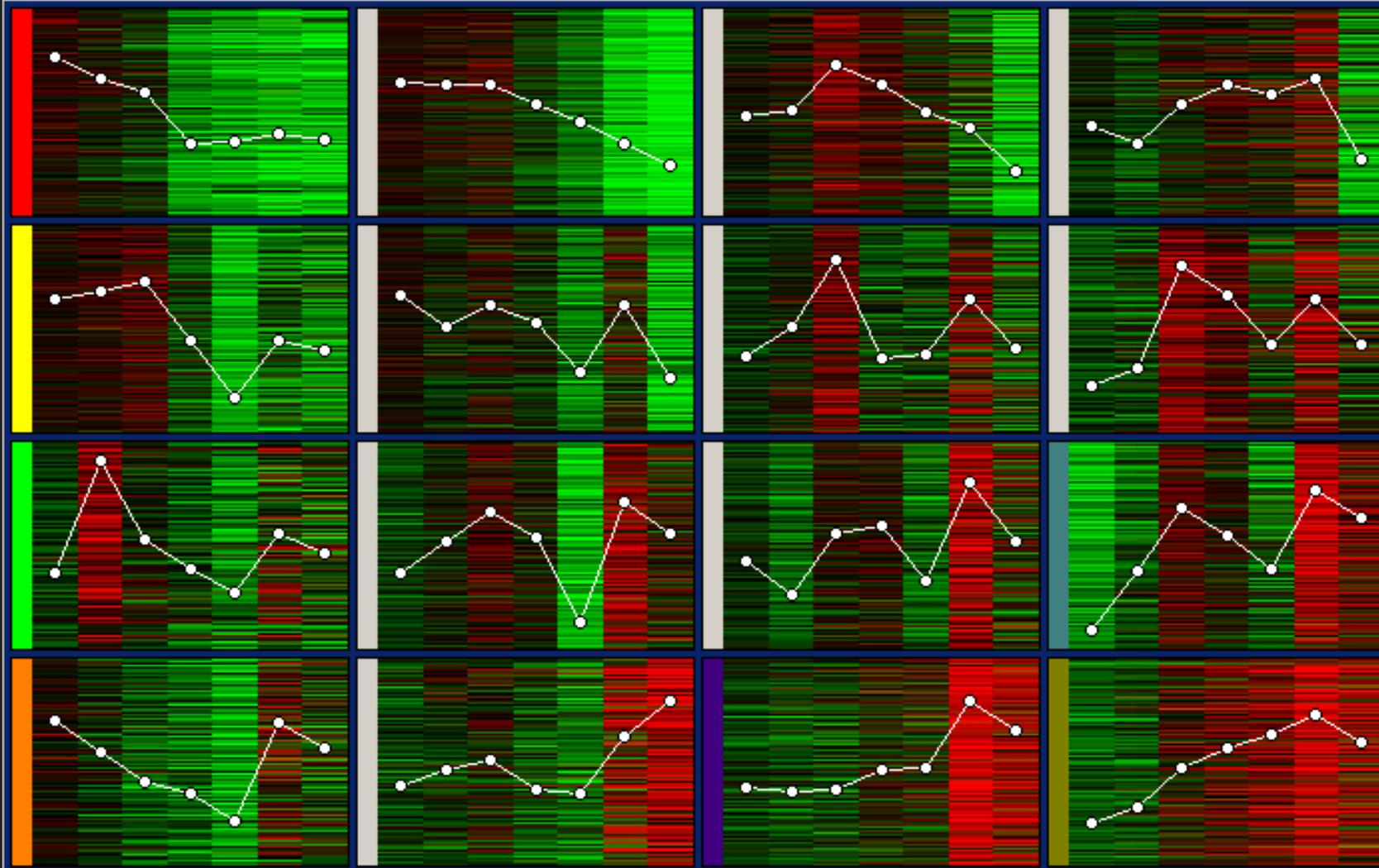
# World Poverty SOM



# World Poverty Map

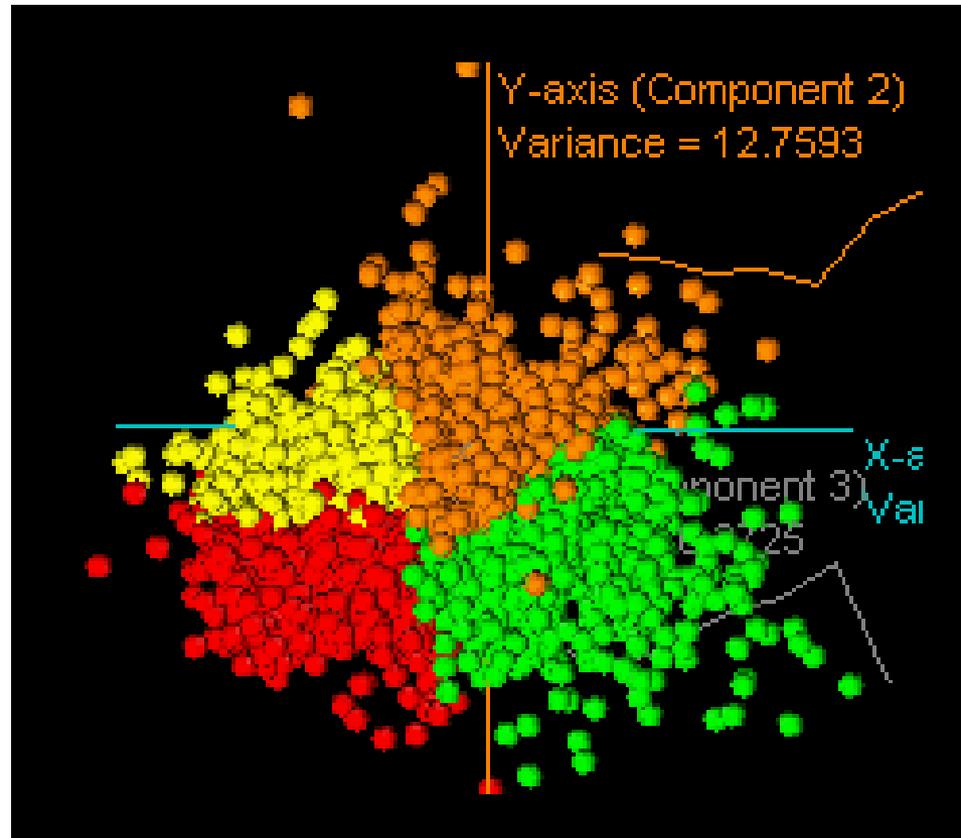




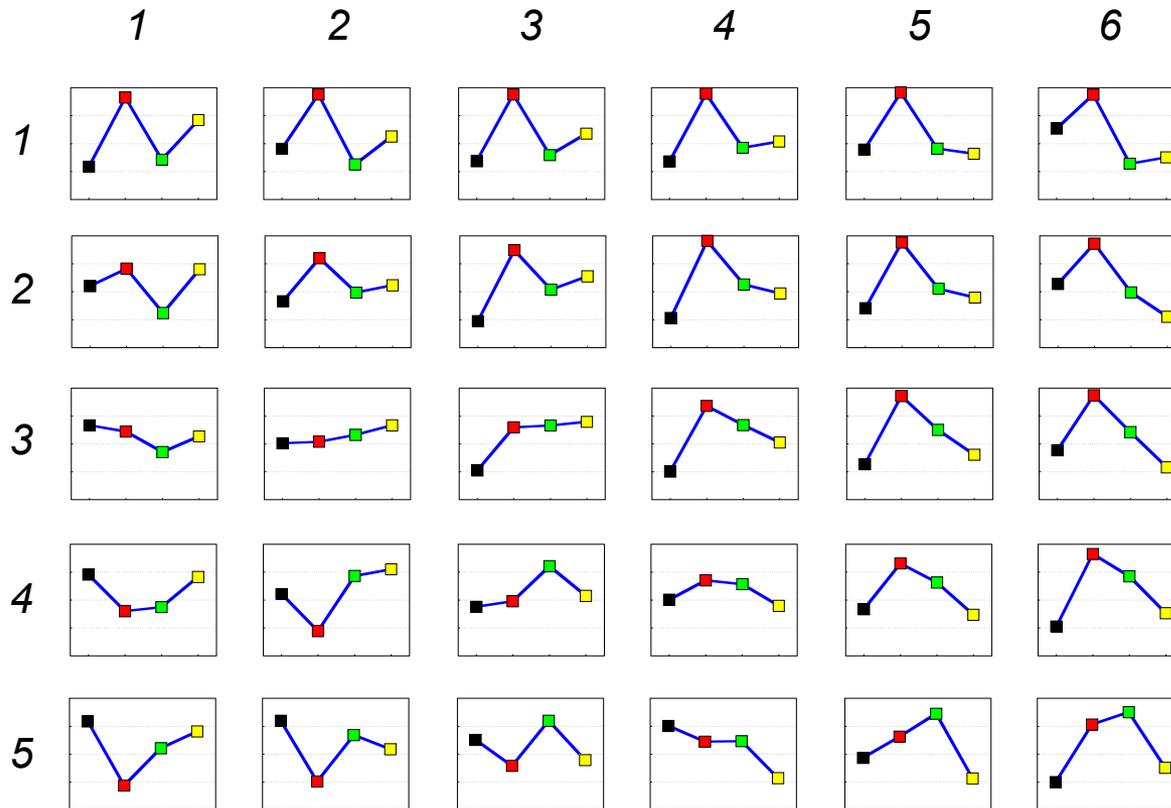


Summary Graph **Visualizations** Results Parameters Report

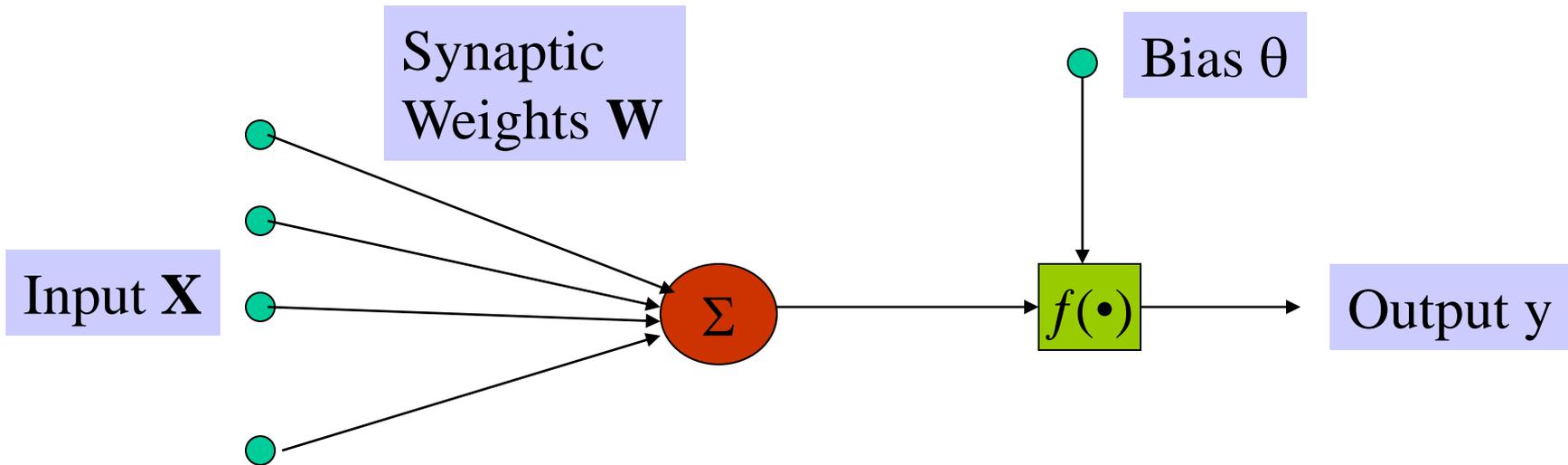
# Viewing SOM Clusters on PCA axes



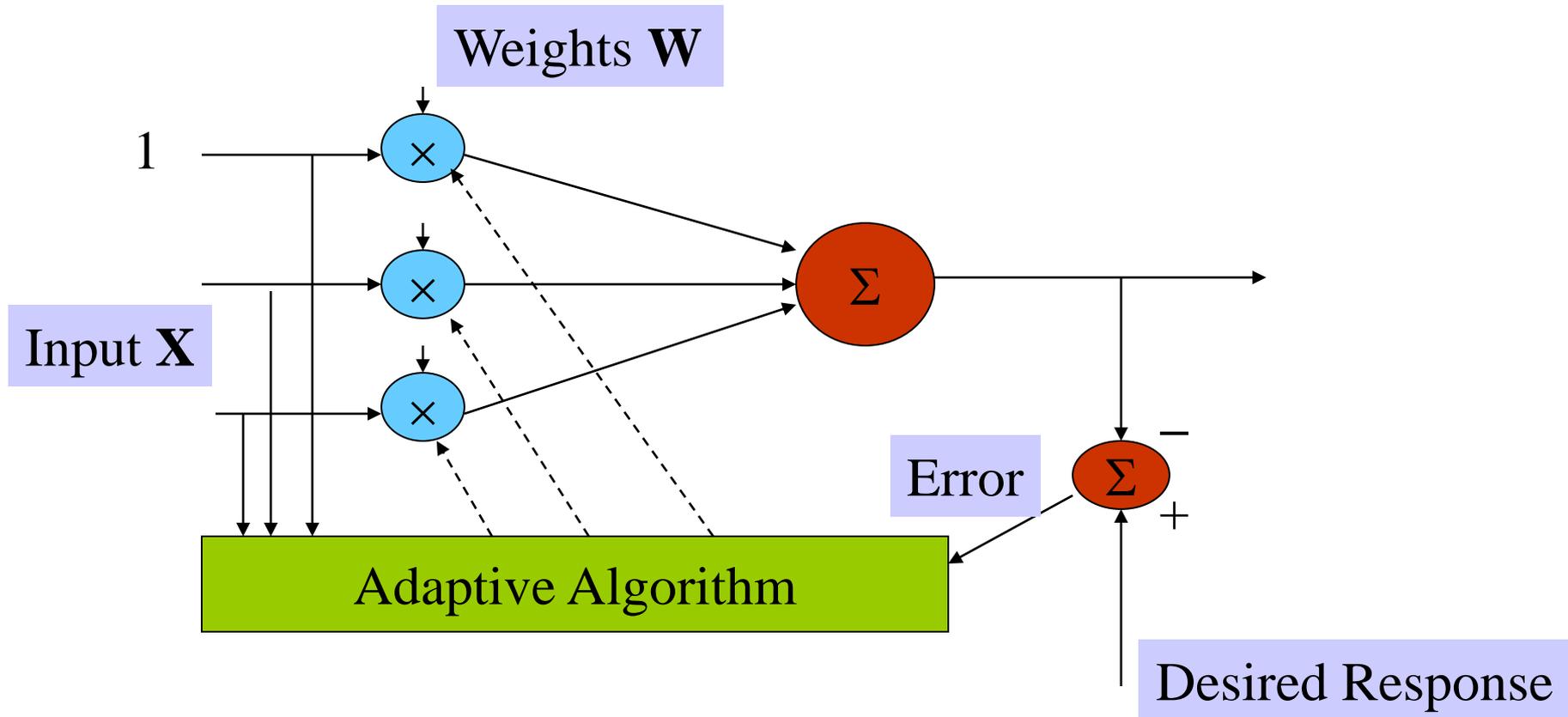
# SOM Example [Xiao-ru He]



# Neural Networks



# Learning NN



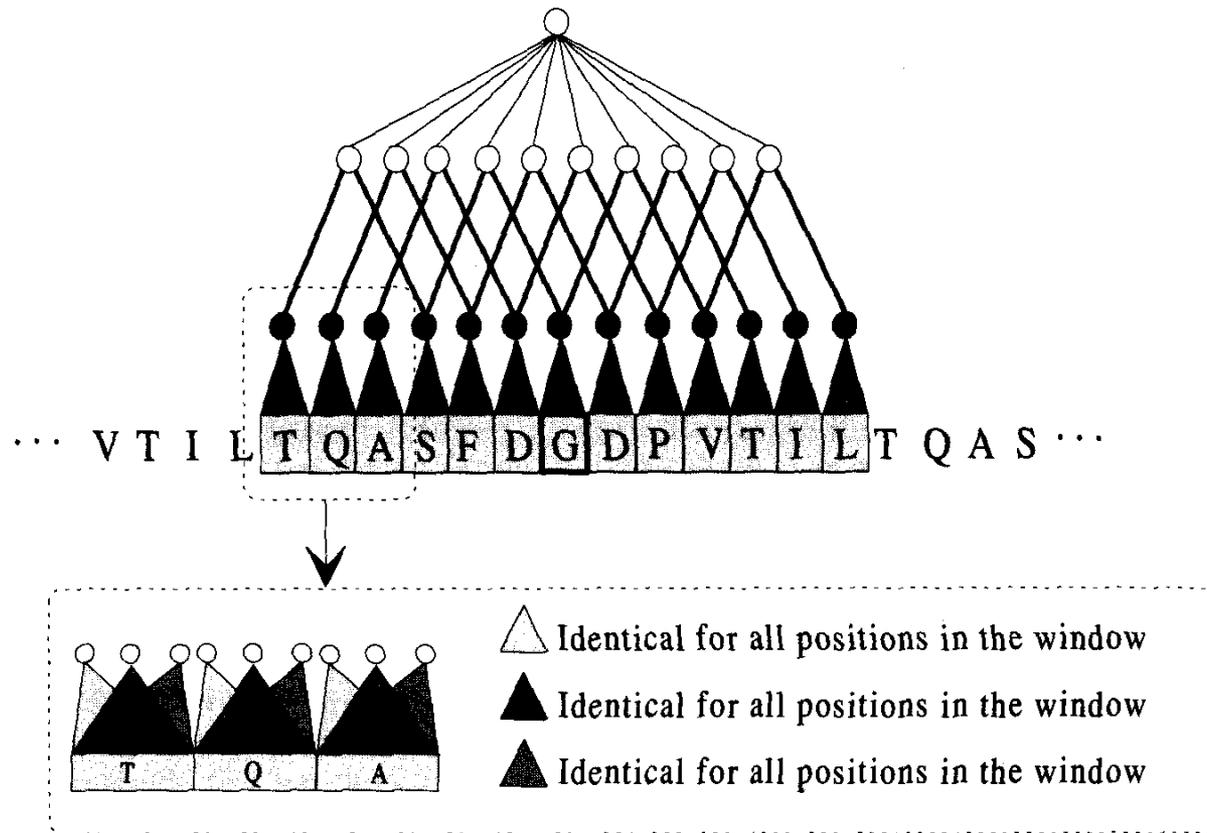
# Types of NNs

- Recurrent NN
- Feed-forward NN
- Layered

## Other issues

- Hidden layers possible
- Different activation functions possible

# Application: Secondary Structure Prediction



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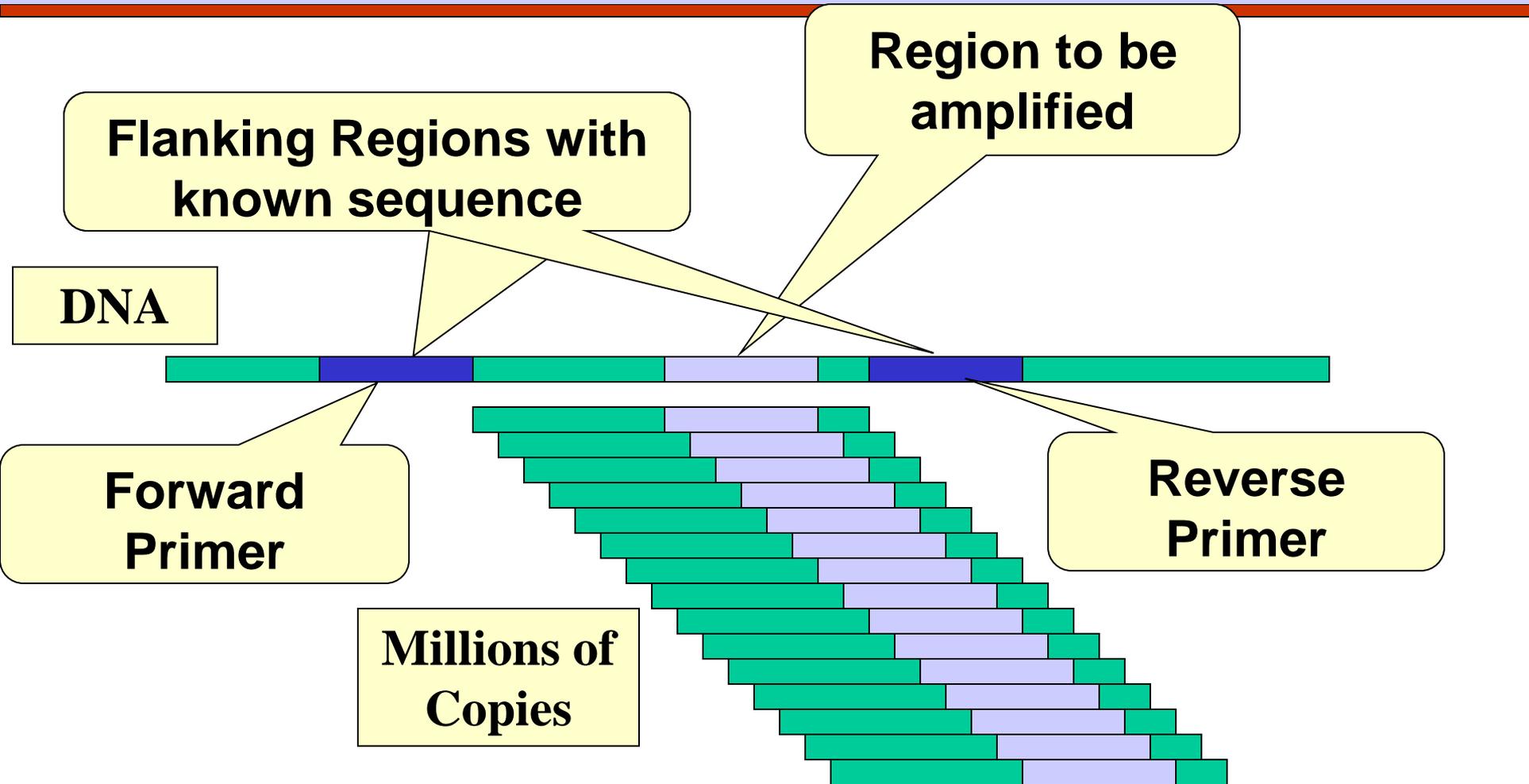
# PCR and Sequencing



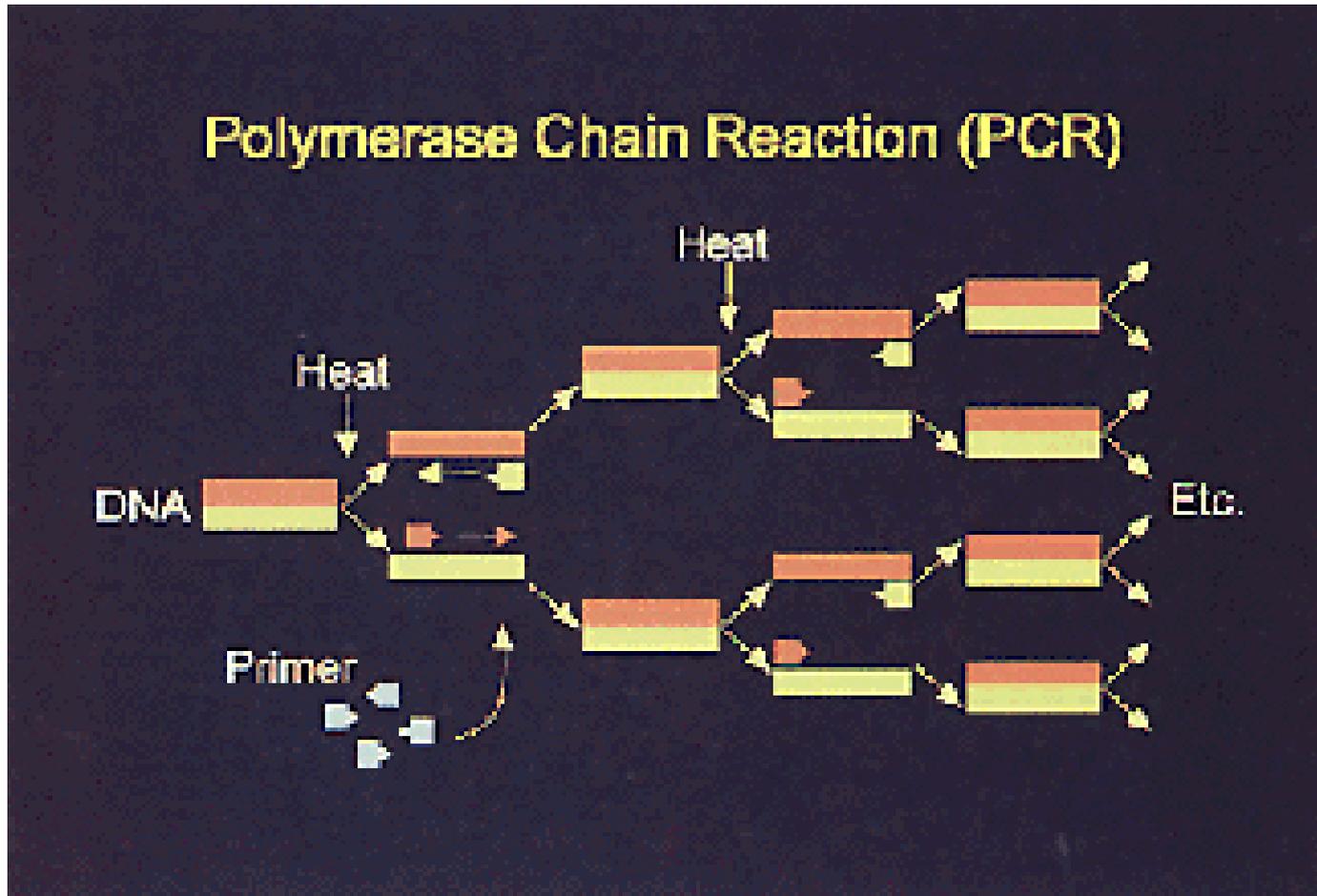
# Polymerase Chain Reaction (PCR)

- For testing, large amount of DNA is needed
  - Identifying individuals for forensic purposes
    - (0.1 microliter of saliva contains enough epithelial cells)
  - Identifying pathogens (viruses and/or bacteria)
- PCR is a technique to amplify the number of copies of a specific region of DNA.
- Useful when exact DNA sequence is unknown
- Need to know "flanking" sequences
- Primers designed from "flanking" sequences

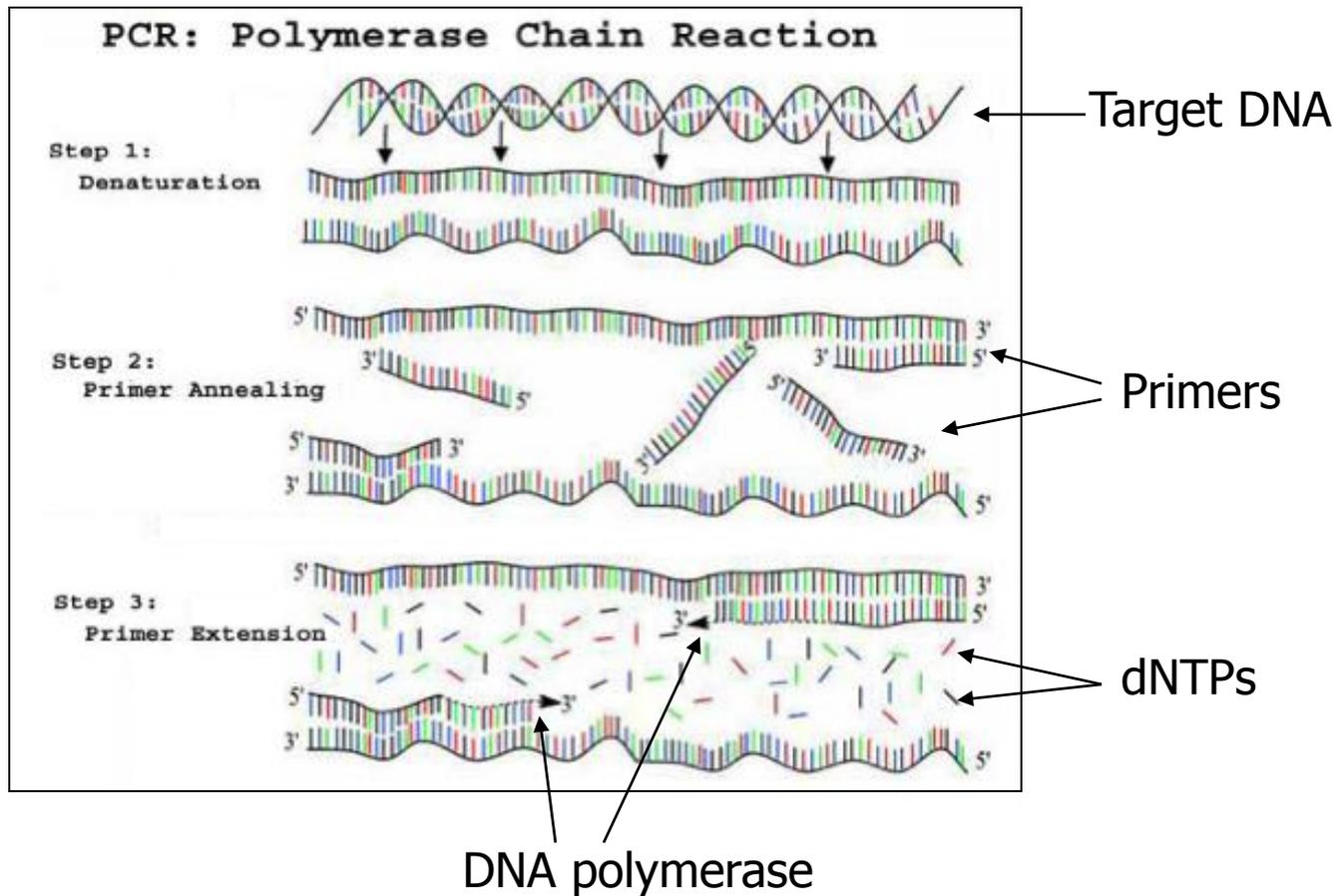
# PCR



# PCR

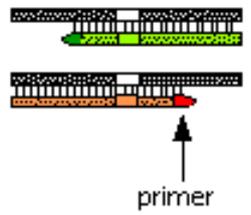
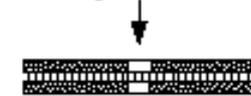


# Schematic outline of a typical PCR cycle



# POLYMERASE CHAIN REACTION

DNA region of interest.



primer

1. DNA is denatured. Primers attach to each strand. A new DNA strand is synthesized behind primers on each template strand.



2. Another round: DNA is denatured, primers are attached, and the number of DNA strands are doubled.



3. Another round: DNA is denatured, primers are attached, and the number of DNA strands are doubled.



4. Another round: DNA is denatured, primers are attached, and the number of DNA strands are doubled.



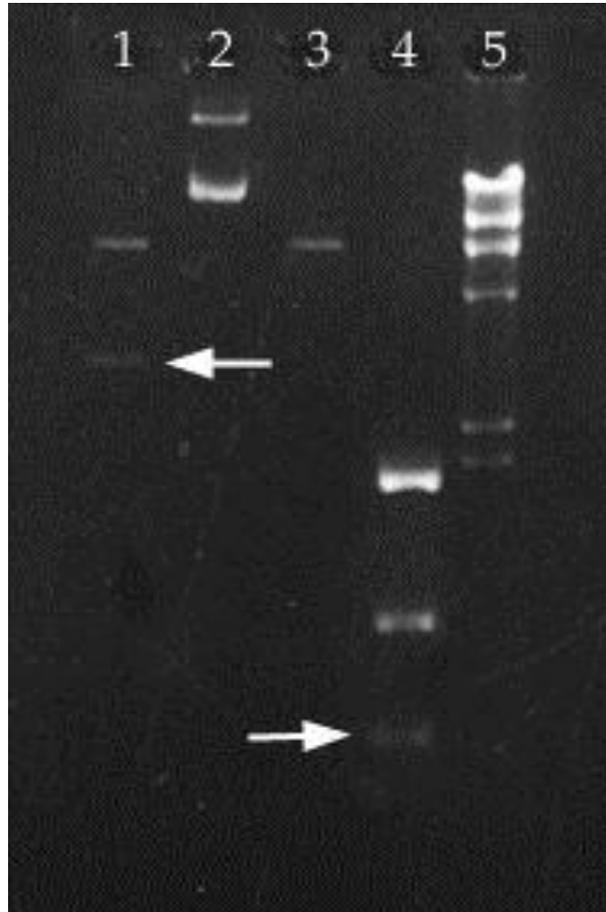
5. Continued rounds of amplification swiftly produce large numbers of identical fragments. Each fragment contains the DNA region of interest.



# Gel Electrophoresis

- ❑ Used to measure the lengths of DNA fragments.
- ❑ When voltage is applied to DNA, different size fragments migrate to different distances (smaller ones travel farther).

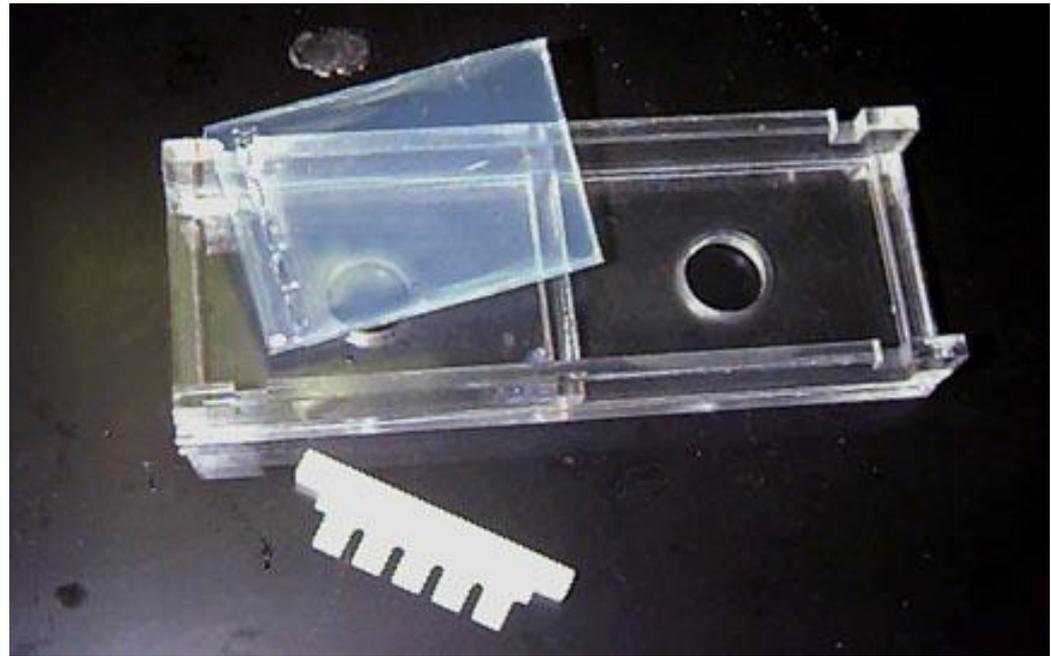
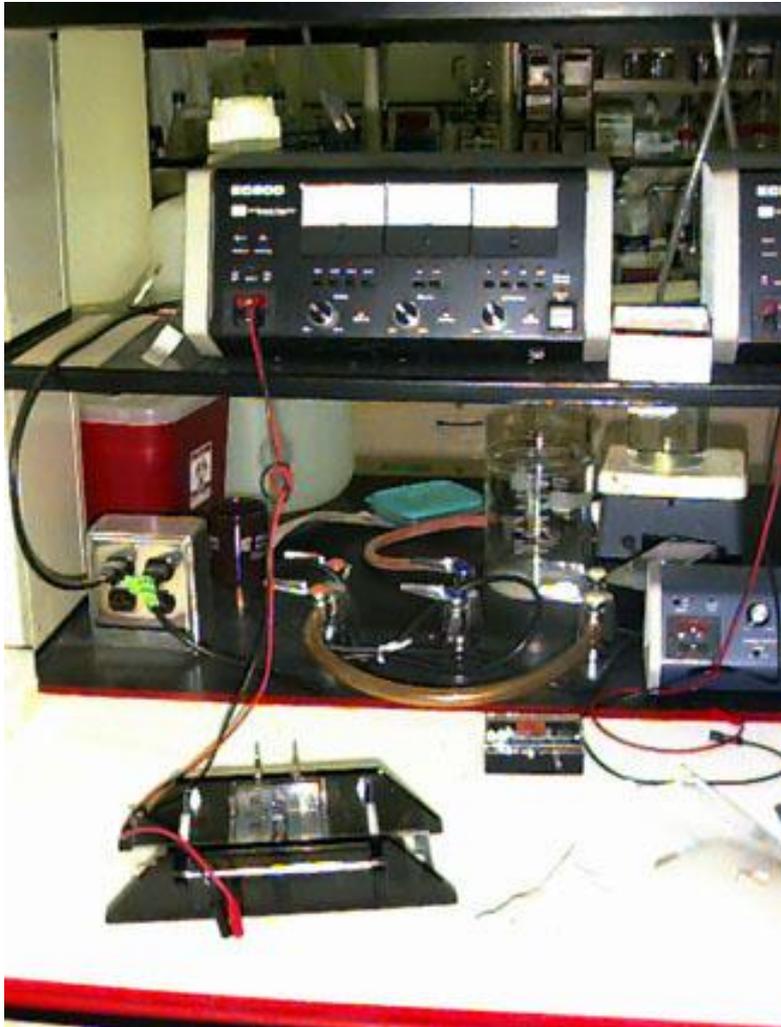
# Gel Pictures



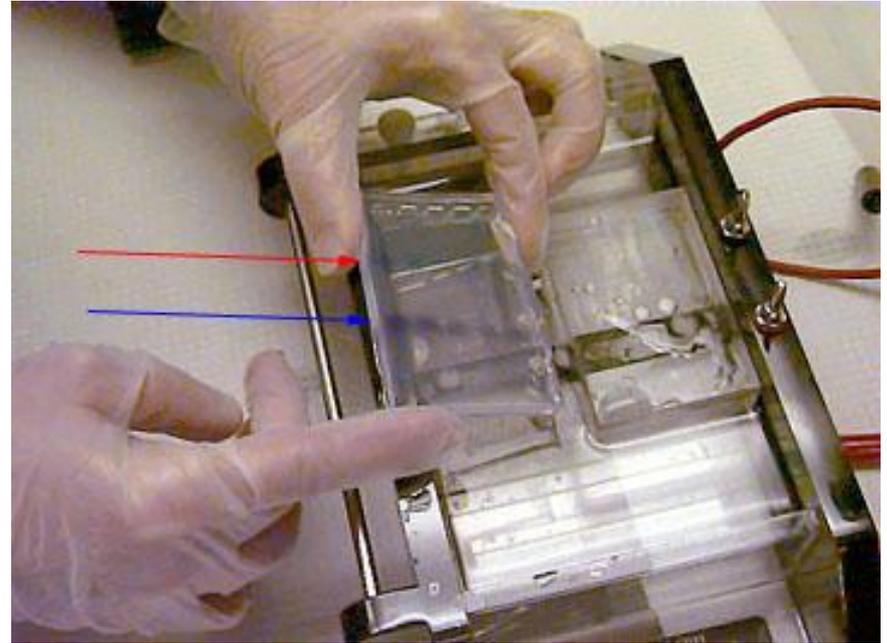
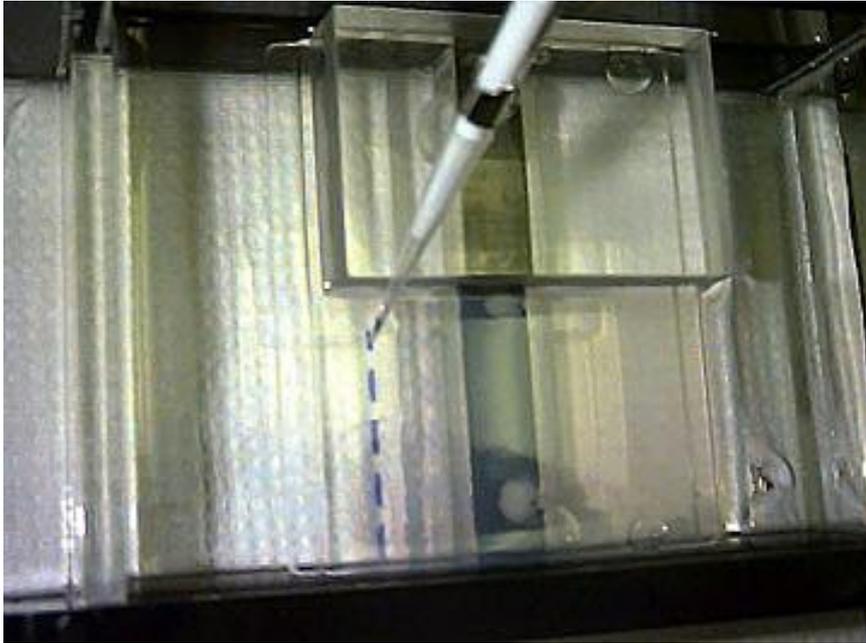
# Gel Electrophoresis: Measure sizes of fragments

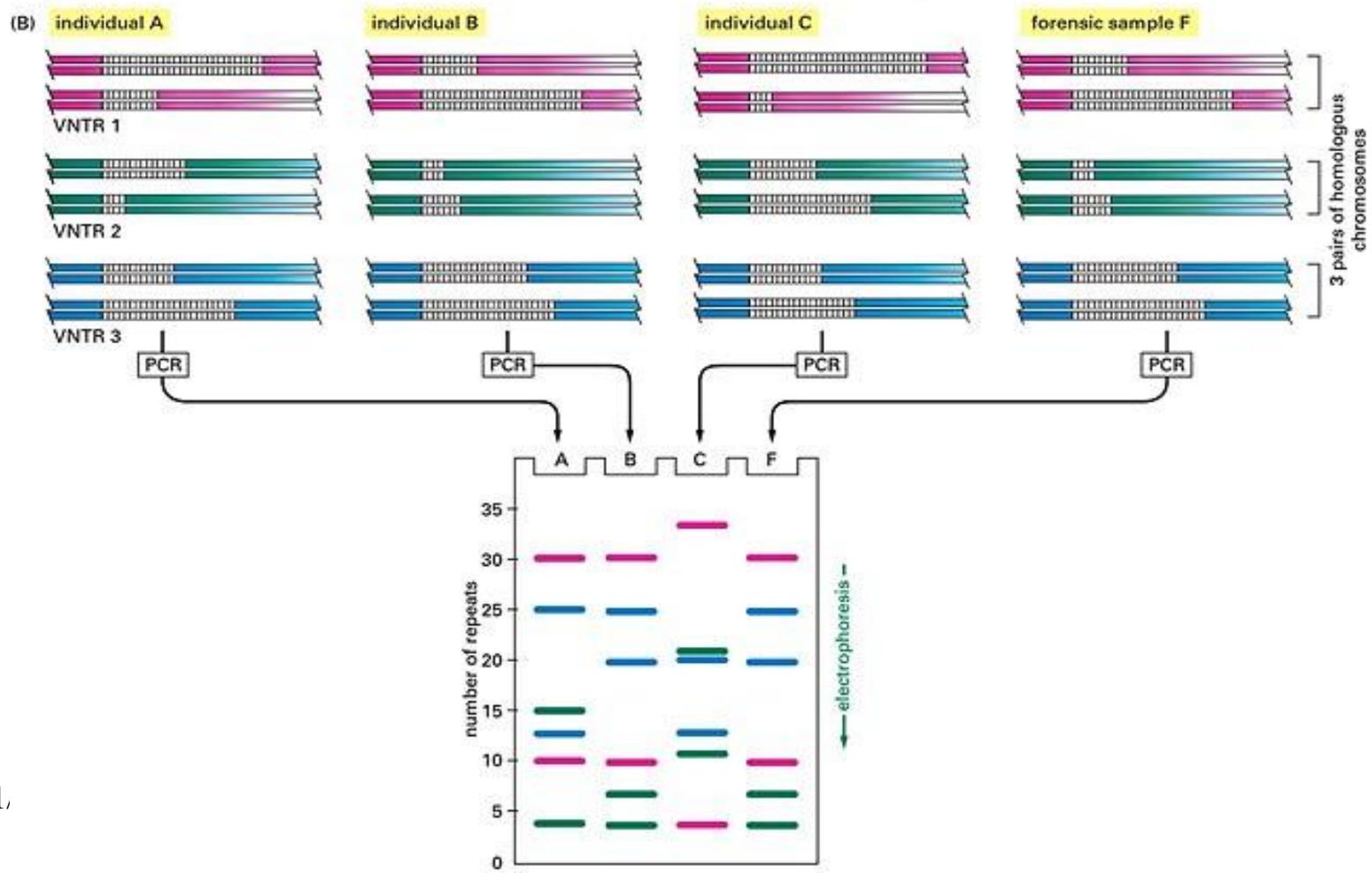
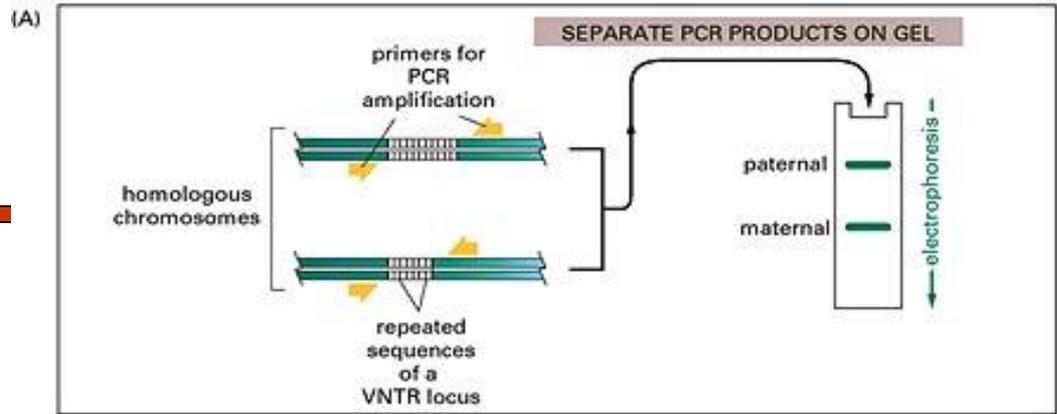
- ❑ The phosphate backbone makes DNA a highly negatively charged molecule.
- ❑ DNA can be separated according to its size.
- ❑ **Gel**: allow hot 1% solution of purified agarose to cool and solidify/polymerize.
- ❑ DNA sample added to wells at the top of a gel and voltage is applied. Larger fragments migrate through the pores slower.
- ❑ Varying concentration of agarose makes different pore sizes & results.
- ❑ Proteins can be separated in much the same way, only acrylamide is used as the crosslinking agent.

# Gel Electrophoresis



# Gel Electrophoresis





# Sequencing



# Why sequencing?

## □ Useful for further study:

- Locate gene sequences, regulatory elements
- Compare sequences to find similarities
- Identify mutations
- Use it as a basis for further experiments

Next 4 slides contains material prepared by Dr. Stan Metzenberg. Also see:  
<http://stat-www.berkeley.edu/users/terry/Courses/s260.1998/Week8b/week8b/node9.html>

# History

- Two methods independently developed in 1974
  - Maxam & Gilbert method
  - Sanger method: became the standard
- Nobel Prize in 1980

# Original Sanger Method

- (Labeled) Primer is annealed to template strand of denatured DNA. This primer is specifically constructed so that its 3' end is located next to the DNA sequence of interest. Once the primer is attached to the DNA, the solution is divided into four tubes labeled "G", "A", "T" and "C". Then reagents are added to these samples as follows:
  - "G" tube: ddGTP, DNA polymerase, and all 4 dNTPs
  - "A" tube: ddATP, DNA polymerase, and all 4 dNTPs
  - "T" tube: ddTTP, DNA polymerase, and all 4 dNTPs
  - "C" tube: ddCTP, DNA polymerase, and all 4 dNTPs
- DNA is synthesized, & nucleotides are added to growing chain by the DNA polymerase. Occasionally, a ddNTP is incorporated in place of a dNTP, and the chain is terminated. Then run a gel.
- All sequences in a tube have same prefix and same last nucleotide.
- <http://www.wellcome.ac.uk/Education-resources/Teaching-and-education/Animations/DNA/WTDV026689.htm>

# Sanger Method

- Example of sequences seen in gel from "G" tube:

```
5' -GAATGTCCTTTCTCTAAGTCCTAAG
3' -GGAGACTTACAGGAAAGAGATTCAGGATTCAGGAGGCCTACCATGAAGATCAAG-5'

5' -GAATGTCCTTTCTCTAAGTCCTAAGTCCTCCG
3' -GGAGACTTACAGGAAAGAGATTCAGGATTCAGGAGGCCTACCATGAAGATCAAG-5'

5' -GAATGTCCTTTCTCTAAGTCCTAAGTCCTCCG
3' -GGAGACTTACAGGAAAGAGATTCAGGATTCAGGAGGCCTACCATGAAGATCAAG-5'

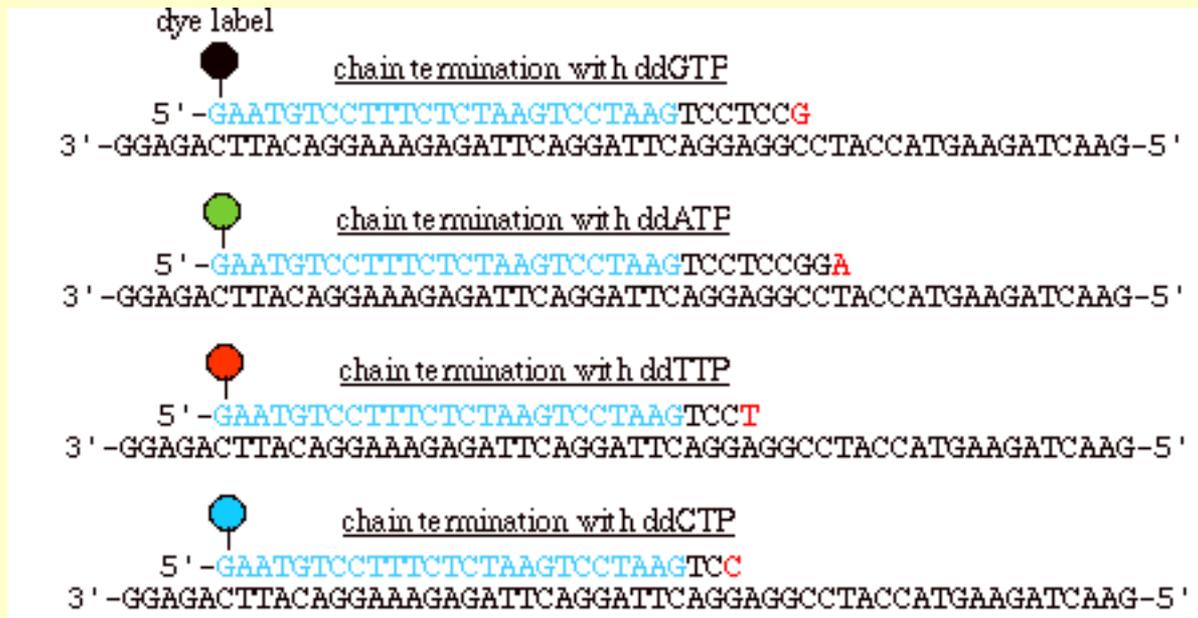
5' -GAATGTCCTTTCTCTAAGTCCTAAGTCCTCCGGATG
3' -GGAGACTTACAGGAAAGAGATTCAGGATTCAGGAGGCCTACCATGAAGATCAAG-5'

5' -GAATGTCCTTTCTCTAAGTCCTAAGTCCTCCGGATG
3' -GGAGACTTACAGGAAAGAGATTCAGGATTCAGGAGGCCTACCATGAAGATCAAG-5'

5' -GAATGTCCTTTCTCTAAGTCCTAAGTCCTCCGGATGGTACTTCTAG
3' -GGAGACTTACAGGAAAGAGATTCAGGATTCAGGAGGCCTACCATGAAGATCAAG-5'
```

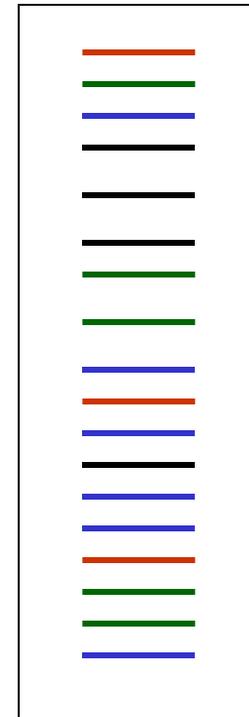
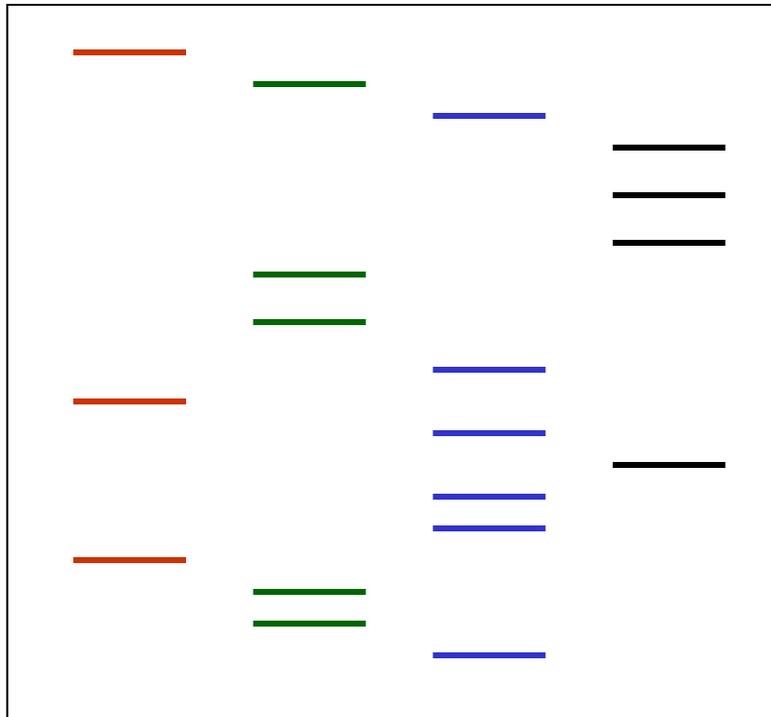
# Modified Sanger

- Reactions performed in a single tube containing all four ddNTP's, each labeled with a different color dye



# Sequencing Gels: Separate vs Single Lanes

GCCAGGTGAGCCTTTGCA



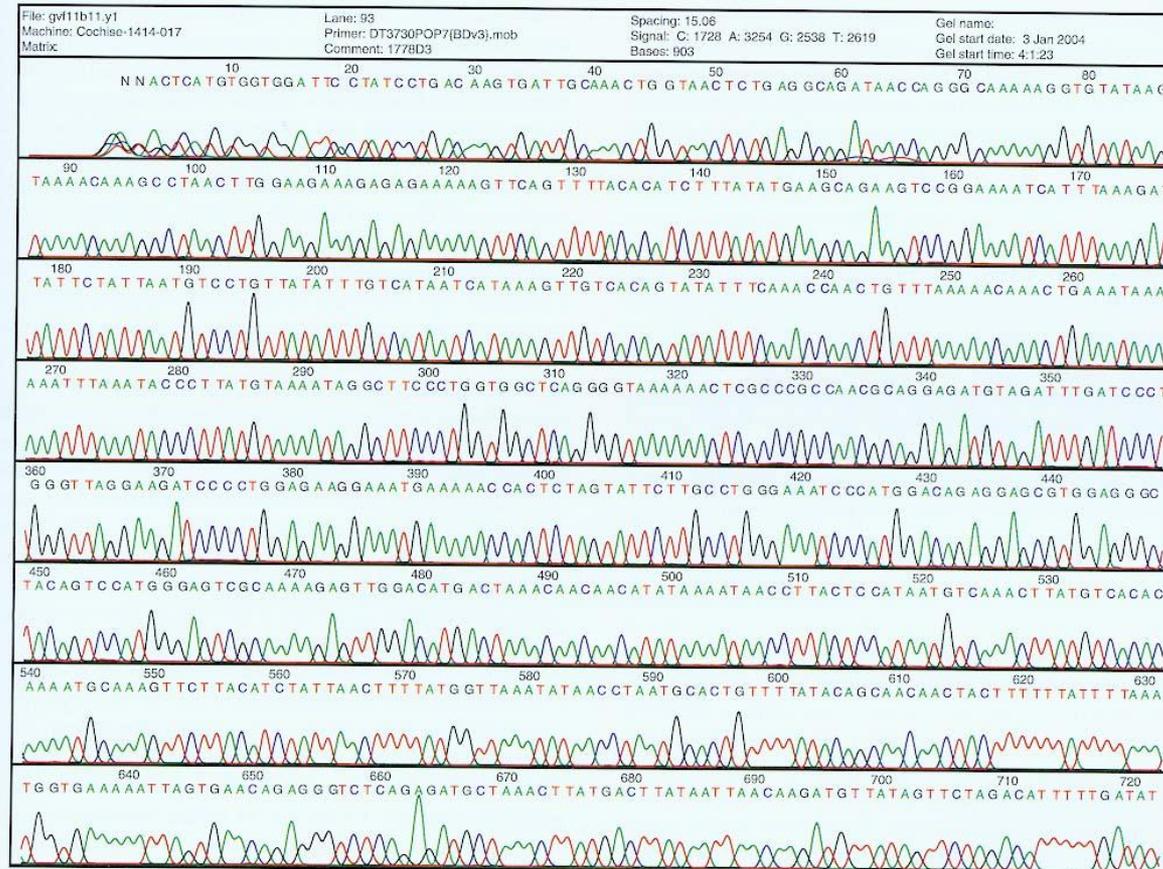
**A**

**C**

**G**

**T**

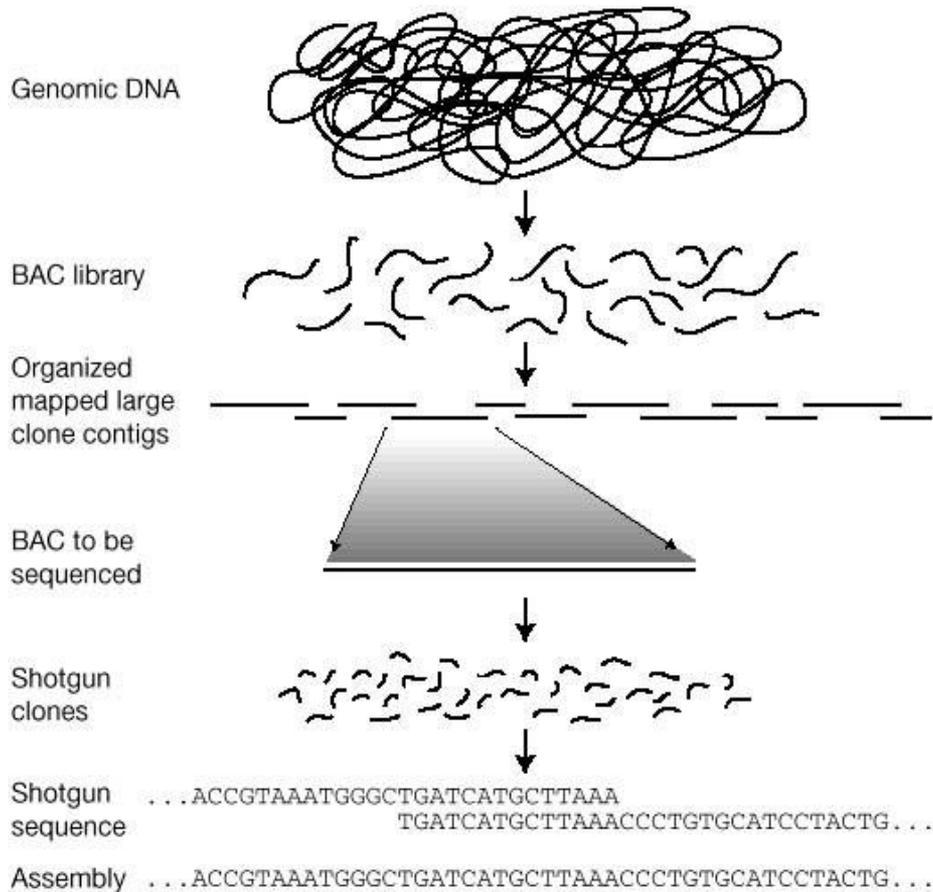
# Sequencing



**FIGURE 13.3** A sample chromatogram, as viewed with the vtrace program (Ewing, 2002). Signal intensities corresponding to fragments ending with A (green), C (blue), G (black), and T (red) are shown out to approximately 722 bases.

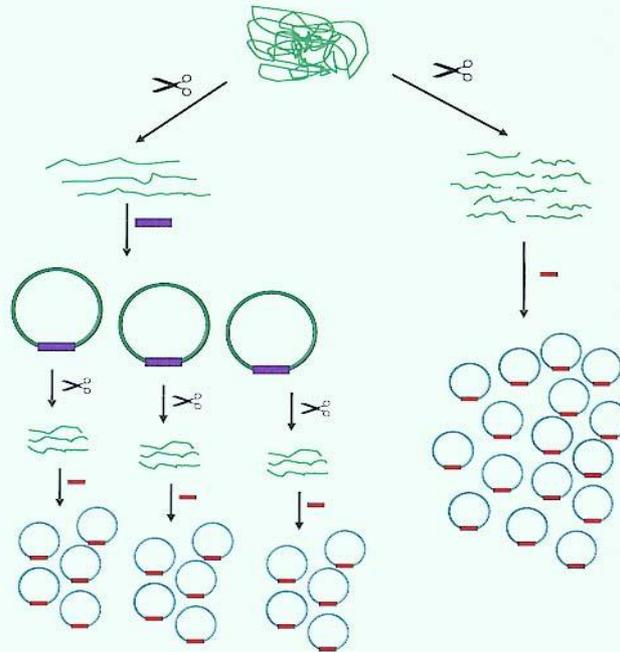
# Shotgun Sequencing

## Hierarchical shotgun sequencing



From <http://www.tulane.edu/~biochem/lecture/723/humgen.html>

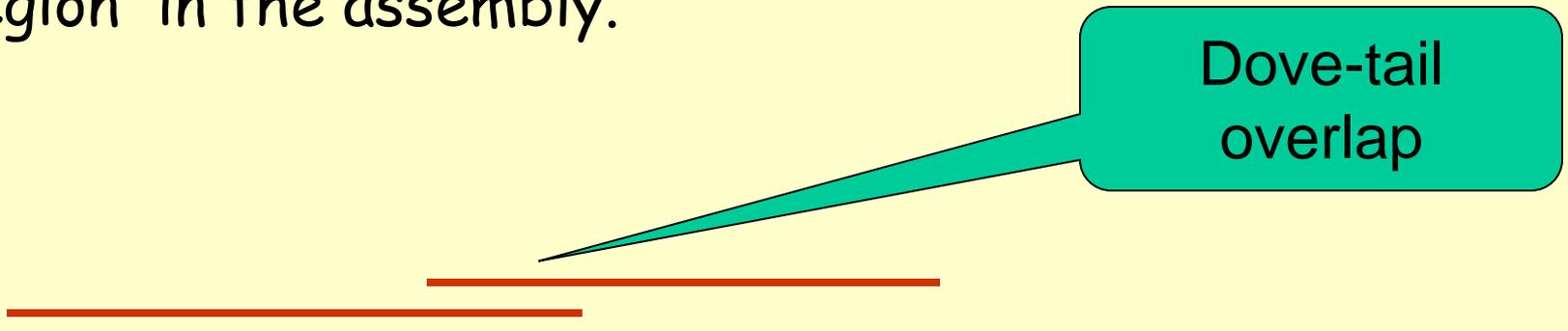
# Sequencing



**FIGURE 13.1** Shotgun cloning. Genomic DNA sequencing begins with isolated genomic DNA in green at the top of the figure. In the hierarchical clone-based shotgun approach on the left, DNA is sheared and the size is selected for large fragments on the order of 200 Kb, then ligated to a suitable vector, such as a BAC vector shown in blue. Individually isolated clones in turn are sheared independently, generating fragments of approximately 4 Kb, which are then ligated to a small-scale vector, typically a plasmid (red bar) suitable for sequencing reactions. The whole genome shotgun approach bypasses the intermediate large-insert clone and generates large numbers of small fragments, typically 4 Kb and 10 Kb.

# Sequencing: Generate Contigs

- Short for "contiguous sequence". A continuously covered region in the assembly.



Dove-tail overlap



Collapsing into a single sequence

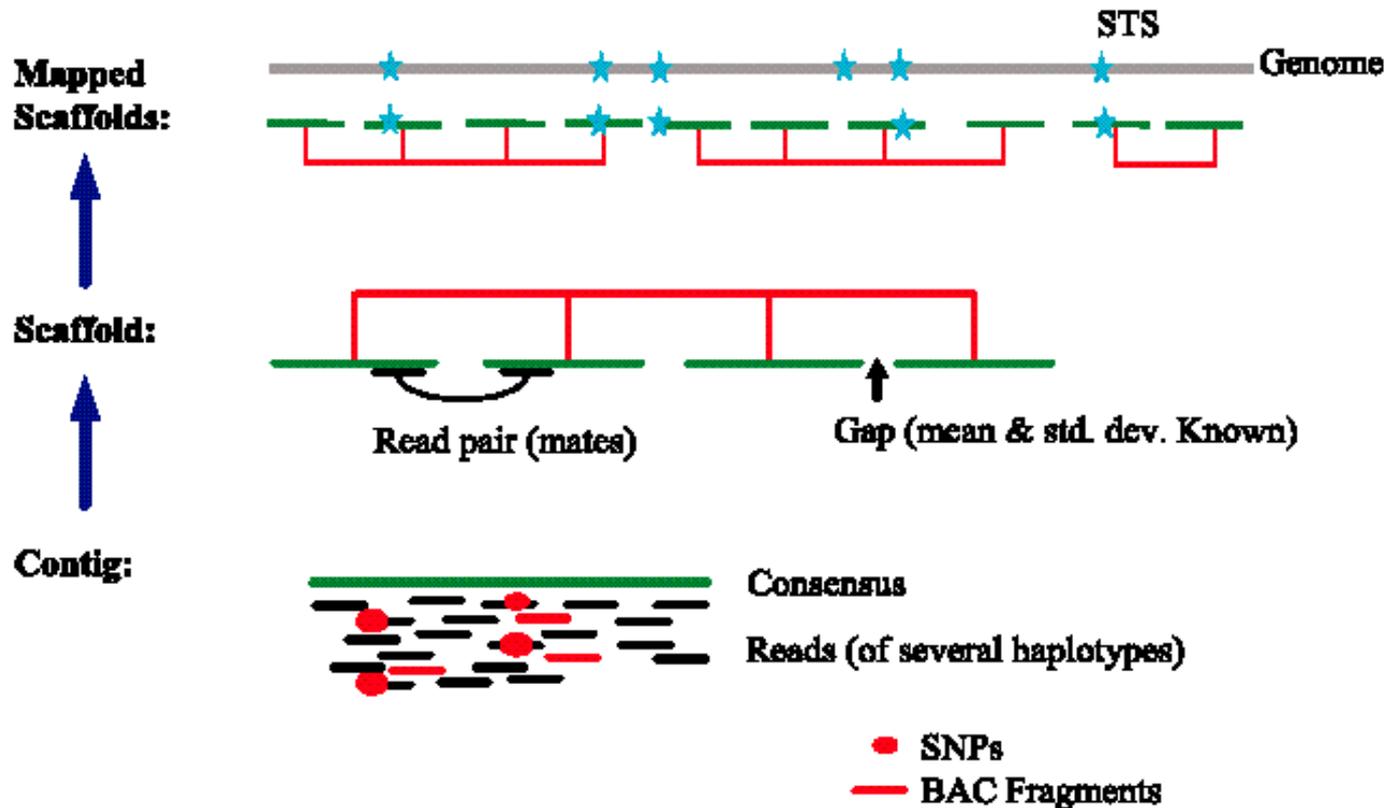
- Jang W et al (1999) Making effective use of human genomic sequence data. *Trends Genet.* 15(7): 284-6.
- Kent WJ and Haussler D (2001) Assembly of the working draft of the human genome with *GigAssembler*. *Genome Res* 11(9): 1541-8.

# Paired Reads

- **Scaffold (supercontig)**: formed when two **contigs** with no sequence overlap can be linked
  - Data from paired end reads help create scaffolds with known gaps
    - If two reads end up in two different contigs, then we can link contigs to form scaffold.



# Shotgun Sequencing



From <http://www.tulane.edu/~biochem/lecture/723/humgen.html>

# Human Genome Project

- ❑ Many videos available on youtube.com, dnatube.com, and elsewhere.
- ❑ Find some and watch them.

# Assembly: Simple Example

□ ACCGT, CGTGC, TTAC, TACCGT

□ Total length = ~10

□

- --ACCGT--
- ----CGTGC
- TTAC-----
- -TACCGT-
- TTACCGTGC

# Assembly: Complications

- Errors in input sequence fragments (~3%)
  - Indels or substitutions
- Contamination by host DNA
- Chimeric fragments (joining of non-contiguous fragments)
- Unknown orientation
- Repeats (long repeats)
  - Fragment contained in a repeat
  - Repeat copies not exact copies
  - Inherently ambiguous assemblies possible
  - Inverted repeats
- Inadequate Coverage

# Assembly: Complications

$w = \text{AGTATTGGCAATC}$   
 $z = \text{AATCGATG}$   
 $u = \text{ATGCAAACCT}$   
 $x = \text{CCTTTTGG}$   
 $y = \text{TTGGCAATCACT}$

```

AGTATTGGCAATC---AATCGATG-----
-----ATGCAAACCT-----
---TTGGCAATCACT-----CCTTTTGG
-----
AGTATTGGCAATCACTAATCGATGCAAACCTTTTGG
    
```

**FIGURE 4.20**

*A bad solution for an assembly problem, with a multiple alignment whose consensus is a shortest common superstring. This solution has length 36 and is generated by the Greedy algorithm. However, its weakest link is zero.*

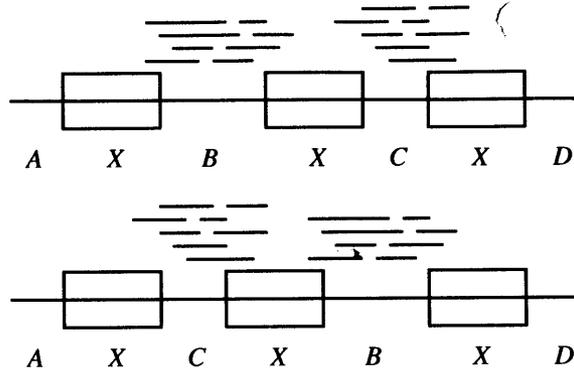
```

AGTATTGGCAATC-----CCTTTTGG-----
-----AATCGATG-----TTGGCAATCACT
-----ATGCAAACCT-----
-----
AGTATTGGCAATCGATGCAAACCTTTTGGCAATCACT
    
```

**FIGURE 4.21**

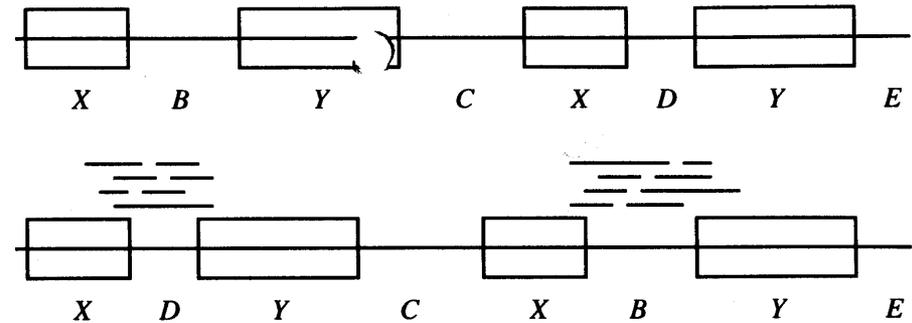
*Solution according to the unique Hamiltonian path. This solution has length 37, but exhibits better linkage. Its weakest link is 3.*

# Assembly: Complications



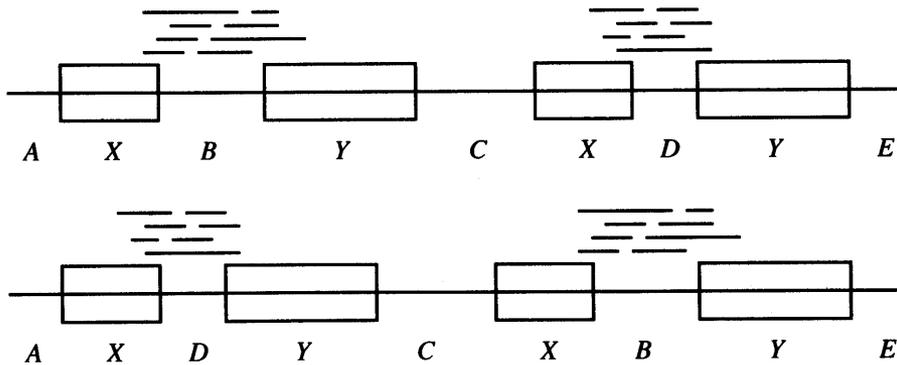
**FIGURE 4.8**

Target sequence leading to ambiguous assembly because of repeats of the form  $XXX$ .



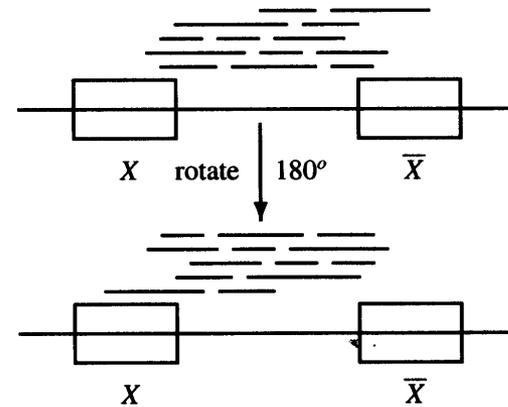
**FIGURE 4.9**

Target sequence leading to ambiguous assembly because of repeats of the form  $XYXY$ .



**FIGURE 4.9**

Target sequence leading to ambiguous assembly because of repeats of the form  $XYXY$ .



**FIGURE 4.10**

Target sequence with inverted repeat. The region marked  $\bar{X}$  is the reverse complement of the region marked  $X$ .