# A General Greedy Channel Routing Algorithm 

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#### Abstract

This paper presents a new channel routing algorithm which assigns wires track by track in a greedy way. The simple underlying data structures and strategy used in this algorithm can be generalized to obtain a class of heuristic channel routing algorithms. The proposed new algorithm has a backtracking capability to increase the chance of completing the routing with a minimum number of tracks. Since the concepts described in this paper are general, they can be applied to other channel problems such as switchbox routing, three-layer routing, and multilayer routing, or it can be even applied to the overlap model with only a few modifications. It successfully routes both the Burstein's difficult switchbox problem and Deutsch's difficult example with 19 tracks in the Manhattan model without any backtracking. The extensions of this algorithm are presented with examples.


Keywords and Phrases-Channel routing algorithm, data structure, backtracking, Manhattan model.

## I. Introduction

EFFICIENT chip design reflects the capabilities of the semiconductor lithography in the areas of logic, circuit, layout, and processing. The routing portion of the VLSI layout problems is to realize a particular interconnection among different modules in as small area as possible. In general, many routing strategies exist for efficient interconnections among different modules of the VLSI layout problem.
One of the most important forms of routing strategies is called "channel routing." This approach allows us to reduce the extremely difficult VLSI layout problem to a collection of simpler subproblems. Typically a channel router is designed to assign wires that interconnect terminals on two opposite sides of a rectangular region called a "channel." Normally the virtual grid is assumed and the Manhattan model is adopted, i.e., all the horizontal wire segments are routed in one layer and all vertical wire segments in the other, and the connection between wires in these two layers is through some electrical contacts called vias. Since the interconnection area usually represents $65-80 \%$ of the total area in a typical polycell integrated circuit design, the primary goal of a channel router is to minimize the above mentioned area by minimizing the number of tracks used. The number of vias and the length of wires are also important in evaluating the quality of the routing.
In recent years we have witnessed a tremendous surge in the development of efficient channel routing algorithms for many types of problems. Normally, all the algorithms can be divided into two categories: those in the overlap model, which allow some wire segments in different conducting layers to be overlapped, and those in the nonoverlap model, which do not allow the overlaps. Traditionally, the nonoverlap model can be further divided into the Manhattan model, which restricts all the

Manuscript received November 9, 1988; revised October 5, 1989. This paper was recommended by Associate Editor, R. H. J. M. Otten.

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IEEE Log Number 9040261.
horizontal wire segments to run in one layer and all the vertical wire segments to run in the other, and the knock-knee model which is free of this restriction. Major past research on the channel routing includes [1]-[4], [6], [10] in the Manhattan model [15], [16], [23], [24] in the knock-knee model, and [8], [12]-[14] in the overlap model.

Unlike the above mentioned algorithms, most of which use some parameters derived from experiments, the algorithm presented in this paper approaches the solution in the Manhattan model in a greedy way, systematically based on simple concepts. The advantages of this algorithm are its simplicity and generality. The data structures used are vertical constraint graph, column density, and spans of nets which are the only information needed to assign wires for the nets. In addition, since the algorithm has a general nature, it treats cyclic and noncyclic constraints in the same way, and can be extended easily to the switchbox router, three-layer channel router, multilayer channel router, or even be applied in the overlap routing environment without much modification.

The algorithm proceeds in a track-by-track fashion. First, possible routings for each net in a certain track are calculated. Depending on channel density $d_{\text {max }}$ and structure of the vertical constraint graph, nets are then chosen to minimize the channel density $d_{\text {max }}$ or length of the directed longest path in the vertical constraint graph, and to maximize the total length of significant horizontal wires in a track through some priority. The performance of the algorithm is shown by experimental results. It successfully routes both Burstein's difficult switchbox problem and Deutsch's difficult example in the Manhattan model without any backtracking. This algorithm can be easily extended to solve other routing problems. For details on the extension of this algorithm see [25]-[28].

The remainder of this paper is organized as follows: some terms and definition of the problem are given in Section II; a framework for a class of heuristic algorithms is given in Section III; the description of our algorithm is given in Section IV, and its performance is given in Section V. In Section VI, we describe several extensions of our algorithm. Finally, the concluding remarks are given in Section VII.

## II. Preliminaries

A rectangle channel $C$ of length $l$ and width $w$ consists of 1) the set $V$ of grid points $(x, y)$ such that $x$ and $y$ are integers, 0 $\leq x \leq l+1$, and $0 \leq y \leq w+1$; and 2) the set $E$ of grid edges connecting points $(x, y)$ and ( $x^{\prime}, y^{\prime}$ ) whenever these points are at distance 1 from each other. A vertical (horizontal) grid line is a line formed by the grid edges connecting grid points ( $x, y$ ) with $x=i(y=i)$; furthermore if $i \neq 0$ and $i \neq l+1$ $(i \neq w+1)$, then we call such a grid line an ith column $(t r a c k)$ of the channel $C$. The horizontal (vertical) lines formed by edges connecting grid points with $y=0$ and $y=w+1(x=0$ and $x=l+1$ ), whose grid points are represented by ordered lists
$T(L)$ and $B(R)$, are called the top (left) and bottom (right) boundary of $C$, respectively.

Let $N=\left(N_{1}, N_{2}, \cdots N_{n}\right)$ be a collection of mutually disjoint subsets of boundary grid points (not including the corner points) of $C$. Each $N_{i}$ is called a net $i$, and the grid points in $N_{i}$ are called the terminals of net $i$. A routing of nets for $N$ is a collection $W=\left(W_{1}, W_{2}, \cdots W_{n}\right)$ of subgraphs of the channel grid such that all the terminals in $N_{i}$ are connected by edges in $W_{i}$. Each $W_{i}$ is called the wire for $N_{i}$. Given a channel grid $C$ and a set $N=\left(N_{1}, N_{2}, \cdots N_{n}\right)$ of nets, the Manhattan mode channel routing problem (MCRP) is to find $W=\left(W_{1}, W_{2}\right.$, $\cdots W_{n}$ ) in $C$ such that two distinct wires $W_{i}$ and $W_{j}$ cannot share a grid edge, and moreover, they can only share a grid point by crossing each other. Generally, terminals can be located on any boundary side of $C$. Such a MCRP is called a switchbox MCRP. A simpler version of a MCRP restricts terminals to be located on two opposite boundary sides, say, the top and bottom boundary sides of $C$. Such a MCRP is called a two-shore MCRP. The objective of a two-shore MCRP is to find a routing $W=\left(W_{1}, W_{2}, \cdots W_{n}\right)$ with a minimum number of tracks. In this paper, we first concentrate on the two-shore MCRP and then extend our algorithm to some related routing problems.

Let $l\left(N_{i}\right)\left(r\left(N_{i}\right)\right)$ be the $x$ coordinate value of the leftmost (rightmost) terminal of $N_{i}$. An obvious lower bound on the number of tracks necessary for a routing solution $W$ is:

$$
d_{\max }=\max \left\{d_{i} \mid 1 \leq i \leq l\right\}
$$

where $d_{i}=$ the number of nets $N_{j}$ such that $l\left(N_{j}\right) \leq i \leq r\left(N_{j}\right)$. Here $d_{i}$ is called the local density at column $i$, and $d_{\text {max }}$ is called the channel density.

In addition to the channel density, another condition that any routing solution must satisfy is that if $N_{i}$ contains a terminal at the top of column $k$, and $N_{j}$ contains a terminal at the bottom of column $k$ and $i \neq j$, then the horizontal wire segment of $W_{i}$ which connects with the top-side terminal $i$ through a vertical wire segment in column $k$ should be above the horizontal wire segment of $W_{j}$ which connects with the bottom-side terminal $j$ through a vertical wire segment in column $k$. This constraint can be characterized by a vertical constraint graph $G_{\mathrm{vc}}=\left(V_{\mathrm{vc}}\right.$, $E_{\mathrm{vc}}$ ), where $V_{\mathrm{vc}}=\left\{v_{i} \mid 1 \leq i \leq n\right\}$ such that $v_{i}$ corresponds to $N_{i}, e_{i j}=v_{i} \rightarrow v_{j} \in E_{\mathrm{vc}}$ iff there is a column $k$ such that $N_{i}$ has a terminal on the top of column $k$ and $N_{j}$ has a terminal on the bottom of column $k$. Normally, we say that $v_{i}$ is an ancestor vertex of $v_{j}$ if there exists a directed path from $v_{i}$ to $v_{j}$ in $G_{\mathrm{vc}}$. In this case, we also say that $v_{j}$ is a descendant vertex of $v_{i}$. In [11], it is shown that there exist MCRP instances with $d_{\text {max }}=2$ and the longest directed path of length $n-1$ in a vertical constraint graph that needs at least $\sqrt{2 n}$ tracks. In such an instance, almost every wire for each net $i$ must be assigned to more than one track, which is referred to as a dogleg for net $i$. This indicates that in some cases, the channel width is related to the structure of the vertical constraint graph.

## III. A Framework for a Class of Algorithms

Since the channel routing problem is $N P$-complete [17]-[19], it is necessary to develop heuristic algorithms for it. In this section we present a framework for a class of heuristic routing algorithms. An algorithm in this class is track oriented. Starting at the topmost track, it processes track after track downwards. The invariant part of this process is that once track $t$ is processed, by treating track $t$ as the top boundary of the channel,
we have a new MCRP. Since the combination of the wires above track $t+1$ and the routing solution for the new MCRP is a solution for the original MCRP, the operations for a single track, which defines the new MCRP, will critically determine the performance of the algorithm. The operations for the current topmost track $t$ can be divided into three phases.
i) Introduce a set $W_{H}$ of nonoverlapped horizontal wire segments in track $t$ such that after connecting the wire segments in $W_{H}$ with the related terminals on the top and bottom boundaries of the channel, the number of tracks required for the new MCRP is as small as possible.
ii) Introduce a set $W_{V}$ of vertical wire segments for each wire segment in $W_{H}$ when possible, such that $W_{H} \cup W_{V}$ and the routing solution of the new MCRP form a routing solution of the original MCRP.
iii) Define a new MCRP for the tracks below track $t$ by identifying a set of grid points in track $t$ and the bottom boundary of the channel as new terminals, and the set of columns that are available.

In the following subsections, we briefly describe the sperations needed to process the topmost track of a given channel $C$.

## A. Finding $W_{V}$ When $W_{H}$ Is Available

Let $T(k)$ and $B(k)$ represent the grid points on the top and bottom sides of the current channel in column $k$, respectively. We call a column $k$ an empty column if both of $T(k)$ and $B(k)$ are not terminals of any net. When $W_{H}$ is available, to complete the routing for the topmost track $t$ and construct the remaining MCRP, it is necessary to introduce a set $W_{V}=W_{V 1} \cup W_{V 2}$ of vertical wire segments, where $W_{V 1}$ is a set of vertical segments from the current top boundary (track $t-1$ ) to track $t$ for those columns $k$ with $T(k)$ being terminals, and $W_{V 2}$ is a set of vertical segments from track $t$ to the bottom boundary of the channel $C$. Finding $W_{V 1}$ is trivial. We can simply introduce a unit vertical segment that is incident at every terminal on the current top boundary. $W_{V 2}$ can be constructed in the following way: for a given column $k$, if $B(k)$ is a terminal of $N_{i}, T(k)$ is not a terminal of $N_{j}$ other than $N_{i}$ and $(k, t)$ is in $W_{i, t}$, where $W_{i, t} \in$ $W_{H}$ denotes the horizontal wire segments of $W_{i}$ in track $t$, then include a vertical wire segment from track $t$ to the bottom boundary in column $k$ into $W_{V 2}$. If $W_{V 2}$ is constructed in this way, then it is impossible that some net can never be completely connected by a wire without overlapping with other wires.

## B. Finding $W_{H}$ for the Current Topmost Track

There are many ways of finding $W_{H}$. As mentioned in the previous section, both the vertical constraint graph and channel density can be used to characterize the lower bound for the number of tracks needed for an MCRP instance. Hence, it is reasonable to use the vertical constraint graph and channel density as heuristics in choosing the wire segments in the current topmost track. We propose some useful concepts which may be applied to devise different routing algorithms. In the next section, we present one algorithm based on these concepts.

Generally, the vertical constraint graph corresponding to a problem instance may have cycles. Since among wires connecting a set of nets whose corresponding vertices in $G_{\mathrm{vc}}$ are in a cycle, at least one dogleg must be introduced; determining where a dogleg is to be introduced is very important to the total number of tracks used in the routing solution. Of course, we prefer to introduce horizontal wires that form a dogleg among those columns with lower densities. That is, when we use ver-
tical constraint graph $G_{v c}$ to guide the selection of horizontal wires for the current topmost track, we need to select a subset of nets which we do not want to use wires forming doglegs to connect them.
Such a selection can be based on an acyclic vertical constraint graph $G_{\text {avc }}$ obtained by deleting a minimal number of edges from $G_{\mathrm{vc}}$. Clearly, there is a unique $G_{\mathrm{vc}}$ for a given MCRP, and there can be more than one $G_{\text {avc }}$. Among these $G_{\text {avc }}$, we are particularly interested in a $G_{\text {avc }}$ constructed as follows:

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procedure \(A V C-G R A P H\) ( \(\left.G_{\text {avc }}=\left(V_{\text {avc }}, E_{\text {avc }}\right)\right)\)
    Let colno be the total number of columns for a given
        MCRP instance.
    Let \(c[1], c[2], \cdots, c[\) colno \(]\) be the sequence of columns
        such that \(d_{c[k]} \geq d_{c \mid k+1]}\), where \(1 \leq k \leq\) colno -1 .
    \(V_{\mathrm{avc}}=V_{\mathrm{vc}}, E_{\mathrm{avc}}=\varnothing\)
    for \(k=1\) to colno do
        \(i=T(k), j=B(k)\)
        if \(\left(i \neq 0\right.\) and \(j \neq 0\) and \(i \neq j\) and \(v_{i}\) is not a descen-
                dant vertex of \(v_{j}\) ) then \(E_{\text {avc }}=E_{\text {avc }} \cup\left\{v_{i} \rightarrow v_{j}\right\}\)
    endfor
end AVC-GRAPH.
```

The above process for constructing $G_{\text {avc }}$ tends to reserve edges in $G_{\text {vc }}$ connecting two nets that share columns with higher column densities. When $W_{H}$ is being constructed, we only consider those constraints which are present in $G_{\text {avc }}$. The missing constraints will be considered in the subsequent steps, processing lower tracks. Consequently, doglegs will likely occur among columns with lower densities. In determining which net is to be connected (or partially connected) in the current topmost track, a parameter level for each net is computed where $G_{\text {avc }}$ is available. The level of $N_{i}$ is defined as the length of the longest path from $v_{i}$ to its descendant vertices in $G_{\text {avc }}$. We identify a subset $N_{F}$ of $N$ as free nets, each of which is a net whose corresponding vertex in $G_{\text {avc }}$ does not have incoming edges.

In the Manhattan routing model, it is easy to see that for each wire segment in $W_{i, t}$, both endpoints should locate in columns $k$ such that $T(k)$ is not a terminal of $N_{j}$ other than $N_{i}$. Let

$$
E_{i}=\left\{k \mid \text { either } T(k) \text { is a terminal of } N_{i} \text { or a nonterminal }\right\} .
$$

Let the horizontal wire segment for $N_{i}$ in the top-most track with two endpoints located in column $k$, where $k \in E_{i}$, be the feasible wire for $N_{i}$, denoted as $f_{i}$. The set of nonoverlapped feasible wires is denoted as $H_{f}$. For an $f_{i} \in H_{f}$, it is possible that there exists a column $k$ such that $B(k)$ is a terminal of $N_{i}, T(k)$ is a terminal of $N_{j}$ other than $N_{i}$, and the left and right endpoints of $f_{i}$ are to the left and right of column $k$, respectively. In such a case, one cannot introduce a vertical wire segment in column $k$ into $W_{V_{2}}$. Let $C\left(f_{i}\right)$ denote the set of columns passed by $f_{i}$. For a given feasible wire $f_{i}$, if there exists no column $k \in C\left(f_{i}\right)$ such that $T(k)$ is a terminal other than a terminal of $N_{i}$ and $B(k)$ is a terminal of $N_{i}$, then we call such a feasible wire $f_{i}$ a safe wire for $N_{i}$, denoted as $s_{i}$. Let $H_{s}$ be the set of nonoverlapped safe wires. Clearly, for each $s_{i} \in H_{s}$, all the bottom-side terminals of $N_{i}$ in column $k$, where $k \in C\left(s_{i}\right)$, can be connected with $s_{i}$ through a vertical wire segment in column $k$ without causing any congestion problem in the new MCRP.
We may insist on finding an $H_{s}$ such that after processing the current topmost track, the remaining MCRP can be simplified so that the operations on subsequent tracks result in a routing
solution with a number as small as possible of tracks. Some heuristics can be used to choose the $H_{s}$.

$$
\begin{aligned}
& \text { Let } E_{i}^{*}=E_{i}^{1} \cap E_{i}^{2} \cap E_{i}^{3}, \text { where } \\
& \begin{aligned}
E_{i}^{1}= & \left\{k \mid k \in E_{i}, B(k) \text { is a terminal of } N_{j} \text { other than } N_{i}\right. \text { and } \\
& \left.\quad \text { level }\left(N_{i}\right)>\text { level }\left(N_{j}\right)\right\} \cup\left\{k \mid k \in E_{i}, B(k)\right.
\end{aligned} \\
& \left.\quad \text { is a terminal of } N_{i} \text { or } B(k)=0\right\} \\
& E_{i}^{2}=\left\{k \mid k \in E_{i}, k=l\left(N_{i}\right) \text { or } k=r\left(N_{i}\right) \text { or } d_{k}<d_{\max }\right\} \\
& E_{i}^{3}=\left\{k \mid k \in E_{i}, l\left(N_{i}\right) \leq k \leq r\left(N_{i}\right)\right\} .
\end{aligned}
$$

For each safe wire $s_{i}$, if both endpoints of $s_{i}$ are located in the columns in $E_{i}^{*}$, then such a safe wire is called an optimal wire for $N_{i}$, denoted as $o_{i}$. A set of nonoverlapped optimal wires is denoted as $H_{0}$. Now consider the relationship between the original MCRP and the new MCRP constructed by introducing an $H_{0}$. Since for each wire segment $o_{i}$ in $H_{0}$ both endpoints of $o_{i}$ are located in the columns in $E_{i}^{1}$, it is easy to verify that the following property holds.
P1) The longest path of $G_{\text {avc }}$ of the new MCRP will be less than or equal to that of the original MCRP if no cycle exists in " $G_{\mathrm{vc}}$.
Since for each wire segment $o_{i}$ in $H_{0}$ both endpoints of $o_{i}$ are located in the columns in $E_{i}^{2}$, it is easy to verify that the following property holds.
P2) The value of $\max \left\{d_{k}^{\prime} \mid k \in C\left(W_{i, t}\right), W_{i, t} \in H_{0}\right\}$ of the new MCRP is less than the $d_{\text {max }}$ of the original MCRP.

Since for each wire segment $o_{i}$ in $H_{0}$ both endpoints of $o_{i}$ are in $E_{i}^{3}$, it is easy to verify that the following property holds.

P3) The total span of the new MCRP is less than that of the original MCRP, where the total span is defined as $\Sigma_{i=1}^{n}\left(r\left(N_{i}\right)\right.$ $\left.-l\left(N_{i}\right)\right)$.

It is desirable to choose an nonoverlapped $H_{0}^{*}$ such that it is a set of safe wires satisfying properties P1), P2), and P3), and satisfying the following additional condition.

H1) When $H_{0}^{*}$ is chosen, the channel density $d_{\text {max }}$ of the new MCRP is less than that of the original MCRP.
To enforce ( $H 1$ ), in addition to the restrictions of choosing endpoints of each $o_{i}$ from $E_{i}^{*}$, it is necessary that for each column $k$ such that $d_{k}=d_{\max }$, there exists an $o_{i}$ passing through or ending at column $k$.
After $H_{0}^{*}$ is selected, it is possible that there is still some space available for the routing in the topmost track. A degenerated case is that $H_{0}^{*}=\varnothing$, that is, there does not exist a set of wire segments that satisfy the conditions for $H_{0}^{*}$. To fully use the current topmost track, one needs to introduce a set of wire segments into the unused gaps. There are two possibilities: either introducing a set $H_{f}^{*}$ of feasible wires or introducing a set $H_{s}^{*}$ of safe wires. The criterion for choosing an $H_{s}^{*}$ or $H_{f}^{*}$ is to simplify the remaining MCRP as much as possible. Since feasible wires have less restrictions than safe wires, more flexibilities can be provided by feasible wires when simplifying the problem is concerned. There are many possible ways of choosing $H_{f}^{*}$. Here we discuss one way of introducing $H_{f}^{*}$.

As mentioned in the previous section, both the vertical constraint graph and the channel density characterize the complex-
ity of an MCRP instance. Again, we use both of $G_{\text {avc }}$ and $d_{\text {max }}$ as heuristics in choosing $H_{f}^{*}$. If we cannot decrease $d_{\text {max }}$ of the MCRP through the current topmost track, we choose to change the structure of the vertical constraint graph. From [11], we know that the length of the longest path of $G_{\mathrm{avc}}$ is an important factor for determining the lower bound of the channel width for a given MCRP; on the other hand, from [1] we also know that for a given MCRP, if there are no vertical constraints (i.e., every net is a free net), then the optimal routing solution can be easily achieved. Subject to possible existence of $H_{0}^{*}$, we can select $H_{f}^{*}$ in the following way: if the length of the longest path in $G_{\text {avc }}$ is greater than or equal to $d_{\text {max }}$, then introduce a set $H_{f}^{*}$ of wire segments to minimize the length of the longest path of $G_{\mathrm{avc}}$; otherwise a set $H_{f}^{*}$ of wire segments is introduced to maximize the number of free nets that can be created. Thus the set $W_{H}$ of nonoverlapped horizontal wire segments in the current topmost track is $H_{0}^{*} \cup H_{f}^{*}$.

## C. Defining the New MCRP

After the $W_{H}$ and $W_{V}$ are introduced, the next step is to identify a set of grid points in track $t$ and on the bottom boundary of the channel as terminals of the new MCRP below track $t$. For each $N_{i}$ such that there is no corresponding wire in $W_{H}$, all terminals of $N_{i}$ located in track $t-1$ are shifted downward to track $t$ as the terminals of $N_{i}$ in the new MCRP and the terminals of net $N_{i}$ located at the bottom boundary of channel remain as the terminals of $N_{i}$ in the new MCRP. If all terminals of $N_{i}$ are completely connected by the wires in $W_{i, t} \cup W_{V}$, then $N_{i}$ will not be considered in the operations for the tracks below. For each $W_{i, t}$ in $W_{H}$ such that $N_{i}$ is not completely connected by the wires in $W_{i, t} \cup W_{v}$, we need to identify a set of new nets with terminals in track $t$ and on the bottom boundary of the channel. In such a case, net $N_{i}$ may be split into at most $\left|W_{i, t}\right|+1$ new nets in the new MCRP, where $\left|W_{i, t}\right|$ is the number of horizontal wire segments in $W_{i, r}$. The basic idea for net splitting is as follows: all the terminals of $N_{i}$ in the gap between each pair of adjacent wire segments in $W_{i, t}$ can be treated as a new net in the new MCRP. The objective of the net splitting is to generate a new MCRP with minimum total span and minimum channel density $d_{\max }$. It is possible that there are more nets in the new MCRP than the nets in the original MCRP; however, if we define the new nets carefully, as the use of concept of net splitting, then the new MCRP problem will have a much simpler structure.

There are several additional issues which must be considered in defining a new MCRP. For example, a wire segment in $W_{i, 1}$ can be a feasible wire, a safe wire, or an optimal wire. Wires of different types may need different treatments. Another aspect we must consider is that a column cannot always be available in the process of routing. Once a vertical wire segment in a column $k$ is introduced into $W_{V 2}$ to connect a bottom-side terminal of $N_{i}$, the section of column $k$ from track $t$ downward is fully occupied. Thus column $k$ must be marked unavailable for the use by wires connecting the terminals of $N_{j}$ other than $N_{i}$. For simplicity, we will not go into details on these issues.

## D. Designing a Channel Routing Algorithm

Based on the framework of a class of track oriented greedy channel routing algorithms discussed so far, we can design different heuristic algorithms. Among the three phases, the operations corresponding to the constructions of $W_{H}, W_{V}$, and a new

MCRP, for the current topmost track, the way of selecting a set $W_{H}$ of horizontal wire segments is a determining factor in obtaining a routing solution with a smaller number of tracks. There are not many choices for the selection of $W_{V}$ that exist. Also, options for defining a new MCRP, when $W_{H}$ and $W_{V}$ are present, are limited.

It is important to note that the feasible wires, safe wires, and optimal wires form an interesting hierarchy. Since an optimal wire is also a safe wire and a safe wire is also a feasible wire, it seems that by setting optimal wires with a priority higher than safe wires and safe wires a priority higher than that of feasible wires, better routing solutions can be always possible. Unfortunately, this is not always true. Since a MCRP instance can be extremely complex, global information about an MCRP instance must be examined when operations for a single track are considered. The vertical constraint graph and the channel density capture some of these global information and that is why they can be used for selecting $W_{H}$. However, there are other factors to be considered in determining how these pieces of information are used to guide the operations for a single track so that a better solution can be achieved. The notions that may be useful are not limited to those given in this section. Concepts similar to feasible wires, safe wires, and optimal wires can be defined by adding or dropping some conditions. Our proposed framework for the channel routing algorithms is general and powerful enough to allow us to obtain algorithms for the MCRP problem and several related routing problems, as shown in the remaining sections of this paper.

## IV. AN AlGORITHM FOR MCRP

In this section we present an algorithm for the MCRP problem. The design of this algorithm directly follows the framework given in the previous section. Since finding the $W_{H}$ is the major issue in the framework, the presentation of our algorithm will focus on constructing the $W_{H}$ for each track. Our algorithm constructs $W_{H}$ in the following way: if there exists more than one $H_{0}^{*}$, then we choose a $H_{0}^{*}$ which minimizes the total span of the new MCRP; if a $H_{0}^{*}$ cannot be found, then we choose a nonoverlapped $H_{f}^{*}$ as discussed in the previous section; if more than one such $H_{f}^{*}$ exists, the one which minimizes the total span of the new MCRP is selected.

## Algorithm MCRP-ROUT

1) Construct the $G_{\mathrm{avc}}$ using procedure $A V C-G R A P H$, and assign the level of each net.
2) Do the following operations track by track downwards until all nets are routed.
a) Find the longest optimal wire $W_{i, t}$ for each net $i$.
b) Select the set $H_{0}$ of nonoverlapped optimal wires $W_{i, r}$, from the high density columns to lower density columns according to the following priorities: whenever possible a) the wire of free net is selected; otherwise b) the wire of maximal span is selected.
c) If the selected $H_{0}$ is not a $H_{0}^{*}$ and an alternative $H_{0}$ exists, then go to step b) and rechoose the $H_{0}$; if the selected $H_{0}$ is a $H_{0}^{*}$ then go to step d); if none of $H_{0}$ is an $H_{0}^{*}$ then let $H_{0}^{*}$ $=\varnothing$ and go to step d).
d) Select $H_{f}^{*}$.
e) Let $W_{H}=H_{0}^{*} \cup H_{f}^{*}$. Construct $W_{V}$ from $W_{H}$. Define the new MCRP. If there exists a net in the new MCRP that is


Fig. 1. Acyclic vertical constraint graph.
not completely connected, then update $G_{\mathrm{avc}}$ and densities; advance to next track, and go to step a).
3) Minor adjustment to reduce the numbers of bends (vias) and the wirelength of the routing solution.

## end MCRP-ROUT.

Let us use a simple example to demonstrate the above algorithm MCRP-ROUT. For a given MCRP in Fig. 2, in step 1), we apply the procedure $A V C-G R A P H$ to construct the $G_{\text {avc }}$ as shown in Fig. 1, where numbers inside the circles and rectangles represent the net numbers and related levels, respectively; solid lines represent acyclic vertical constraints, and dotted lines represent the cyclic vertical constraints, which are ignored in $G_{\text {avc }}$.

In step 2.a), all longest optimal wire segments $W_{i, t}$ constructed from the candidate endpoints located in $E_{i}^{*}$ are shown in Fig. 2, where dots represent the candidate endpoints in $E_{i}^{*}$.

In step 2.b), we select an $H_{0}^{*}$ from all possible optimal wire segments constructed in step 2.a). The details are shown as follows: in Fig. 2, we check the left highest density column 9, where $d_{9}=d_{\max }$, and find four wires ( $W_{1, t}, W_{2, t}, W_{3, t}$, and $W_{7, t}$ ) pass this column. From Fig. 1, we know only $N_{2}$ and $N_{3}$ are in $N_{F}$. Since the span of $W_{3, t}$ is greater than that of $W_{2, t}$, $W_{3, t}$ is selected. After wire $W_{3, t}$ is selected, the wires ( $W_{2, t}$, $W_{5, t}, W_{7, t}, W_{8, r}$, and $W_{10, t}$ ) are ignored, and wires ( $W_{1, t}, W_{4, r}$, and $W_{9, t}$ ) are partially chopped off. Then we check the left highest density column $16\left(d_{16}=6\right)$ which is passed by the remaining candidate wire segments. Since only the wire segment of $W_{4, t}$ passes this column, the wire segment of $W_{4, t}$ from column 16 to column 18 is selected. Since the wire segments of $W_{1, t}$ and $W_{9, t}$ overlap with the selected wire segment of $W_{4, t}$, both wire segments can also be ignored. Hence, $H_{0}$, which is also an $H_{0}^{*}$ in this case, selected in track $t$ will include the wire segment of $W_{3, t}$ from column 4 to column 15 and the wire segment of $W_{4, t}$ from column 16 to column 18 .
Since the selected $H_{0}$ is an $H_{0}^{*}$ and no feasible wires exist in the unused space, it is easy to see that $H_{f}^{*}=\varnothing$ and $W_{H}$ is an $H_{0}^{*}$.

The consideration for the limited backtracking in step 2.c) is obvious. Since if a column has the highest density and is not used for some optimal wire, it is very likely that the total number of tracks in the final solution is larger than it should be just because an $H_{0}^{*}$ is not used. Thus the backtracking in step 2.c) for finding an $H_{0}^{*}$ is necessary for obtaining better solutions, although considerable running time may be required to search for an $H_{0}^{*}$. Since the algorithm always routes the nets which pass the high density columns first, in most cases, it is very unlikely that backtracking capability is needed in this step. For example, when our algorithm is applied to both Burstein's difficult switchbox and Deutsch's difficult example, no backtracking occurs. However, when the given problem is more difficult, the backtracking capability is a powerful tool to reach a good solution.


Fig. 2. The set of all the longest safe wires $W_{i, 1}$ for the topmost track.

Since the main idea of this algorithm is to fully utilize one track before going to the next one, it is not always desirable to assign wires passing through high density columns as soon as possible. In fact, in some cases delaying assigning wire segments through high density columns may result in better overall routing performance in terms of wirelength and number of vias. That is why, in the final step, adjustment operations are necessary to improve the routing result. For simplicity, we omit the details of these operations.

## V. Performance

We applied our algorithm MCRP-ROUT to many problem instances. It turns out that our algorithm generates optimal routing solutions in most cases. For example, for the Deutsch's difficult example [3], we achieved a routing solution with 19 tracks, which is equal to the lower bound, as shown in Fig. 3. It is worth mentioning that although minimizing the wirelength and via number is not as important as minimizing the number of tracks emphasized in designing our algorithm, the total wirelength of 5004 and via number of 333 in this solution are better than those achieved by hierarchical wire routing [10], which is the only known algorithm that achieves the lower bound of channel width for this problem instance in the Manhattan model. We also applied our algorithm to the Burstein's difficult channel [7]. As shown in Fig. 4, the solution by our algorithm uses 6 tracks without allowing wires to go beyond the leftmost and rightmost nonempty columns. We believe this is the optimal solution in terms of tracks used in the Manhattan model.

It is easy to see that the running time of the algorithm is dominated by the operations for choosing $H_{0}^{*}$ and $H_{f}^{*}$ in each track. Let $c$ be the number of columns and $n$ be the number of nets. Clearly, sorting the columns in the order of nondecreasing column density can be done in $O(c \log c)$ time. To obtain $H_{0}^{*}$, we need to find the longest optimal wire for each net. Finding the longest optimal wire $W_{i, t}$ for net $N_{i}$ takes $O(c)$ by a linear scanning of the columns from left to right. Thus finding the longest optimal wires for all the nets requires $O(n c)$ time. Choosing the $H_{0}^{*}$ from these optimal wires can be done in $O\left(c d_{\text {max }}\right)$ time since in each column at most $d_{\text {max }}$ wires need to be considered. Therefore, the total time for choosing $H_{0}^{*}$ takes $O((\log c+n$ $\left.+d_{\max }\right) c$ ). For the purpose of deleting a certain vertical constraint, each wire in $H_{f}^{*}$ incident at the top boundary of the channel should find a column to dogleg. So choosing $H_{f}^{*}$ takes $O\left(c^{2}\right)$. Normally, after $H_{0}^{*}$ is chosen, only a small portion of


Fig. 3. Deutsch's difficult example.

columns need to be considered for $H_{f}^{*}$. In this case, the constant factor for $O\left(c^{2}\right)$ will be small. The resulted time complexity for the whole procedure is $O\left(\left(\log c+n+d_{\max }\right) c d_{\text {max }}+c^{2} k\right)$, where $k$ is the extra track needed for the final routing beyond the $d_{\text {max }}$. In above analysis, we did not consider backtracking which takes $O\left(n c d_{\text {max }}\right)$ for each track, when finding $H_{0}^{*}$ from high density columns to low density columns always finds the $H_{0}^{*}$ satisfying $(H 1)$ at the first time if it exists. Since not enough evidence shows that such a mechanism is sufficient to find such $H_{0}^{*}$, the backtracking routine is included.

## VI. Extensions of the Algorithm MCRP-ROUT to Other Problems

In this section, we briefly discuss several extensions of our algorithm MCRP-ROUT. The detailed results will be reported in subsequent papers.

## A. Manhattan Switchbox Problem

Our algorithm MCRP-ROUT can be extended to the switchbox problem easily. Since that is a switchbox problem, terminals can be located on any of four boundaries of the rectangular channel; the definitions of vertical constraint graph $G_{\mathrm{vc}}$, acyclic vertical constraint graph $G_{\text {avc }}$, feasible wires, safe wires, and optimal wires need to be slightly modified. Then a modified version of algorithm MCRP-ROUT for the switchbox problem can be designed. The modified MCRP-ROUT connects nets in a track-by-track fashion. By its greedy feature of fully utilizing a track before proceeding to the next track, terminals on the left and right sides of the channel should be connected as soon as possible so that more of the space in the remaining tracks can be available. Consequently, a higher success rate of routing inside the given channel area can be expected.
We have modified algorithm MCRP-ROUT to obtain an algorithm for the switchbox problem. We applied the modified version of MCRP-ROUT to Burstein's difficult switchbox [10] and successfully found a solution without backtracking. The result is shown in Fig. 5.

## B. Channel Routing in Two-layer Overlap Model

Currently, our algorithm is implemented under the Manhattan model, i.e., all the horizontal wire segments run in one layer, and all the vertical wire segments run in the other. To adapt our algorithm to the overlap model, we must allow horizontal wire segments or vertical wire segments to run in different layers with overlaps. We can simply modify the definitions of feasible wires, safe wires, and optimal wires in a way that nonoverlap restrictions are released, with all other features re-


Fig. 5. Burstein's difficult switchbox.


Fig. 6. Burstein's difficult channel in overlap model.
maining unchanged. In the Burstein's difficult channel [7], all previous works either add one or two empty columns in the middle to achieve the routing with five or six tracks [7], [8], or allow wire overlaps to achieve the routing with four tracks [12]. Applying our preliminary modified algorithm to this problem, the routing solution with only three tracks is achieved. The result is shown in Fig. 6.

## C. Channel Routing with More Than Two Layers

As a two-layer channel routing problem, there are two versions of the problem of routing with more than two layers. The first version does not allow wire segments in different layers to overlap. Thus two wire segments can only share a grid point only by crossing each other or by forming a knock-knee. Usually, this version of multilayer channel routing is called knockknee mode channel routing. Typically, knock-knee mode channel routing algorithms consist of two phases. In the first phase, a layout $W=\left(W_{1}, W_{2}, \cdots, W_{n}\right)$ is constructed, where $W_{i}$ is a subgraph of the channel grid that connects all terminals of $N_{i}$ and no two distinct $W_{i}$ and $W_{j}$ share a grid line segment. Such a layout is also called a planar layout. In the second phase, each wire segment in a planar layout $W$ is assigned to a layer such that any two wire segments belonging to the wires connecting different nets do not share a grid point in the same layer. It is well kno vn that any planar layout $W$ can be wired in four layers [20] anc the problem of determining whether $W$ is three-layer wirable is $N P$-complete [21]. The necessary and sufficient conditions for constructing a three-layer wiring of $W$ are given in
[22]. The only modification needed to adapt our algorithm MCRP-ROUT to the knock-knee mode channel routing is to allow wires sharing a grid point by knock-knees. The second version of problem of routing with more than two layers is the one that allows wires in different layers to overlap not only by crossings and knock-knees. Techniques developed for (27) can be generalized to cope with layers more than two. For details of this section, see [26]-[28].

## VII. Concluding Remarks

In this paper, as a framework for a class of heuristic routing algorithms, a general approach for the channel routing problem is presented. As an example, we showed how to follow this approach to design a particular routing algorithm MCRP-ROUT for the two-shore Manhattan channel routing problem. The performance of this algorithm has been tested on many problem instances and good results have been obtained. Applying our algorithm MCRP-ROUT to the benchmark Deutsch's difficult problem and Burstein's difficult problem, we obtained routing solutions of 19 tracks and 6 tracks, respectively. These solutions are either optimal or believed optimal. It should be mentioned that algorithms similat to MCRP-ROUT can be easily developed by following the same lines and using different heuristics. For example, for the current topmost track, there are many ways to select $W_{H}$. Instead of vertical constraint graph and channel density, other heuristics may be used.
We also showed that track oriented greedy algorithms can be modified to solve other channel routing problems. As examples, we described how to modify algorithm MCRP-ROUT to solve the Manhattan switch-box problem and channel routing problems in the overlap and knock-knee models. By our preliminary experiments, the modified algorithms have good performance and show strong potential to out perform the existing algorithms.
Many refinements can be incorporated into our framework and algorithm MCRP-ROUT. There is a tradeoff between the quality of the routing solutions and the computing resources required for the more complicated algorithms. Our framework provides the flexibility for running an algorithm to achieve better routing performance.

## Acknowledgment

The authors wish to thank all the reviewers for their comments, which improved their presentation of this paper.

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