COT 5407 Introduction to Algorithms

Homework 5

DUE: Thursday, December 1, 2011

I would like to strongly reiterate that all submissions are to be your own work and must be typeset. Joint work and work that does not properly cite sources will recieve no credit. Handwritten submissions will NOT be accepted.

- 1. A double-ended queue is a data structure that supports insertion and deletion at both ends of the queue. Suppose we add the findMin operation to the double-ended queue; findMin returns (but does not remove) the smallest item in the double-ended queue. Design a data structure that implements the double-ended queue in O(1) amortized cost for all operations. You must prove your time bound.
- 2. Let A be an N-by-N matrix of zeros and ones. A submatrix S of A is any group of *contiguous* entries that form a square. Design an $O(N^2)$ algorithm that determines the size of the largest submatrix of ones in A. For instance, in the matrix that follows, the largest submatrix is a 4-by-4 square.

- 3. Given an *undirected* graph G = (V, E), and an integer K, the **ARC-DELETION** problem is that of determining if there is a set of K edges whose deletion breaks all cycles. Either give a polynomial-time algorithm or prove that ARC-DELETION is NP-complete.
- 4. A coin collector has an opportunity to purchase N coin collections $S_1, S_2, ..., S_N$. Some collections may contain coins in common with others. The collector wants to buy at least K collections out of the N, but **must avoid duplicates**. The **COIN COLLECTOR'S PROBLEM** is whether there is a selection of at least K mutually disjoint collections out of the N. Either give a polynomial-time algorithm or prove that COIN COLLECTOR'S PROBLEM is NP-complete.
- 5. CLRS Problem 34-1 (Independent Set), page 1101.
- 6. CLRS Problem 34-3 (Graph Coloring), page 1103.